Chapter II:

Emergence of a Low-Viscosity Channel in Subduction Zones Through the Coupling of Mantle Flow and Thermodynamics

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Abstract

We couple a petrological model (pHMELTS) with a 2D thermal and variable viscosity flow model (ConMan), to describe and compare fundamental processes occurring within subduction zones. We study the thermal state and phase equilibria of the subducting oceanic slab and adjacent mantle wedge and constrain fluid flux. Using a Lagrangian particle distribution to perform thousands of thermodynamically equilibrated calculations, the chemical composition of the domain is continuously updated. Allowing the buoyancy and viscosity to be compositionally and thermally dependent permits a consistent linkage between the effect of water addition to and flow within the mantle wedge, leading to predictions as to the fate of hydrated material as subduction proceeds.

We present seven model cases that span normal ranges in subducting slab age, convergence velocity, and slab dip angle. In all models, the coupling between the chemistry and the dynamics results in behavior previously unresolved, including the development of a continuous, slab-adjacent low-viscosity channel (LVC) defined by hydrous mineral stability and higher concentrations of water in nominally anhydrous minerals and bounded by the water-saturated solidus. The LVC develops due to fluid ingress into the mantle wedge from the dehydrating slab, and can be responsible for slab decoupling, large-scale changes in the wedge flow field, and a mechanism by which hydrated slab-adjacent mantle material can be transported to the deep mantle. Changing model parameters indicate that slab age and slab dip angle exert primary control over variations in LVC shape and thickness, due to changing fluid release patterns within the slab. Slab convergence velocity appears to exert a secondary control over LVC shape. Younger slabs tend to have thinner,
more uniform LVCs, while older slabs tend to have a thinner LVC at shallow depths with a large increase in LVC thickness at ~100 km depth, followed by a gradual thinning deeper in the model domain as material is advected down.

**Keywords:** subduction, low-viscosity channel, coupled models, Costa Rica, Izu-Bonin, Mariana

1. Introduction

A complete understanding of subduction zones requires a model that accounts for complex interactions between chemical and dynamic features of the system. Modeling that addresses principally either the force balance or the chemistry, using results from one direction to infer behaviors in the other, has succeeded in reaching broad conclusions as to the manner of hydration of the mantle wedge and melting beneath the arc [1-7]. However, when the thermal structure, viscosity, and the solid flow field are addressed within the context of a fully coupled geophysical and geochemical model, emphasizing the importance of interdependent contributions, more detailed interpretations can be made. The evolution of dynamical quantities such as the flow field, entropy, and bulk composition should provide input to thermodynamic calculations, which output chemically-governed quantities such as melt fraction, compositional buoyancy, water speciation, and latent heat contributions to the thermal balance. This forms an essential loop where neither chemistry nor physics are independently evaluated. Indeed, it is the dependence of one on the other that presents insights into the subduction system on a
fundamental level.

A particular part of the subduction system where strong coupling between mass and energy flows and geophysical and geochemical processes is most important is the mantle wedge adjacent to the slab. There is general agreement that fluids from the dehydrating slab are introduced to the overlying mantle as the slab descends and that the pressure-temperature path, chemical composition, and phase equilibria within the slab determine the locations of water-rich fluid release [4]. The delivery of this water-rich fluid phase into and interaction with the overlying mantle induces hydration reactions within the peridotite and, where temperature is sufficient, water-fluxed melting [8]. Conventional steady-state thermal solutions of subduction indicate that the slab-wedge interface is too cold for even water-saturated melting of peridotite, so the fluids must somehow migrate into hotter areas of the wedge in order for melting to begin [9]. However, the mechanism by which wedge hydration proceeds and the pathways by which water-rich fluids are introduced to the sites of melting remain speculative [2, 4]. Previous modeling studies have specifically addressed the role of water in the subduction system together with dynamical considerations, emphasizing the role of hydrous minerals in acting as transport agents and/or sources of water and using phase diagrams for consideration of the peridotite solidus. Davies and Stevenson [1] propose a model where water released from the basaltic slab at 2.3 GPa is transferred into the wedge and stabilizes amphibole. Advection with the solid flow field results in a net horizontal transport of water along the amphibole-out boundary until the water-saturated peridotite solidus is crossed and melting begins. The model of Iwamori [2] improves upon [1] by adding the potential stabilization of additional hydrous phases within the wedge into the model. This method results in nearly all the
water expelled during primary dehydration from the altered oceanic crust being hosted within a slab-adjacent layer of hydrated peridotite (serpentine and chlorite). Secondary dehydration of this hydrated layer allows the formation of fluid columns leading to zones of active melting. Arcay et al. [3], using non-Newtonian rheology, include the presence of lithospheric serpentinite in the down going slab as a major contributor to the water budget, and discuss a process by which the entire mantle wedge can experience hydration as the slab subducts. However, these studies do not include a full evaluation of water stability in nominally anhydrous minerals or changing bulk composition of the peridotite due to melt extraction. In addition to contributing to the stability of hydrous phases and the initiation of melting, the influx of fluid induces partitioning of hydrogen into defect sites within nominally anhydrous minerals (NAM) such as olivine. Recent investigations introduce the potential importance of these minerals in both the water budget and the dynamics of subduction zones [10-12], and this study aims to improve upon previous modeling by including water partitioning in NAM in the mantle wedge as the primary focus of a coupled geochemical and geodynamic model which emphasizes the origination and development of hydration features within the wedge in an internally consistent treatment.

There is a dual impact on the viscosity structure along the slab-mantle interface due to temperature dependence and compositional dependence (water-weakening) [10]. The implications of the reduction of viscosity of the mantle due to slab-related hydration have been considered [13, 14]. For example, a low-viscosity mantle wedge has been shown to have a substantial effect on the force balance in a subduction zone, and leads to observable signals in topography, state of stress, gravity, and the geoid [13, 15]. The viscosity of the wedge may be at least a factor of 10 smaller than the surrounding mantle lithosphere and
asthenosphere [13], consistent with estimates from seismic dissipation [16] and rock deformation experiments [10]. The low-viscosity wedge potentially resolves the over-prediction of back-arc basin depths by several kilometers [13]. In models that successfully fit the observed geoid, the addition of a low-viscosity wedge changes the state of stress in the over-riding plate from compression to extension [13]. Such a wedge may play an important role in controlling the presence of back-arc spreading. While the importance of a localized low-viscosity region in a subduction zone has been evaluated, the mechanism by which it develops and its detailed geometry have yet to be considered.

We present GyPSM-S (Geodynamic and Petrological Synthesis Model for Subduction), a self-consistent model that includes the thermodynamic minimization algorithm pHMELTS [17-19], which takes into account water partitioning into nominally anhydrous minerals, in conjunction with the 2-D thermal and variable viscosity flow model ConMan [20] and a fluid migration scheme. Evaluation of properties such as the melt fraction, fluid flux, the impact of water in NAM on the viscosity structure and overall flow field, and spatial extent of fluids and melts within the subduction system are all incorporated into GyPSM-S. It is important to mention that the overall structure of GyPSM can be adapted for other tectonic regimes such as mid-ocean ridges (GyPSM-R, [85]).

2. Model Formulation

2.1. Component programs

The two primary component programs used within the GyPSM-S computational
scheme are (1) ConMan, a two-dimensional thermal and variable viscosity numerical flow model [20], and (2) pHMELTS, a thermodynamic energy minimization algorithm that can calculate water partitioning into nominally anhydrous minerals [17-19].

