

Chapter 5

Ambient noise correlation on the Amery Ice Shelf, East Antarctica

5.1 Abstract

The structure of ice shelves is important for modeling the dynamics of ice flux from the continents to the oceans. While other, more traditional techniques provide many constraints, passive imaging with seismic noise is a complementary tool for studying and monitoring ice shelves. As a proof of concept, here we study noise cross-correlations and auto-correlations on the Amery Ice Shelf, East Antarctica. We find that the noise field on the ice shelf is dominated by energy trapped in a low velocity waveguide caused by the water layer below the ice. Within this interpretation, we explain spectral ratios of the noise cross-correlations as P -wave resonances in the water layer, and obtain an independent estimate of the water-column thickness, consistent with other measurements. For stations with low levels of incoherent noise, noise auto-correlations also provide similar results. High-frequency noise correlations also require a 50-m firn layer near the surface with P -wave velocity as low as 1 km/s. Our study may also provide insight for future planetary missions that involve seismic exploration of icy satellites such as Titan and Europa.

5.2 Introduction

Ice shelves are important interfaces between grounded ice sheets and oceans, and contribute to the majority of grounded ice loss either through basal melting or iceberg calving. Accurate modeling of ice shelf dynamics (e.g., sub-ice circulation and ice flow modeling) requires high-resolution ice drafts and water-column thicknesses, which are usually poorly constrained for ice shelves. Currently, ice drafts and water-column thicknesses are constrained mostly from digital elevation modeling (Fricker et al., 2005), tidal modeling (Hemer et al., 2006; Galton-Fenzi et al., 2008), and sparse active seismic surveys and drillings (Craven et al., 2009; McMahon and Lackie, 2006). It is therefore of interest whether other methods can contribute additional and/or better constraints. One method that has received little attention in cryospheric studies is passive imaging with ambient seismic noise. Passive imaging can be applied over large areas at a low cost and without direct sampling, and has been widely used to study crustal structure around the globe in recent years (e.g., Shapiro et al., 2005; Yao et al., 2006; Lin et al., 2008), including in Antarctica (Pyle et al., 2010). However, most of these studies are located in the interior of the continent and concentrate on the structure of the crust or upper mantle using long-period ($T > 5$ s) surface waves. To our knowledge, there has not been any report of small-scale noise correlation on ice shelves. The reason for this may be twofold. First, due to the harsh environment and difficult logistics, there is little continuous data available on ice shelves. Second, the ice-water-rock setting with a strong low velocity layer is significantly different from ordinary crustal structure and could affect the convergence and interpretation of noise cross-correlation functions (NCFs). To address the question of what can be gained with such an approach, we apply noise correlation methods to the Amery Ice Shelf on the east coast of Antarctica (Figure 5.1A), where a number of seismic instruments were deployed for multiple years near the tip of the Loose Tooth Rift

system to monitor its growth (Bassis et al., 2005; Bassis et al., 2007; Fricker et al., 2005; Figure 5.1B). Near the site, the thicknesses of the ice and water layers are about 300m and 500m, respectively (Fricker et al., 2005; Galton-Fenzi et al., 2008; Figure 5.2). One question we explore is whether we can retrieve this structural information from noise correlations.

This experiment also serves as a proof of concept for planetary applications of the noise correlation method on icy satellites. For example, a variety of evidence suggests that there may exist subsurface liquid oceans on Europa (e.g., Carr et al., 1998; Kivelson et al., 2000) and Titan (e.g., Tobie et al., 2006; Lunine and Lorenz, 2009; Castillo-Rogez and Lunine, 2010). The thicknesses of the ice and liquid layers, which are important for understanding icy satellite dynamics, are still uncertain. Different kinds of seismic experiments have been proposed to improve estimates in future missions (e.g., Kovach and Chyba, 2001; Lee et al., 2003; Panning et al., 2006; Jackson et al., 2010; Tsai, 2010a). In particular, the emerging noise correlation method is attractive for planetary missions because it potentially provides surface-wave (e.g., Shapiro et al., 2005) and body-wave (e.g., Zhan et al., 2010; Poli et al., 2012; Lin et al., 2013) Green's functions without seismic events. For example, Larose et al. (2005) applied the noise correlation method to lunar data and constrained the near-surface (top 10-meter) seismic structure. Recently, Tibuleac and von Seggern (2012) and Gorbato et al. (2013) also reported reflected crustal phases from noise auto-correlations on individual stations. Because it is difficult to deploy more than one seismic station in planetary missions, the noise auto-correlation method might be more practical than the cross-correlation method. With a similar ice-liquid-solid structural setting, the Amery Ice Shelf is an ideal test ground for the application of noise cross-correlation and auto-correlation methods on icy satellites.