ConMan solves equations for incompressible buoyant viscous flow using the finite element method (FEM) in two dimensions. While an extension to three-dimensional flow is important to fully model variables that may contribute to along-arc observables, it is beneficial to first consider the consequences of a two-dimensional approach. A penalty formulation is used to enforce incompressibility in the solution of the momentum equation [20]. The dynamics are controlled by conservation equations of mass, momentum, and energy, with the Boussinesq approximation. The non-dimensional equations for mass and momentum are:

\[ \nabla \cdot v' = 0 \quad \text{and} \quad \nabla P' - \nabla \cdot (\eta' \nabla v') = Ra T' \hat{k}, \]

where \( v' \) is the dimensionless velocity, \( T' \) is the dimensionless temperature, \( P' \) is the dimensionless pressure, \( \eta' \) is dimensionless viscosity, and \( \hat{k} \) is a unit vector in the direction of gravity. The dimensionless Rayleigh number combines all the material properties:

\[ Ra = \frac{g \alpha \rho A T d^3}{\kappa \eta}, \]
where \( g \) is the acceleration due to gravity, \( \alpha \) is the coefficient of thermal expansion, \( \Delta T \) is the temperature drop across the box, \( d \) is the depth of the box (Table 3), \( \kappa \) is the thermal diffusivity, and \( \eta \) is the dynamic viscosity (Table 1).

The effects of latent heats of melting, hydration, and dehydration can be better evaluated in pressure-entropy space, where an isentropic calculation can result in an increase or decrease in temperature depending on melting or crystallization. Consequently, compared to the normally-posed convection problem ConMan was designed to solve [20], we have modified the energy equation such that entropy is advected instead of temperature. Our non-dimensional energy equation is:

\[
\frac{\partial S'}{\partial t'} = -v' \cdot \nabla S' + \frac{C_p'}{T'} (\nabla^2 T')
\]

(4)

where \( S' \) is the dimensionless entropy, \( C_p' \) is the dimensionless heat capacity, and \( t' \) is dimensionless time. A streamline upwind Petrov-Galerkin method [21] is used to solve (4). In the model formulation of GyPSM-S, we employ a near-fractional melting scheme that accounts for the instantaneous removal of all melt above a certain residual porosity (MINF, Table 1). Because of this, we do not allow the melt to subsequently interact with or crystallize in the lithosphere, which negates the possibility of increases in temperature there due to crystallization of melt.

For all of the results presented here, the computational grid consists of \( 2 \times 10^4 \) uniformly sized bilinear quadrilateral elements: 100 in the vertical direction and 200 in the horizontal direction (20301 Eulerian nodes). All numerical experiments use the same
number of elements, and as such the different model grids have slightly different resolutions from one to another, as the width of the model domain varies among experiments. The dimensional grid resolutions and dimensions of the calculation domains of all models are presented in Table 3.

The viscosity law is both temperature and composition dependent, as influenced by water in nominally anhydrous minerals, specifically olivine [10]:

\[
\eta' = \frac{\eta}{\eta_0} = \exp \left( \frac{Q}{RT_0} \right) \left( \frac{T_0}{T} \right)^{-1} \left( \frac{XH_2O}{XH_2O_{crit}} \right)^{-1},
\]  

where \(XH_2O > XH_2O_{crit}\), \(\eta_0\) is the reference viscosity, \(Q\) is the activation energy, \(R\) is the gas constant, \(T_0\) is the model reference temperature, \(XH_2O\) is the water content in olivine, and \(XH_2O_{crit}\) is the critical value for water weakening (Table 1). The law was determined empirically from experimental results for dislocation creep of hydrated olivine aggregates [22] and is relatively simplistic, meant to account for a large range of pressures, temperatures, and water contents well outside current experimental bounds. The possible compounding effects of the hydration of other NAM are neglected in the viscosity formulation. The viscosity of the thermal lithosphere and the slab depends on temperature and has a maximum value of \(1.0 \times 10^{24}\) Pa s for the coldest regions (\(10^3 \times\) reference viscosity, Table 1). Within the models, we expect variations in temperature of 1500 degrees and water in olivine contents up to \(~2000\) ppm at the highest pressures. As such, we observe that the viscosity law as stated results in a range of potential viscosities of \(5.5 \times 10^{19}\) to \(1.0 \times 10^{27}\) Pa s (with the maximum value seen in the model results set at \(1.0 \times 10^{24}\) Pa s). This model maximum viscosity restricts the range of solid viscosities found within
the model to approximately 5 orders of magnitude (Fig. 1). For comparison, Kelemen et al. [23] show that there is a variation in viscosity of three orders of magnitude from temperature dependence alone.

The initial and boundary conditions within the model are summarized in Figure 2. The subducting slab velocity as well as the velocity of all material subjacent to the slab is kinematically imposed and the magnitude is dependent on the rate of convergence of the model being calculated (Table 3). The velocity boundary conditions on the left-side and the base of the wedge domain are imposed by an analytical solution for corner flow (equation 4.8.23, [24]), while the velocities within the wedge itself are allowed to respond dynamically. The top surface is isothermal (273 K), and the thickness of the over-riding plate and the thermal age of the down-going slab define the initial thermal conditions within the model. The initial particle distribution within the convecting portion of the mantle is assigned a temperature based on a pHMELTS-calculated adiabatic gradient. A prescribed potential temperature and an imposed adiabatic gradient on the sidewalls (Table 1) determine the temperature of incoming material for the duration of the calculation. Specifically, temperatures and entropies along the sidewalls are fixed and determined by independent pHMELTS calculations based on the position of the intersection of the convective (adiabatic) asthenosphere with the conductive thermal lithosphere [80 and references therein]. This explicit treatment of the thermal boundary layer discourages melting of the peridotite immediately upon entering the model domain, and we do not include decompression melting associated with a back-arc in any model. The initial composition-space spanned by the model includes depleted peridotite solved for by pHMELTS (with some supplemental calculations required where pressure and temperature
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conditions restrict pHMELTS applicability, see below for discussion), hydrated altered oceanic crust (AOC) within the slab, and hydrated lithospheric serpentinite also within the slab. The latter two compositions are not solved within pHMELTS, but refer to phase diagrams [25] for dehydration reaction locations within pressure-temperature space. This is due to the fact that the calibration of pHMELTS does not encompass the full spectrum of lithologies within the model domain. Within the slab, we impose a layered structure. The first layer is composed of AOC (basaltic, 2 km, and gabbroic, 5 km) modeled after [25], which treats the entire oceanic crust as basalt and gabbro of MORB composition (Table 2b) and initially contains ~5.0 wt. % H$_2$O. The second layer is composed of a serpentinite lithology (5 km) and is modeled on the hydrated harzburgite phase diagram in [25], initially containing 14.8 wt. % H$_2$O. Within the wedge, we use an initial depleted peridotite composition which includes an initial bulk water content of 110 ppm (Table 2a) [26]. There is no K$_2$O included, which effectively suppresses formation of mica within pHMELTS, but results in a more realistic melt productivity. Equilibration of the original peridotite composition, mass-normalized to 100.0 g, occurs at 3.3 GPa, 1424.56 ºC and f$_{O_2}$ = NNO, which is then used as the starting composition within the pHMELTS algorithm. In selecting a single depleted mantle composition, we are not specifically accounting for the range of source compositions presumably encountered within subduction zone wedges, which can include depletion due to extraction of melt at a back-arc, or larger-scale mantle source variations. While mineral-melt trace element partitioning is included, pHMELTS cannot currently calculate trace elements within the fluid phase itself, making it impossible to directly include the fluid-mobile trace element composition of the slab lithologies in the fully-coupled experiments. Supplemental modeling done independently using GyPSM-S
results is required to address this (Chapter 3).

pH-MELTS can be used to calculate water partitioning among hydrous minerals, nominally anhydrous minerals, melt, and free water, and the effect of such partitioning on melt productivity. The underlying thermodynamic model behind pH-MELTS is pMELTS [27]. This is calibrated for peridotite bulk compositions between 1 and 4 GPa. In pMELTS, water is treated as an oxide component accommodated only in melt, vapor, or hydrous mineral phases, whereas in pH-MELTS the effects of storage of water in nominally anhydrous minerals are approximately modeled [19]. The pH-MELTS calculation uses trace element partitioning to distribute water between the system-consisting of melt, pure vapor, or hydrous minerals-and a hidden reservoir within the nominally anhydrous minerals. Although the algorithms used to calculate thermodynamic equilibria are powerful and generally reliable, especially when melt is present, there are situations where they fail to converge to a correct solution. The pH-MELTS starting solutions are carefully constructed to avoid many of these potential pitfalls, but where they do occur, and also in regions outside of the calibrated pressure-temperature-composition range of pH-MELTS, we use a heat-capacity polynomial formulation for entropy [28] with pMELTS-calculated end-member parameters, in conjunction with an equation of state for water [29]. pH-MELTS uses the Birch-Murnaghan equation of state for the melt phase, but a polynomial expression for the solid volumes [28]. We do not allow the system to re-equilibrate above 5.3 GPa, but use an extrapolation of the equation of state and the heat capacity formulation of assemblages at 5.3 GPa that is continuous in volume and its first derivatives. Liquids are only calculated at pressures below 4 GPa.
2.2. Code coupling and tracer particles

The adiabat_1ph interface to pHMELTS [17] uses scripts to invoke subroutine versions of the (pH)MELTS program, which has the advantage over the graphical user interface (GUI) version of allowing almost complete automation of the calculation process. GyPSM-S uses an extension of adiabat_1ph that can be exploited with parallel processing.

Bulk density is computed by pHMELTS from the equations of state of the constituent phases and the equilibrium phase assemblage and is a function of temperature, pressure, and composition. The latest estimates of water solubility in olivine are included [30].

The component programs are executed and controlled by scripts governing the parallel computing process (Fig. 3). Within GyPSM-S, quantities such as temperature, entropy, volatile content in nominally anhydrous minerals, and water content are passed in a loop structure which includes the component programs until the model reaches a state independent of its initial conditions. A network of Lagrangian particles, acting as chemical tracers, provide iterative feedback among the component programs and are advected within ConMan using a predictor-corrector method [31]; for one convective overturn (about twice the residence time of a particle in our calculations), the particles accumulate a spatial error $O(10^{-5})$. The particle set includes an initial distribution of approximately $4 \times 10^4$ particles (Fig. 4a), with four particles randomly introduced per element within the area of interest and one particle per node in rigid regions and in regions of relatively uniform bulk composition (beyond the extent of water introduction from the slab). In areas where single particles are on the nodes, because of the uniformity of bulk composition and the redundancy of pHMELTS calculations, we do not allow the particles to advect with the
flow field (Fig. 2a). We chose this particle distribution in order to maximize computational efficiency and minimize errors due to interpolation and interference with boundaries (see below).

Particles within the model have several different compositional "tags" that determine lithology. As the experiment proceeds, the particles can be advected across the boundaries of the model domain. In order to keep a uniform particle density, new particles are added at the boundaries (the right sidewall and the interface between high and low particle densities, Fig. 2a) as older particles are advected out of the model domain. The temperature of new particles is interpolated from fixed boundary values along the sidewalls. The criterion for adding particles is a particle summation test within the elements along the boundaries. If an element has become empty, then four more particles are introduced in a random configuration within that element. The type of particle added is appropriate to its initial position: peridotite within the wedge (for particles entering the left boundary within the convecting region and along the right sidewall beneath the 12 km hydration depth), AOC (for particles entering along the right sidewall within 7 km of the top of the slab), and serpentinite (for particles entering along the right sidewall between 7 km and 12 km from the top of the slab). Throughout the computation, the wedge remains well-resolved (Fig. 4b). Encroachment of streamlines against the interface between the convecting and rigid parts of the mantle results in the necessity for a random "kick" given to particles to prevent clumping. Each peridotite-composition particle is associated with a full pHMELTS calculation, translating into thousands of thermodynamically equilibrated calculations per iteration. This allows for a continuously updating dataset and a strong chemical feedback mechanism into the dynamics, provided by particle-to-node and node-
to-particle interpolations at each time step. The particle-to-node step is performed using a
triangle-based linear interpolation scheme for smoothly-varying quantities such as
temperature, but a bilinear scheme for interpolation of available fluid (particles in the four
surrounding bilinear quadrilateral elements all contribute an area-weighted value to each
node) in order to conserve mass. The node-to-particle step is performed using a bilinear
interpolation method (area-weighted value at the particle position within an element
calculated from quantities at the four surrounding nodes). It has been suggested that, for
area-weighted bilinear methods, 5 particles per element represents the optimal load for
high resolution interpolation [32]. We tested three interpolation methods (bilinear,
triangle-based linear, and bi-cubic triangulated) with particle densities of up to 9 particles
per element and ultimately chose to use 4 particles per element as the slight improvement
in resolution presented by the increased particle density was offset by the high
computational cost (pHMELTS). Over the model duration, there is a slight numerical
diffusion that results in overall cooling of tens of degrees due to the interpolations. This
appears to be unavoidable, and we have chosen the scheme and particle distribution that
minimizes it while maximizing computational efficiency. Errors in temperature are highest
in areas of high thermal gradients, namely in the wedge corner and along the slab interface,
and the triangulation scheme appears to perform best at minimizing errors in these areas.

Prior to coupling, the finite element program is used independently (with only
temperature-dependent viscosity) to achieve a quasi-steady-state thermal structure
(approximately 56 million years of subduction); this is then used as our thermal initial
condition for the coupled GyPSM calculations. These nodal values for temperature are
interpolated onto the particle set, with pressure and compositional information (e.g.,
depleted peridotite, altered oceanic crust, lithospheric serpentinite, etc.), including initial water content, being assigned (or "tagged") based on the position of each particle within the dimensional domain (200 km depth, variable width, see Table 3, Fig. 4a).

This first set of pHMELTS calculations involves an isothermal thermodynamic minimization: inputs being temperature and pressure, and outputs being entropy and water content in nominally anhydrous minerals, along with chemical information such as melt presence and composition, water content, trace element abundance, solid phase mode and mineral compositions, and melt and solid density. Each subsequent pHMELTS calculation will be isentropic. At each ConMan timestep, the chemical information is returned to the FEM, influencing the viscosity and energy fields. The appropriate particles move with the updated velocity field, into a new pressure-entropy state, which then becomes the condition sent to the next set of pHMELTS calculations. The energy equation is an advection-diffusion formulation in entropy terms, dependent upon the temperature state of the system. Key variables are updated accordingly, including the water content in nominally anhydrous minerals and the density of the residue. The total duration of the coupled computations in dimensional model time are typically two to five million years of subduction. This is sufficient to approach a state independent of initial conditions, judged by the complete progression of original particles from the top of the model slab to its base.

We use a near-fractional melting scheme, employed such that after every iteration all but a small residual porosity of melt (MINF, Table 1) is instantaneously removed. As the equations governing the finite element calculation assume incompressibility and single-phase flow, we do not allow the removed melt to interact with the remaining solid residue (amounting to an assumption of perfect chemical isolation of migrating melts).
Additionally, we do not account for any impact the remaining porosity has on the solid flow field or the viscosity. However, a small but finite residual porosity helps to stabilize the pHMELTS calculation. Melt extraction depletes the residue (changes the bulk composition of sources for future melts), which changes the solidus temperature. When a packet of mantle peridotite residue (that has experienced melting due to fluid fluxing) is advected along slab-parallel streamlines, encountering new fluid sources from the slab, the temperature of the solidus of the residue should be slightly higher than for the original peridotite composition, influencing where melting will initiate (Table 2a). In order to account for this, pHMELTS retains knowledge of the changing bulk composition of each particle. The bulk composition of the residue, plus any residual liquid, is re-summed to 100.0 g of material so that the extensive quantities calculated by pHMELTS (such as entropy and volume) can be readily incorporated into the finite element model, which deals with intensive quantities (such as density).