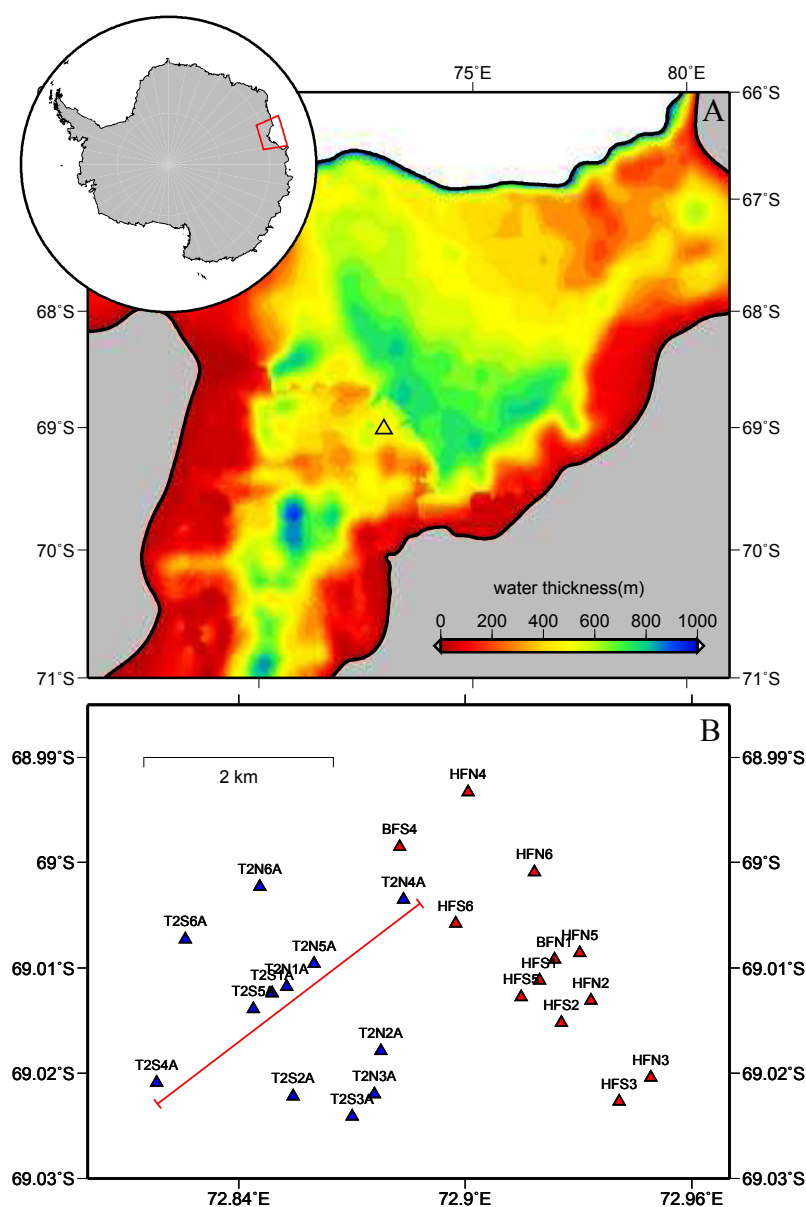


Figure 5.1: (A) Map of the Amery Ice Shelf and water-column thickness. The triangle marks the location of the seismic deployment. (B) Station distribution map. Blue triangles and red triangles show the stations deployed in 2005 and 2007, respectively. The red line denotes the profile whose NCFs are shown in Figure 5.3. In both years, the instruments surround the same ice area, but the ice has advected ~ 2 km (to the NE) in the 2 years between deployments.

5.3 Data and Method

Figure 5.1B shows the locations of the three-component short-period (1-10 Hz) instruments deployed during the 2005 and 2007 field seasons. Both campaigns (Bassis et al., 2007) were active for about 2 months during the Antarctic summer. Because of the different environment and frequency band from most noise correlation studies, we modified some of the common procedures (e.g., Bensen et al., 2007; Zhan et al., 2011) to calculate the 9-component NCFs (E, N, Z with E, N, Z) for all station pairs. We first remove instrumental responses and cut the data into 10-minute segments. Because signals from earthquakes are weak in the frequency band of 1 to 10 Hz, here we do not use temporal normalization to remove earthquakes. To preserve the amplitude spectrum, especially for auto-correlations, we also do not apply spectral whitening to the waveforms. The two stations' waveforms are cross correlated for each segment and then stacked with normalized maximum amplitudes. The use of very short 10-minute segments and normalized stacking achieves the equivalent of the temporal normalization used in most noise correlation studies to remove earthquakes, and may be important in the presence of occasional icequakes.

5.4 Noise cross-correlations in time domain

Although the elastic structure of the ice shelf near the site can be estimated with other methods (e.g., Vaughan, 1995), the NCFs produced here provide the first direct in situ measurement of ice shelf elastic structure. Elastic structure is inferred from the NCFs by comparing the observations with synthetic Green's functions produced for various assumed structures using a frequency-wavenumber method (Zhu and Rivera, 2002) to compute the synthetic Green's functions due to a surface point force. Using borehole measurements, Craven et al. (2009) show that the ice shelf consists of a ~50 m firn layer on top of a ~250 m continental meteoric and marine ice layer.

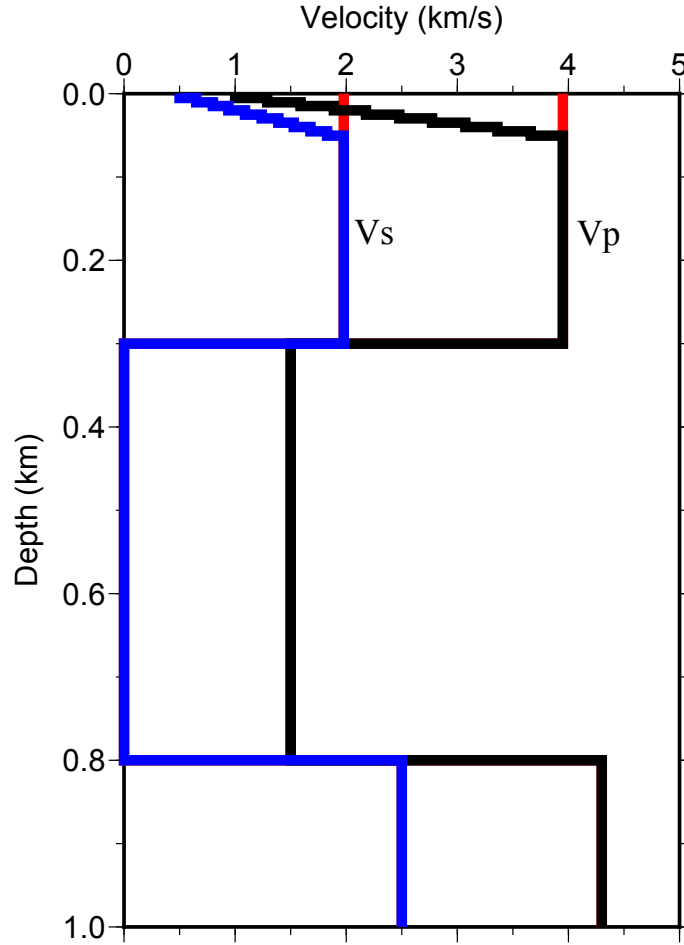


Figure 5.2: 1D P - and S -wave velocity models used to compute synthetic Green's functions. Differences between the two 1D models with or without the top 50-m firn layer are highlighted by the red segments.

Following Wittlinger and Farra (2012), we set the V_p and V_s to be 3.95 km/s and 2 km/s, respectively, for both the meteoric and marine ice layer. The velocities in the firn layer are poorly constrained and V_p can be as low as 0.5 km/s (Albert, 1998), and we therefore test two different models, one without a slow firn layer, and one with a slow layer of constant gradient and V_p/V_s ratio of 2 (Figure 5.2). For the latter model, we adjust the absolute V_p on the surface to best fit the seismic data.