2.3. Water migration

The hydrated slab is progressively dehydrated as it moves deeper into the mantle, with slab particles advected into increasing temperature and pressure conditions. We use the hydrous mineral stability calculations of [25] to approximate the amount of free water liberated from slab hydrous mineral phases upon crossing univariant reactions, solving for slab dehydration during subduction as thermobaric conditions change. We assume an initial hydration depth into the slab of 12 km, including both an AOC layer and a lithospheric serpentinite layer, as mentioned previously. A serpentinite layer has been
observed in Alpine ophiolites [33, 34] and seafloor exposures and is presumed to be formed by the introduction of fluids at the ridge crest or along normal faults occurring during plate bending [35]. We do not, however, include a sediment layer, assuming that most sediment water is lost to compaction early in slab descent [79]; sediments probably do not contain enough water to be significant water sources at these depths [36]. However, this assumption disallows sediment melting, which may be significant in certain subduction zones as sources of chemical slab tracers [37]. We assume that the initial state of the slab is water-saturated, resulting in an immediate vertical flux of water into the wedge (running the model long enough so that this initial transient is passed). There is the possibility that temperature changes associated with phase changes, melting, or hydration/dehydration reactions in the mantle wedge can progressively heat or cool the slab, influencing the flux of water at each subsequent iteration. However, because we rely on phase diagrams to predict reactions within the AOC and serpentinite lithologies, we cannot directly account for the thermodynamics of slab dehydration reactions within the model. We do account for the movement of entropy with the fluid phase.

The evolved pure water (water that is not bound by NAM, melt, or hydrous phases) is advected vertically by Darcy's law, taking into account the estimated domain permeability:

\[
(v_{\text{water}} - v_{\text{solid}}) = \frac{Kg\Delta\rho}{\eta_W} 
\]

and

\[
K = \frac{d_m^2 \phi^n}{C},
\]

where \( K \) is the permeability, \( d_m \) is the characteristic spacing of transport tubules (on the order of grain size), \( \phi \) is the mean fluid fraction, \( \Delta\rho \) is the density difference between fluid
and solid, $\eta_w$ is the fluid viscosity, $n$ is a constant parameter indicating the type of pore geometry, and $C$ is a geometrical constant [38] (Table 1). We estimate the fluid velocity to be approximately $2 \times 10^{-8}$ m/s (63 cm/yr) with the current parameters. The choice of $n = 2$ includes a fundamental assumption that flow is occurring within an isotropic network of cylindrical pores of uniform size. Experimental investigation of natural systems indicates that the pore geometry may differ significantly from this idealized case in natural systems, with $n = 3$ [39, 40], and may be anisotropic [41]. The simplifications used in our models can be justified by the lack of information available for conditions at depth. However, we consider the range of fluid velocities dependent on grain size and on the value of $n$ to assess the impact on the model results. Changing $n$ from 2 to 3 effectively extends the time in which it takes water to migrate through the LVC to reach the zone of active melting, however, the LVC geometry and the orientation of the zone of active melting remain the same. At each iteration (dimensionally ~8,000-14,000 years), we assume that chemical equilibrium between the fluid and the solid matrix is attained, such that the water may be bound in nominally anhydrous minerals or in hydrous minerals such as chlorite and/or amphibole, or freely move through water-saturated regions up into the hotter regions of the wedge, where it may be partitioned into a melt phase. We do not account for the solubility of silicate components in our hydrous fluid, which may be of importance to phase relations, as the second critical endpoint beyond which H$_2$O-rich fluids and silicate melts forms a single supercritical phase exists within the bounds of our models (approximately 3.8 GPa and 1000 °C) [42].

2.4. Model input parameters
Subduction parameters such as slab convergence velocity, slab dip angle, and slab thermal age vary on Earth over ranges of 10-100 mm/yr, 10-70°, and 10-160 Ma, respectively [43]. To evaluate the role of changing physical characteristics on the thermal and chemical development of the LVC, we have varied the subduction variables (Table 3) convergence velocity, slab dip, slab thermal age, and crustal thickness among seven models, spanning significant ranges of convergence velocities (47.5-90 mm/yr), slab dip angles (30-60°), and slab thermal structures (incoming plate age 15-165 Ma). Four of the models are immediately applicable to two geographical regions (and two sub-regions within each): (i) the Costa Rica-Nicaragua segment of the Central American subduction zone and (ii) the Izu-Bonin-Mariana subduction zone, and the model results can be used to specifically match physical and chemical datasets.

The Central American subduction zone involves relatively young lithosphere (15-25 Ma) of the Cocos Plate subducting beneath the Caribbean Plate [44]. The convergence rate increases slightly towards the southeast, but the primary difference between the Central Costa Rican (CCR) and Southeastern Costa Rican (SCR) models is the slab dip, which changes from 45° to 30°, respectively. The Izu-Bonin-Mariana (IBM) subduction zone involves relatively mature lithosphere of the western Pacific Plate subducting beneath the eastern Philippine Sea Plate [45], allowing us to evaluate the possible effects of a significantly older slab and a slower convergence rate, as compared to the CCR and SCR cases. The primary difference between the Northern Izu-Bonin (NIB) and Northern Marianas (NMAR) models is the slab dip, which changes from 45° to 60°, respectively. Model ADD1 addresses fast subduction of an older plate, while ADD2 is a slow-
subducting young plate. Model ADD3 involves slow subduction of a mature slab with a thicker overlying lithosphere. All additional models have slab dips of 45º, allowing an evaluation of slab age and slab convergence velocity at a constant dip angle (compared with models CCR and NIB).

3. Model Results

3.1. Development of the low-viscosity channel and controls on its shape

For a young, moderately fast subducting plate, we summarize the results for the process of slab-adjacent mantle wedge hydration (Fig. 5). The pressure-temperature path of the descending slab allows the release of water in distinct locations along the slab surface (Fig. 5c), corresponding to the crossing of dehydration reaction boundaries [25] of particles within the basalt-gabbro and the serpentine layers (within the slab). At the early stages of this model, the majority of the shallow water release (< 100 km) is due to reactions within the AOC layer (jadeite lawsonite blueschist → lawsonite amphibole eclogite, lawsonite amphibole eclogite → amphibole eclogite, and amphibole eclogite → zoisite eclogite) [25]. Reactions within the serpentine layer account for fluids coming from ~110 km depth (rock containing serpentine chlorite brucite → serpentine chlorite dunite; lithologic descriptions from [25]) and from ~170 km depth (chlorite harzburgite → garnet harzburgite) [25]. As the initial fluid transient dissipates, the primary sources of fluid become shallow sources within the AOC (60-80 km depth) and a source around 140 km depth within the serpentinite layer (chlorite harzburgite → garnet harzburgite). The
flux of water from the slab interacts with the nominally anhydrous minerals (NAM) such as olivine, pyroxene, and garnet in the overlying wedge. There is a substantial increase in the water content of these minerals in a region of the wedge adjacent to the slab (Fig. 5c). Through the viscosity formulation (Eq. 5), this creates a strong variation (a reduction of 10-100 times, due to water-weakening) in wedge viscosity within ~25 kilometers of the slab surface (Fig. 5d). Despite discontinuous point sources of water influx, the low-viscosity zone is extended into a continuous layer that is further advected downward by entrainment in the slab-dominated velocity field. Ultimately, the low-viscosity layer extends from 50 kilometers depth to the base of our model region (200 km) and results in a non-uniform low viscosity channel (LVC) (Fig. 5f). The difference in hydration between the ambient mantle wedge and the LVC increases with depth, leading to a strong variation in viscosity that extends perpendicular to the slab. There is a lack of fluid release at the highest pressures beyond the initial transient (in contrast to other models, see below) that results in an LVC thickness at 200 km that is primarily a result of advection of hydrated material from lower pressures, thinned slightly relative to the LVC at lower pressures directly above the fluid sources. The flow field changes with the development of the LVC as seen in the difference in the streamlines within the wedge (Fig. 5a versus Fig. 5e). There is a stronger component of upward flow across the boundary between the nominally anhydrous mantle wedge and the hydrated LVC.

In addition to the hydration of NAM, there is the concurrent appearance of hydrous phases within the hydrated region of the slab-adjacent wedge. Amphibole appears at pressures below 2.1 GPa, and chlorite appears as a stable slab-adjacent phase at pressures from 2.0 GPa to ~5.3GPa, where chlorite breaks down by the reaction clinochlore +
enstatite → forsterite + pyrope + H₂O [46-48], leading to a continuous hydrous phase layer above the slab surface and below the 1000 K isotherm within the wedge (Fig. 6a). Small amounts of deep chlorite (> 5.3 GPa) are an artifact of pHMELTS not including a high-P hydrous phase such as Mg-sursassite or phase A. An evaluation of the position and extent of melting reveals a localized slab-adjacent region of hydrous melt production formed by water-fluxed wedge melting that extends deeper than 100 km. Instantaneous low-degree fractional melts bound the top of the LVC (water-saturated solidus). Water transport occurs solely within the hydrous fluid phase, and therefore, as melting initiates, and water partitions strongly into the melt phase, the activity of water drops below unity and the fluid phase disappears, preventing further transport of water and additional flux melting. The region of melting is therefore thin (~6 km) as measured normal to the LVC surface and is restricted to the top of the LVC, but displaced from the slab-wedge interface due to the thermal structure. In areas with quasi-continuous dehydration from the slab, the melting region is oriented at a slight angle to the slab-wedge interface with depth, as progressive depletion of the advecting slab-adjacent mantle by melting results in a displacement of the water-saturated solidus further into the wedge to higher temperatures. Indeed, melt initiation provides the limitation on the geometry of the hydrated region as demonstrated in a comparison calculation with the silicate liquid phase suppressed in pHMELTS (Fig. 6c). If melting is suppressed, fluid continues to react with the wedge peridotite, hydrating NAM and moving through the wedge until it enters the overlying rigid lithosphere. A sharp, upper boundary (Fig. 6b, c) is imposed to prevent water from entering low-temperature and low-pressure regions where pHMELTS is not stable.

The development of a low-viscosity channel within a subduction zone is a
consequence of the dehydration of the subducting slab and progressive hydration of the overlying mantle wedge below the water-saturated solidus. The thickness of the LVC is determined by the thermal structure of the wedge, in that initiation of flux melting effectively restricts further transport of fluid in a hydrous phase within the system and forms an upper boundary to the hydrated low-viscosity region, controlling the channel geometry. We do not observe hydrous phases (amphibole and chlorite) restricting water transport as a fluid phase to the active melting region. If melting is not present within the wedge, for whatever reason, then a low-viscosity "wedge" geometry may prevail. Due to our assumption of purely vertical fluid flow, initiation of melting appears discontinuous, controlled primarily by the spatial position of water influx, and the presence of active melting can be transient, depending on a consistent influx of water. As mentioned earlier, we do not include a back-arc spreading region, and take care to avoid melting of the peridotite source prior to its introduction into the wedge corner. Latent heat of melting results in net cooling of the residue before turning the corner in the wedge, potentially counter-acting the incorporation of temperature-dependent viscosity variations, which allow for higher slab-adjacent temperatures than an isoviscous rheology [45].

3.2.Model comparison (Table 3)

The influence that slab age and convergence velocity have on the LVC and flow geometry are illustrated with four models at a constant slab dip angle (45°) with different slab ages (18 Ma versus 135 Ma) and different convergence velocities (50 mm/yr versus 87 mm/yr) (Fig. 7). LVC shape changes substantially with changing subduction parameters.
The cases involving a younger slab have thinner, more uniform LVCs. Cases involving older slabs show a very different geometry: a very thin LVC at shallow depths and a large increase in LVC thickness around 100 km depth, followed by the gradual thinning of the LVC towards 200 km depth as the hydrated material is advected out of the model domain. The abrupt truncations at the base of the LVC (Fig. 7a, b) at 220 km from the trench (x-axis) are due to a change in particle distribution (Fig. 2a), and the upper limit of fluid migration (Fig. 7b) is imposed by the position of the overlying lithosphere. The thick hydrated envelope in models with older, colder slabs originates from stronger fluid sources at greater depths than the models with young, warm slabs, which rely on fluid sources from the slab at < 130 km depth. In the case of the older slabs, the streamlines show a marked kink upwards as they cross the thick region of lower viscosity, and the temperature structure is also decidedly influenced, resulting in significant cooling associated with zones of melting. This is a consequence of the latent heat of melting. In regions of high water flux at higher pressures, which occur in models with colder thermal structures due to subduction of older slabs, the melting column is longer, and time-dependent cooling of the wedge occurs. This results in an upward retreat of the water-saturated solidus and an extension of the fluid pathways, allowing fluid from dominantly serpentinite lithology to interact with a shallow melting region. Over time, the zone of melting retreats vertically and stalls below the thermal lithosphere, reducing to direct fluid transport into the overlying lithosphere (similar to the water transport columns of [2]) and melting restricted to the edges of the hydrated region (Fig. 9). The differences in the LVC shape among the models with younger slabs (and likewise among the models with older slabs) can be attributed to variations in slab velocity. Increasing convergence velocity with other
parameters held relatively constant results in a colder thermal regime, and so changes the locations of dehydration reactions within the slab. For the younger slab models, there is melting at 100 km depth in both models as a result of the dehydration of lithospheric serpentinite (chlorite harzburgite → garnet harzburgite), but additional releases at lower pressures (50 mm/yr convergence) and at higher pressures (87 mm/yr convergence) determine the overall shape of the LVC, with the model with more rapid convergence velocity having a slightly thicker LVC due to the deeper fluid release. In terms of comparing lateral variations in viscosity at higher pressures, the slower converging case then involves a greater contrast between the ambient nominally anhydrous mantle wedge and the LVC due to the thinner LVC shape. The overall thinning at higher pressures is a result of the continuation of the LVC solely by advection of hydrated material down-dip, without strong additional fluid sources. For the more mature slab models, the case with the faster convergence velocity likewise involves a slightly deeper fluid source and a somewhat thicker LVC at the base of the model domain. Notably, this is reflected in the position of the melting region (Fig. 9) in that melts for the faster converging case are further down-dip from the trench.

Slab dip has a major control on the geometry of wedge hydration. Models comparing variations in slab dip from 45º are shown in Fig. 8. Fig. 8a and b compare a slab dip shallowing from 45º to 30º, with all other parameters remaining relatively constant. Fig. 8c and d compare a slab dip steepening from 45º to 60º, again with all other parameters remaining relatively constant. The primary observation with regard to the shallowing of the slab dip angle is that while the uniformity of the LVC remains, the thickness of the LVC increases. In the case of the steepening slab dip, the fluid pathways
become closer to slab-parallel, decreasing the thickness of the LVC along the slab and resulting in a sharp thinning of the LVC at 200 km depth, leading to large lateral variations in viscosity as the overprinting of the cold boundary layer adjacent to the slab is not as extensive as in other models. While deep fluid sources are influencing shallower melting via a long fluid pathway, the melting region is closer to the trench due to the near-slab-parallel fluid trajectory, reflecting a narrower trench-perpendicular region of melting. The locations of fluid release remain relatively constant throughout the experiment, except for the initial transient.