We first compare the NCFs along a NE-SW profile (red line in Figure 5.1B) with

the synthetic Green's functions in the 5-10 Hz frequency band (Figure 5.3A, 5.3B). We rotated the EN-EN NCFs into radial-radial (RR) components and summed the positive and negative sides. We see clear Rayleigh waves in the NCFs (dashed line in Figure 5.3A) propagating at a speed of about 1.5 km/s, much slower than the synthetic Rayleigh waves of the 1D homogeneous ice model (without a slow firn layer), as shown in red in Figure 5.3B. To fit the observed Rayleigh waves, we adjust the 1D model with a slow firn layer to have a surface V_p of 1 km/s and plot the synthetics in black in Figure 5.3B. We note that if a more complex velocity structure were allowed, there would be tradeoffs between the various parameters, including the thickness of the slow layer and its velocity anomaly.

In the 5-10 Hz frequency band, the observed Rayleigh waves are only sensitive to depths shallower than about 100 m, significantly shorter than the ice thickness, and therefore do not have sensitivity to the ice-water interface. To sample the interface, we need to study NCFs at lower frequencies. For the same station pairs at 1-5 Hz, the synthetic Green's functions are similar for the two 1D models because they are only different in the thin top layer. However, we find that the NCFs do not resemble these synthetic Green's functions (Figure 5.3C, 5.3D). In fact, the observed NCFs clearly cannot be represented by a Green's function because they violate causality. The dashed line in Figure 5.3D marks the onset of the synthetics, and the P, S and surface waves must arrive after this dashed line due to causality. On the other hand, the observed NCFs are acausal, with most of their energy arriving before or around the same time as the dashed line shown in Figure 5.3C. This comparison is also true for other station pairs. Therefore, it is not possible to interpret the NCFs solely as being Green's functions between stations, and we must rely on an alternative interpretation of the NCFs to retrieve further structural information.