Instantaneous melt fractions in all cases are low (<1%) (Fig. 9) as a consequence of the size of the time-step between extractions (and therefore the corresponding change in pressure and addition of water). However, using residual compatible trace element abundances to map cumulative melt fraction results in total melt fractions of up to 20%, comparable to petrological estimates of arc magma fractions. The shape of the instantaneous melting region is complex, as melting relates closely to the positions of fluid release from the slab, and is thin, as a function of our fluid migration scheme (vertical transport, water transport in a hydrous fluid only). However, for a batch melting case, the melt layer can be more continuous and the thickness of the melting region will increase. The influence of the latent heat of melting on the thermal regime (and slight additional cooling due to numerical diffusion from the interpolation algorithms) within the wedge is to thicken the LVC (Fig. 9g-i). Specifically, the position of the melting region produced by fluid releases at high pressures transits vertically into the wedge as the wedge cools, leading to longer fluid pathways. The displacement of the solidus could be exaggerated by the presence of prior depletion due, perhaps, to melting at the back-arc, and would result in
even thicker LVCs.

The thickness of the LVC is related to the distribution and magnitude of fluid resulting from dehydration reactions within the slab (a function of the slab age and convergence velocity), to the degree of melt extraction (cooling and prior melt depletion due to flux melting or to potential back-arc spreading), and to the slab dip angle. The variations in shape of the LVC indicate that changing slab thermal age and slab dip angle exert a primary control over the degree to which the slab is viscously decoupled from the overlying wedge, judging by the continuity of the LVC along the length of the slab and the extension of the hydration region into the wedge. Changing convergence velocity exerts a secondary control, mainly in terms of variations in LVC shape and position of the melting region within the wedge. Subduction of older slabs emphasizes shallow melts from deeper fluid sources (serpentinite). Steeper-dipping slabs (> 45º) allow for melting regions closer to the trench. Shallower dipping and younger slabs emphasize shallower melts and shallower fluid sources (AOC). As the AOC and serpentinized lithosphere have different fluid-mobile trace element chemistries, fluids from different sources should manifest themselves in different trace element patterns in arc lavas from different regions (Chapter 3). Additionally, the greater extent of the low-viscosity region in ADD1 and NIB (subduction of older, colder slabs) has a significant impact of the force balance, manifesting itself in geophysical observables such as the geoid, gravity, and topography (Chapter 4). Despite differences in shape, the development of the spatially-restricted LVC geometry occurs across the range of model parameters evaluated.

4. Discussion
4.1. The low-viscosity channel (LVC)

In all models we observe the development of a spatially-restricted layer of hydration present continuously along the slab-mantle interface. This layer can extend from the slab-wedge interface vertically into the wedge to the overlying lithosphere, up to 100 km in some cases (Fig. 10), and is comprised of hydrous phases (chlorite and hornblende) and nominally anhydrous minerals with high water contents (olivine up to ~1400 ppm, clinopyroxene up to ~5700 ppm, orthopyroxene up to ~2800 ppm, and garnet up to ~600 ppm as the solubility of water in NAM increases with pressure). As there is a fundamental assumption of a pure water phase, we can discuss water contents in terms of solubility, as opposed to storage capacity. This layer is responsible for a large reduction in viscosity ($10^1$ to $10^2 \times$) due to water-weakening along the slab, and can therefore be referred to as a low-viscosity channel (LVC). The development of the specific geometry of the LVC is affected by slab age, convergence velocity, and dip angle through the specific pressure-temperature evolution of the slab, resulting in differing dehydration patterns for different subduction parameters. The hydrated layer defining the LVC is initiated and thickened by fluid release from the slab and is also advected downward with the slab-dominated velocity field, resulting in a continuous extension of the hydrated layer along the slab-mantle interface. This smearing out by the sub-solidus flow in the wedge counteracts the discontinuous pattern of water release from the slab. Our models are restricted in vertical dimension due to the pressure limitations of pHMELTS, but we observe the persistence of the hydrated layer to the base of our domain, and reasonably assume that it can persist
deeper. The increasing solubility of water in olivine with pressure may allow for an even greater influence on viscosity with depth, assuming that the slab has not been completely dehydrated. Indeed, for models with subduction of older slabs, the lithospheric serpentine layer still contains as much as 6.8 wt. % H\textsubscript{2}O as it exits the model domain. The peak water content in NAMs in the LVC, as it reflects a water-saturated zone, is primarily a reflection of the solubility of water at a particular temperature and pressure, and therefore the peak hydration does not vary significantly among the models tested. The extent of the LVC into the mantle wedge is governed by the position of the water-saturated solidus within the specific thermal structure defined by the subduction parameters of a particular model and the degree of melt extraction and prior depletion. As soon as melting initiates, the activity of water drops as water is strongly partitioned into the melt. In the absence of a hydrous fluid phase, water transport ceases, and melting is restricted to a thin zone immediately above slab fluid sources.

We do not see the formation of Rayleigh-Taylor instabilities (cold diapirs) along the surface of the hydrated LVC, in contrast to [49], because of lower density contrasts across that boundary predicted by our models. There are like to be two reasons for the lower density contrasts. Firstly, we do not include a very low-density sediment layer in our slab lithology and do not assume mechanical (solid) mixing between slab lithologies and the overlying mantle wedge peridotite (which decreases the density of the hydrated peridotite and therefore increases the density contrast between that hydrated layer and anhydrous peridotite above it). Secondly, we do not observe the presence of serpentinized wedge peridotite against ambient nominally anhydrous peridotite. The position of the hydrated peridotite solidus in pHMELTS is sufficient to allow some distance between the
upper stability limits of the hydrous phases and the water-saturated peridotite solidus. Compositional limitations within pHMELTS result in a restriction in the range of hydrous minerals that can be stabilized in the wedge. Along the slab interface, pHMELTS stabilizes hornblende at lower pressures and chlorite at higher pressures (Fig. 6a). There is residual amphibole present in the shallowest melt source regions, but along the majority of the slab surface, chlorite is the only stable hydrous phase and is restricted to within ~10 km of the slab surface due to breakdown above 1000 K. Coincident with the sharp drop in water content along the top of the LVC boundary, we observe slight density contrasts increasing from water-saturated peridotite in the LVC to ambient nominally anhydrous peridotite ($\Delta \rho \sim 20-50$ kg/m$^3$), which are much less than those predicted by [49] for the diapir-source region ("mixed" hydrated layer vs. anhydrous peridotite) along the top of the slab. The thermal conditions of our model predict a much thicker hydrated channel before water-saturated melting begins. Therefore, we never see fully-serpentinized (implying stability of chrysotile and antigorite) mantle lithology adjacent to the nominally anhydrous region above it. Finally, the hydrated channel in our models is capped by the initiation of melting. At lower pressures (~1.5 GPa), melting of a fully-saturated assemblage results in a higher density residue and a lower density melt phase. The residue density is comparable to the anhydrous density, but is slightly lower. At higher pressures (~4.0 GPa) there are even smaller density contrasts between fully-saturated peridotite and residues of melting. The low density contrasts across the top of the LVC compared to the contrasts of [49] across the top of their thinner hydrated layer ultimately inhibit the formation of Rayleigh-Taylor instabilities in this model at the pressures evaluated.

Iwamori [2] presents a numerical model that describes the generation and migration
of fluids from the slab with consequent equilibration with the overlying convecting mantle solids, producing hydration and melting. Similar to our results, there is a stable slab-adjacent layer of chlorite within the wedge and a displacement of the region of melting into the wedge. In contrast to our results, their chlorite layer [2] is able to absorb the majority of the water released from the slab and dehydration of the chlorite around 150 km depth allows for a singular fluid source, transporting water to the melting region. Our results, which include consideration of water stability in NAM, indicate that fluid is able to both hydrate the slab-adjacent layer of chlorite and an overlying thickness of NAM. Successive fluid flux through this saturated zone produces melting at multiple depths within the wedge, ultimately producing a discontinuous slab-parallel melting region that is displaced into the wedge. Our melting region looks very similar to the disequilibrium transport case of [2], in which water is allowed to "leak" from the slab-adjacent hydrated layer at depths less than 150 km.

Independent of results presented here, time-dependent models of subduction with a parameterized wedge viscosity show that slab dip can be substantially influenced by a low-viscosity channel geometry with a thickness of tens of kilometers and a viscosity contrast of a factor of two [50]. In such models, a low viscosity channel generally leads to increased slab dips as the suction force drawing the slab upward is reduced. Our model provides a self-consistent mechanism to generate such a low-viscosity channel geometry, however, we are unable to demonstrate the effect changing slab dip would have on an existing LVC because we did not include dynamical feedback to the slab. We can estimate the effect that a changing slab dip may have based on our model results encompassing a range of slab dip angles. Initiation of subduction at a shallow dip angle would result in a
continuous LVC to at least 200 km depth of roughly uniform thickness. If the formation of this LVC leads to increasing slab dip angles [50], the LVC would most likely remain as a continuous channel, but the thickness may change, and, more importantly, the positions of the melting region within the wedge would change. This may lead to observable increases in lava flux from the volcanic arc as melts are produced further from the trench initially (perhaps feeding the rear-arc), and then closer with time as the slab dip angle changes. The trenchward progression could also be mapped by signals in fluid-mobile trace elements consistent with lithospheric serpentinite dehydration as opposed to dehydration from AOC proceeding from the rear-arc to the volcanic front with time (Chapter 3).

Although we do not specifically include prior melt depletion at a back-arc into GyPSM-S, we note that it can potentially impact the character of melts produced in the models with time as a function of position in the mantle wedge. For example, considering subduction of an older, cold slab, the melting region influenced by the deep fluid sources changes position in the wedge with time, driven by cooling of the mantle wedge due to latent heat of melting (Fig. 11). At the beginning of the experiment, the source region for these melts is relatively fertile. There is a displacement of the melting region into the wedge away from the residues of the shallow melts traveling along the slab-parallel flow field, and therefore no prior source depletion due to episodes of flux melting earlier along the streamline. Additionally, the position of these melts in relation to the flow field and potential prior depletion from the back-arc melting region implies that they are relatively fertile as well. As the experiment continues, the deep-sourced melting region shallows, and while the fluid-mobile trace elements are still consistent with a deep source (serpentinite), the extent of potential prior depletion due to a back-arc increases, potentially
changing the values of trace element indicators such as Zr/Nb with time. Shallowing of the deep-sourced melting region also produces even greater depletion signatures for the shallow-sourced melts, as the two melting regions are aligned along streamlines within the wedge.

Our use of pHMELTS allows for a self-consistent application to the problem of a changing bulk composition (source depletion) due to melting and for the partitioning of water into NAM. Hydrous phases such as amphibole and chlorite are present, but do not dictate the transport of fluid to the active melting region, and while they act as effective "sponges," they do not inhibit the flux of a hydrous fluid phase. Instead, fluid migrates vertically into the wedge, progressively saturating a layer of NAM and hydrous phases. As mentioned previously, we do not see the stability of hydrous phases up to the zone of active melting except in the case of very low pressures. Once the layer is saturated, water can move through to the melting region (water-saturated solidus of peridotite), where it is partitioned into the melt phase and effectively removed from the system.

4.2. Water mobility: recycling to deep mantle and timing of transport to active melting region

The formation of enriched mid-ocean-ridge basalts (E-MORB) at normal mid-ocean ridges hints at the presence of chemical heterogeneities in the mantle which may have been generated by recycling of material at subduction zones [51-55]. Geochemical arguments exist for the relative importance of the slab-adjacent mantle, metasomatized by either slab-derived fluids or small-degree slab melts, rather than recycled oceanic crustal materials or
Analyses of basaltic glasses from the mid-Atlantic ridge (MAR) near the Azores reveal evidence (high $\delta^{18}$O, La/Sm, Ce/Pb, and $^{87}$Sr/$^{86}$Sr and low $^{143}$Nd/$^{144}$Nd) for an enriching agent [52]. However, bulk incorporation of sediments or altered oceanic crust to the ridge melting source region will not reproduce observed geochemical trends [52]. A two-stage model of the slab-adjacent mantle, modified by either fluids or slab-derived small-degree melts, and then mixed with ambient mantle to form a mixed, enriched source region for partial melting allows for erupted E-MORB lavas with major element systematics similar to normal MORB, isotopic ratios reflecting long-term enrichment of the source region, and the required trace element fractionations and concentrations [53]. Additionally, high lithium isotope ratios in enriched East Pacific Rise lavas may be explained by enrichment by fluid-modified recycled wedge material instead of altered oceanic crust itself [36]. The slab-adjacent mantle is carried down with the subducting slab, but, as opposed to altered oceanic crust, may be more efficiently mixed in with ambient upper mantle to produce enriched source regions for normal upwelling and melting beneath ridges.

In these models, the LVC emerges as a stable zone of fluid-modified slab-adjacent mantle material and trapped low-degree melts that is transported with the slab-dominated flow field, presumably to depths beyond our model region, where it may, at some point, separate from the denser oceanic crust and mix with surrounding upper mantle material. The persistence of the LVC to great depths is due to it being spatially limited by the water-saturated solidus. As the subducting slab descends, although water solubility in NAM increases, the pressure-temperature path of the LVC will not cross the solidus, allowing a mechanism for the recycling of water and slab-adjacent water-rich wedge material deep
into the mantle, as well as possibly affecting the solid flow and contributing to slab decoupling. Excluding hydrous phases (as pMELTS does not stabilize realistic hydrous phases near 200 km depth), and assuming a peridotite assemblage of 57% olivine, 8% garnet, 16% orthopyroxene, and 16% clinopyroxene, the LVC can potentially transport ~2200 ppm H$_2$O into the deeper mantle in NAM alone, providing a significant, robust, water source.

The presence of the LVC has implications for the timing of fluid-bearing element transport from the slab to the arc. It has been hypothesized that two separate mantle wedge enrichment mechanisms result in the $^{238}$U excesses observed at the Mariana arc: an episode of sediment-derived (uranium-rich) fluid addition to the mantle source followed by >350ky of radiogenic ingrowth as the solid flow advects the material deeper, and then a second episode of (aqueous) fluid influx from the dehydrating altered oceanic crust [37]. Timing from this second release of fluid to the eruption of lavas is on the order of tens of thousands of years, a time-frame which necessarily includes melt migration and lower crustal processing, and the rapidity of this process suggests that the fluids themselves are the trigger for the initiation of significant mantle wedge melting [37]. The LVC, defined by tens of kilometers of water-saturated mantle material, may allow fairly rapid fluid transport with minimal chemical water-rock equilibration, resulting in direct delivery to the melting region and immediate triggering of melting. With the model fluid velocity ($d = 100$ µm, $n = 2$), it would take < 50 kyr for the fluids to penetrate to the active melting region with an LVC thickness of 25 km, a sufficiently short timeframe that would correspond to the U-series timescale for the second (and applicable, considering a lack of sediment) fluid influx to the wedge from the AOC. Changing these parameters (i.e., $n = 3$) results in timescales
of fluid transport on the order of 1.5 Ma for a similar LVC thickness.

4.3. Melting

In all models, there is a distinct spatial region of melt production within the mantle wedge. We find that the dominant factor in subduction systems for controlling this melt distribution is the amount and spatial location of dehydration and free water release within the slab. Not only do fluids carry slab signatures, but the spatial location (pressure and temperature) of their release has implications for the resulting fluxed melt composition. Additionally, although we do not account for the influence of melt on viscosity, the presence of a melt lens may serve to either increase the effective thickness of the LVC, or to smooth out the sharpness of the viscosity transition from the LVC into the interior of the mantle wedge. In contrast to our near-fractional melt extraction scheme, melt migration at depths greater >90 km may be consistent with porous/reactive flow [56]. This would add an additional transport mechanism for water in the system: allowing hydrous melts to react with solids as they migrate will re-distribute water within NAM beyond the LVC, leading to a smoothly decreasing activity of water upwards and a finite extension of the hydration region and a wedge-type low-viscosity geometry.