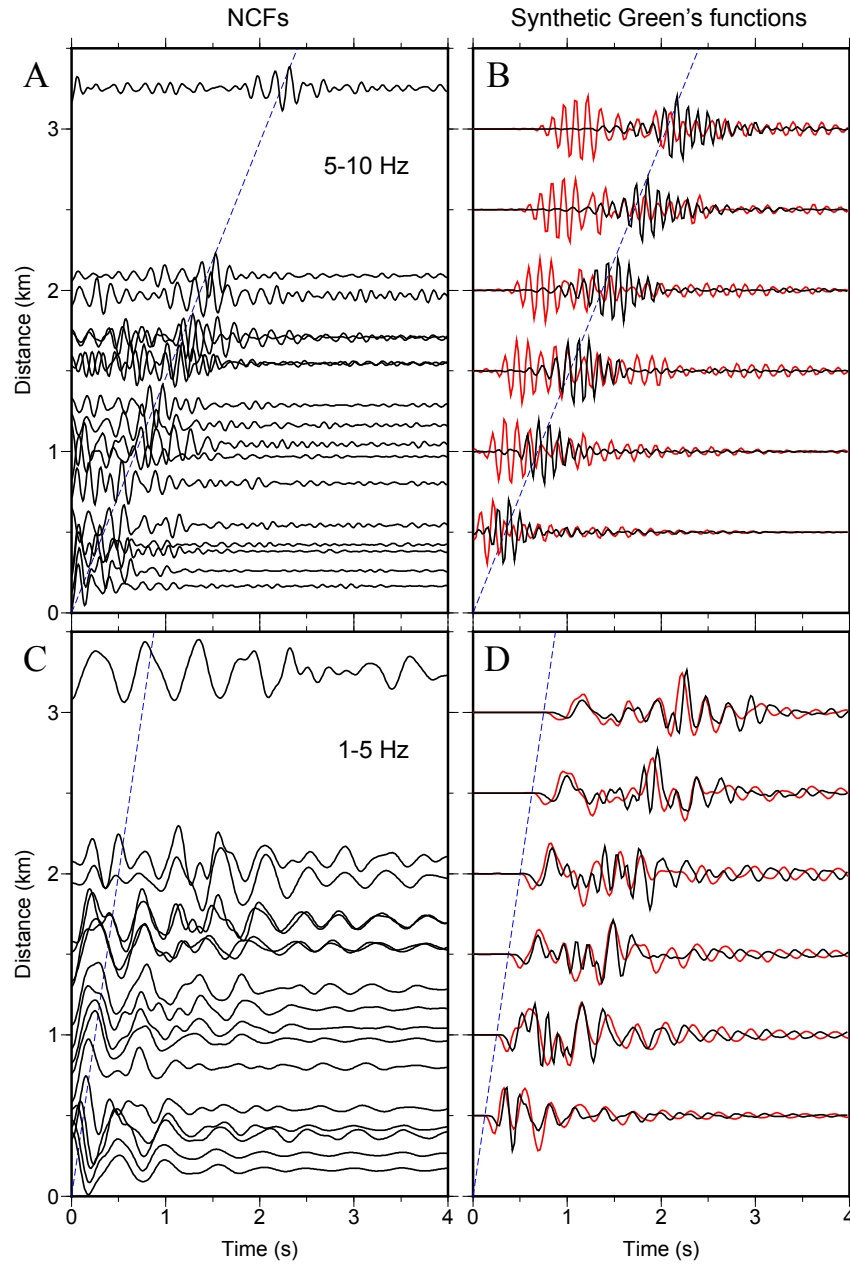


Figure 5.3: NCFs in the time domain (A, C) and comparisons with synthetic Green's functions (B, D). The top and bottom panels are for the frequency bands 5-10 Hz and 1-5 Hz, respectively. In (B, D), the red and black synthetics are computed with the 1D models without and with the firm layer, respectively.

5.5 Spectral ratios of noise cross-correlations

Although the 1-5 Hz NCFs in the time domain are difficult to interpret, we find that the spectral ratios of NCFs on different components still contain useful information about the velocity structure. With the three-component stations, we have 9 components of the NCFs (ZNE-ZNE) for each station pair. We first estimate the NCF amplitude spectra for all components and then take their spectral ratios with the ZZ component (ZZ/XY, where X and Y can be Z, N, or E). Figure 5.4 shows the average spectral ratios over all station pairs for each component in 2007. For all the components (except ZZ/ZZ which is 1 by definition), we observe regularly spaced peaks at about every 1.5 Hz up to about 6 Hz. These peaks are stronger on the components involving only East or North (Figs. 5.4E, F, H, and I). The observed peaks in the NCF spectral ratios are approximately equally spaced in frequency (a phenomenon typical for resonating systems), and imply more coherent waves on the vertical components than the horizontal components at these frequencies.

We interpret the observed peaks in Figure 5.4 as *P*-wave resonances in the water layer (Figure 5.5). As shown in Figure 5.2, the water layer sandwiched between the ice and rock layers is a strong low-velocity waveguide with little attenuation (high *Q*). Therefore the water layer traps seismic waves and creates a diffuse wavefield inside it. The *P*-wave critical angle is about 22° for the ice-water interface and even smaller ($\approx 20^\circ$) for the water-rock interface. Therefore, waves in the water layer with incident angles larger than 22° will be completely reflected back to the water and are not recorded on the free surface under the assumption of geometrical ray theory. Waves with incident angles (θ in Figure 5.5) smaller than the critical angle can leak into the ice layer and reach the stations at the free surface. Due to the slow firn layer on top, the transmitted *P* waves will bend steeper toward the surface, and reach the stations with incident angles smaller than the $\theta \leq 22^\circ$ in the water layer (Figure 5.5).

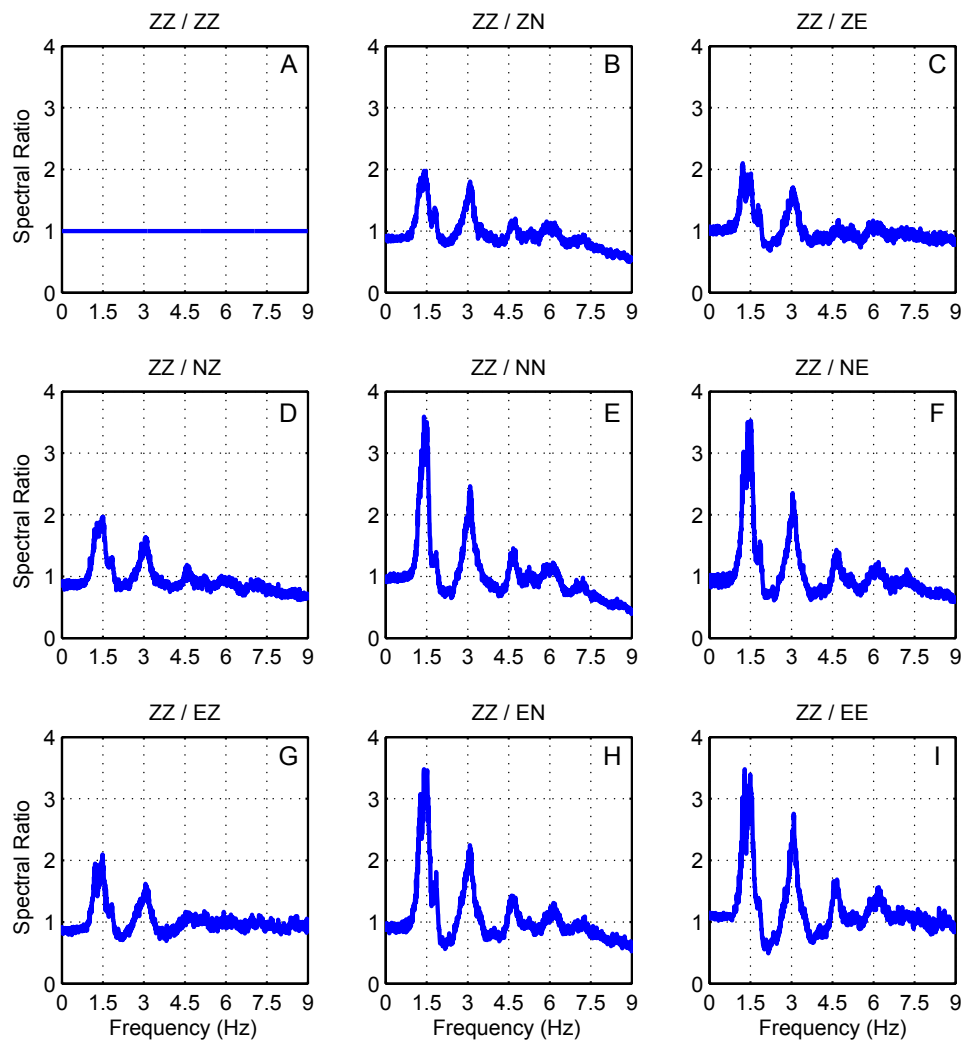


Figure 5.4: Average NCF spectral ratios for the year 2007. The title of each panel shows the components in format ZZ/XY, where X and Y can be one of E, N, Z.

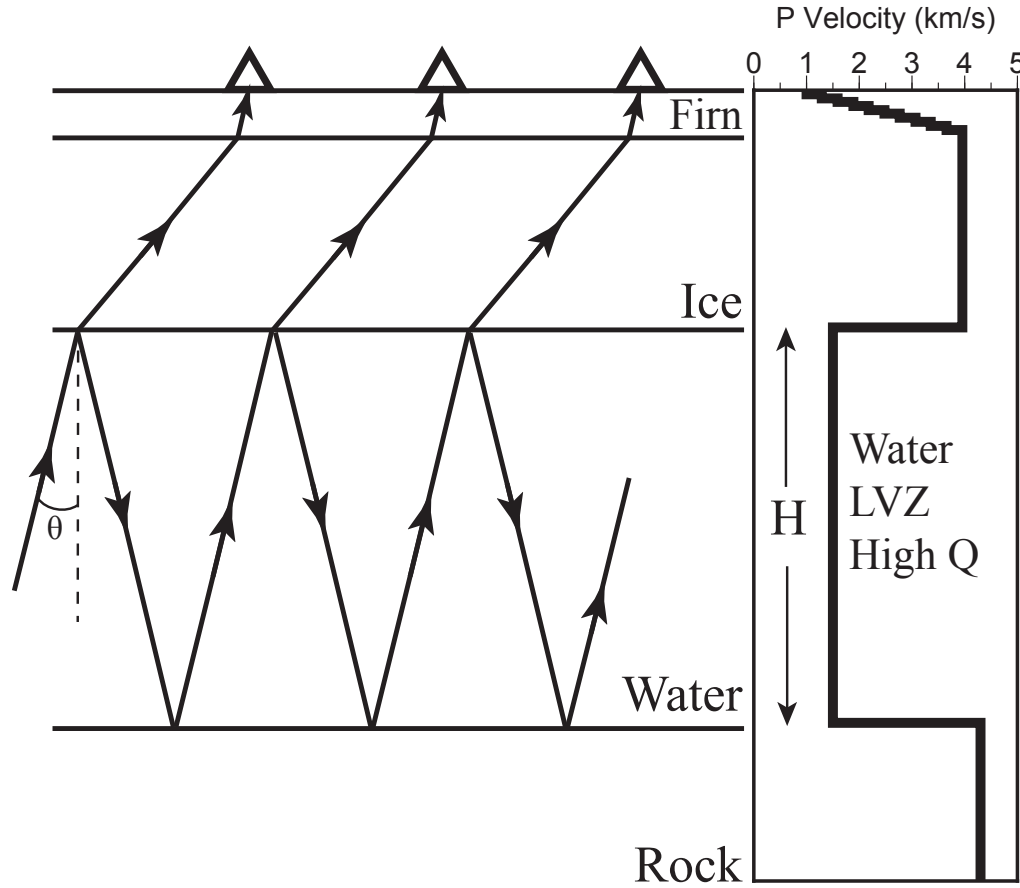


Figure 5.5: Illustration of how trapped waves in the slow water layer propagate to the free surface. The 1D P -wave velocity model is plotted to the right as reference. See the text for more details.

These steeply traveling P waves will cause stronger ground motion on the vertical components than the horizontal components. Because these transmitted P waves have travelled nearly vertically ($\theta \leq 22^\circ$) inside the water layer, we can calculate the resonance frequencies as $f_n = n \frac{V_p}{2H}$, where $n = 1, 2, 3, \dots$, H is the water-column thickness, and assuming θ is small. Given $V_p \approx 1.5 \text{ km/s}$, we derive $H \approx 500 \text{ m}$ from the resonance peaks at 1.5 Hz, 3 Hz, 4.5 Hz, 6 Hz (Figure 5.4), consistent with the previous measurements shown in Figure 5.1A (Galton-Fenzi et al., 2008).

With the new interpretation of the NCF spectral ratios described above, we can

now explain the observed NCFs in the time domain (Figure 5.3C). Because the coherent 1-5 Hz noise at the stations are dominated by the nearly vertical P waves from the water layer, the NCFs will have most of their signal near zero lag and will not resemble the Green's functions between the stations (Figure 5.3), which would have been retrieved if the noise field were diffuse (Lobkis and Weaver, 2001). Note that the NCFs' failure to converge to Green's functions is directly related to the structure itself, i.e. the strong low-velocity water layer causes the noise field to be non-diffuse. In order for the noise field to remain diffuse with this structure, a very specific non-uniform distribution of noise sources would be required (Tsai, 2010b). The observed resonance peaks decay as frequency increases (Figure 5.4) and are small at about 6 Hz. This may be caused by stronger seismic scattering or attenuation at higher frequencies. Therefore for the frequency band of 5-10 Hz, the coherent noise field may be more diffuse than in the 1-5 Hz band, and the observed NCFs resemble the Rayleigh-wave Green's functions (Figure 5.3).

5.6 Noise auto-correlations

The raw ambient seismic noise at a station consists of coherent and incoherent contributions. The coherent noise consists of seismic waves propagating in the medium and, in this study, is dominated by the P waves from the water layer. The incoherent parts may be mechanical noise, electronic noise, inelastic deformation, or any other perturbations that do not propagate from one station to another. Cross-correlations between two stations emphasize the coherent noise and reduce the incoherent noise such that we can clearly identify the resonance peaks from the NCFs. If the incoherent noise is weaker than the coherent noise at some stations, we should still be able to observe the resonance peaks in the spectral ratios of auto-correlations. Indeed, for one broadband station during the 2007 deployment, we can observe the

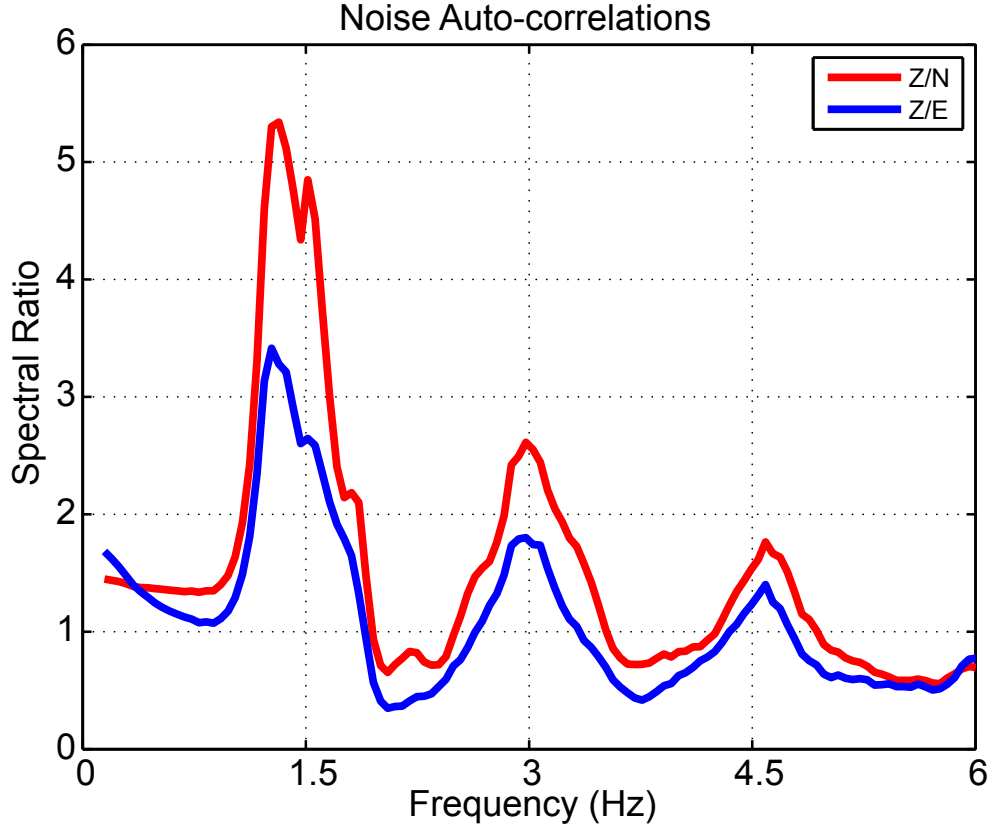


Figure 5.6: Spectral ratios of noise auto-correlations at station BFN1 in 2007. The red and blue curves are for ratios between vertical and north or east, respectively.

same resonances in the spectral ratios between the vertical and two horizontal components (Figure 5.6). This suggests that noise auto-correlations can also be used to study ice shelf structure but requires a better setup (e.g., instrument type, wind isolation, ground coupling) for lower levels of incoherent noise. Since the auto-correlation method is particularly attractive for planetary missions with a single station, these factors should be considered in the design of such experiments.

5.7 Conclusions

In this paper, we have studied noise cross-correlations and auto-correlations on the Amery Ice Shelf. For the frequency band 5-10 Hz, we retrieved Rayleigh-wave Green's

functions between stations, and determined that P -wave velocities in the top 50-m firn layer (down to 1 km/s) are significantly slower than typical ice P -wave velocities. For the frequency band 1-5 Hz, we find that the NCFs do not converge to the Green's functions. Instead, we explain the observations as resulting from a significantly non-diffuse noise field caused by the low velocity waveguide of the water layer sandwiched between the ice and rock layers. Under this new interpretation, we explain the observed peaks in the NCF spectral ratios as P -wave resonances in the water layer, and estimate the water-column thickness. For stations with low levels of incoherent noise, noise auto-correlations also provide a consistent estimate of water thickness. These results can help in the design of future passive seismic experiments to estimate and monitor the structure of ice shelves and water-column thicknesses. Our study may also provide insight for the design of future missions involving seismic exploration of other planetary bodies. In particular, the study presented here serves as a proof of concept for planetary applications of the noise correlation method on icy satellites, such as Titan and Europa.

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