A number of geochemical and petrological studies have suggested that partial melting of subducting slab components (sediment and/or altered oceanic crust) is a possibility in many arc systems. This is due to recycling of trace elements such as Th that are considered relatively fluid-immobile but can be partitioned strongly into partial melts of metasediments and metabasalt [37, 57-59] and by the similarities between trace element
patterns of partial melts of eclogite with primitive arc andesites [60-64]. Plots of slab-wedge interface pressures and temperatures for the models alongside the water-saturated MORB solidus of [25] (i.e., 650-700 deg. C from 1-3 GPa) show that we would not reasonably expect melting of the AOC to occur in any of the models (Fig. 12). If, indeed, melting of the oceanic crust were to occur, as suggested by some thermal models incorporating temperature-dependent [23] and temperature and stress-dependent viscosity [6], the implications for the development of the LVC could be significant. Melting of the slab (sediment and/or AOC) would encourage partitioning of water into the melt phase, reducing the capacity of fluid for transport into the wedge. In this case, relying on a fluid phase to initiate melting may be incorrect, as the fluid could be taken up wholly in NAM and hydrous phases. We would then rely on the migration of the hydrous slab melts as the transport mechanism for water, and a more complicated fluxing process to initiate peridotite melting.

We note that the observation of the volcanic front forming at nearly constant globally-averaged height (~105 km) above the Wadati-Benioff zone [43] does not appear to be fulfilled by a discontinuous melt lens that extends along the slab surface (Fig. 9). However, we do not take into account melt migration processes that may serve to focus the melt, or may exploit the channel geometry for flow reversals back up the slab. Porous flow driven by pressure gradients as a mechanism of melt focusing towards the wedge corner [5], diapirism of melts towards the overlying lithosphere [65], or fracture propagation as a mechanism of melt extraction [66] have all been invoked as potential melt migration processes within subduction zones. We assume vertical fluid transport, immediately moving fluid into the mantle wedge upon release. Accounting for up-dip migration of
fluids along the slab-wedge interface to lower pressures may concentrate melting within the wedge. Despite the simplistic approach to melt migration in our models, we can infer quite a lot from the positions of the zones of active melting. Seismic tomographic studies in northeastern Japan show an inclined, slab-parallel seismic low-velocity and high-attenuation zone in the mantle wedge [67, 68]. These discontinuous inclined regions exist at depths less than 150 km, are separated from the upper surface of the slab by ~50 km, and show very similar geometries to melting regions calculated by GyPSM-S in that the regions are inclined towards the position of the arc (Fig. 9).

Latent heat of melting appears to be the cause of the significant cooling of the mantle wedge. Since we remove melt completely from the system (above a certain porosity), we do not allow for crystallization of that melt within the wedge, which may also counteract wedge cooling by latent heat of crystallization. The calculated solidi from pHMELTS show a systematic offset from values calculated by [69]. At pressures less than 1 GPa, pHMELTS predicts lower solidus temperatures, while it gives significantly higher temperatures at higher pressures with a steeper dT/dP solidus curve, (1150 °C vs. 800-1000 °C at 3 GPa) (Fig. 13). This may lead to an over-extension of the zone of active melting into the wedge in our models, especially at pressures in excess of 3 GPa, as well as the lack of a contact between the chlorite stability field and the zone of active melting. However, the overall relationship between fluid migration, hydration of NAM, and displacement of the inclined zone of melting away from the slab with increasing pressure should remain the same.

4.4. Impact of LVC on seismic wave propagation
Seismic velocity and attenuation studies have interpreted a hydrated region directly adjacent to the slab. From regionally detected body-wave phases, low velocity layers (LVLs) exist above seismically fast slabs with thicknesses of 5-10 km in the Mariana, Japan [70], Kurile, Nicaragua [71], and Aleutian arcs. However, the LVL may be up to 20 km thick in parts of Alaska [72]. The Japan results suggest that the LVL extends down to 300 km depth with substantial velocity reduction. The P-wave velocity reduction could be as much as 14% if the thickness of the LVL is only 10 km, but only 4% if the layer is 30 km thick [70], suggesting a thick zone of hydrated phases. In addition, studies of seismic attenuation (with lower spatial resolution than the velocity models) suggest that there are broad zones of high attenuation (low Q) above slabs in Tonga [73], Alaska [74], and elsewhere.

It has been shown that the presence of hydrous phases can have a direct impact on seismic properties, and estimates of low-velocity anomalies along the slab-wedge interface in subduction zones have been hypothesized to be due to a continuous layer of hydrous phases [72, 82]. While hydrous phases can certainly hold more water than NAM, it remains true that NAM can account for significant amounts of water (in olivine alone as much as 0.6-0.9 wt. % can be held at 12 GPa [30, 75]) with steadily increasing solubility with increasing pressure and may have an indirect effect on seismic properties. The LVC is defined by an increased water content in NAM, present as hydrogen-related defects, which can enhance anelasticity and lead to an increase in attenuation and a reduction in seismic wave velocities [76-78,16]. Therefore, our results for a continuous channel of high water content in NAM may be consistent with regionally detected body-wave phase results.
showing low velocity layers (LVLs) of order tens of kilometers thickness above slabs [70].

5. Conclusions

As our models show, the ability to simultaneously explain geophysical and geochemical observations is essential to demonstrate certain behaviors such as the development of boundary features along the slab-mantle interface. The spatial extent of the low-viscosity region of the wedge may be a large-scale volume extending from the slab-mantle interface to the back-arc (e.g., [13]) or a relatively thin, continuous channel defined by water-saturated NAM and hydrous phases along the slab-mantle interface, depending on subduction parameters (slab age, convergence velocity, slab dip angle). The development of the LVC is a consequence of the vertical migration of fluids into the mantle wedge and reaction with peridotite to produce hydrous phases and higher water contents in NAM. Its extent is limited by the onset of melting and is therefore dependent on the position of the water-saturated solidus, which changes spatial position within the wedge due to source depletion (prior melt extraction) and/or the thermal evolution of the wedge (progressive melt extraction). The zone of active melting exists at the upper surface of the LVC, and the thickness and instantaneous melt fraction are restricted in our models by the assumptions of near-fractional melt extraction and the limitation of water transport to the hydrous fluid phase. Despite changing subduction parameters, the geometry of the melting regions are quite similar in all models: discontinuous lenses inclined to the slab surface and displaced from it by tens of kilometers. The persistence of the LVC would provide a mechanism by which hydrated slab-adjacent mantle material (consisting of a
significant reservoir of water and potentially very low-degree mantle melts) is transported to the deep mantle without melting, providing a source for enriched OIB magmas such as the Azores. The LVC is also significant because of the effect it has on the large-scale flow field within the wedge, possibly leading to slab decoupling [13] and changes in slab dip [50]. Additional evidence for the existence of the LVC includes seismic wave propagation and attenuation and recent studies showing the significant displacement of the active melting region from the slab-wedge interface [67, 68].

Acknowledgments

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**Figure Captions**

**Figure 1:** Range in viscosity produced from Eq. 5 implemented in GyPSM-S for the model water in olivine contents (0-2000 ppm) and model temperatures (0-1500 °C in 100 °C intervals). The range spans 5 orders of magnitude in viscosity when the maximum viscosity cut-off is imposed.
**Figure 2:** (a) Initial conditions and (b) boundary conditions imposed within the GyPSM-S model domain. See text for details.

**Figure 3:** Computational organization and data flow of the GyPSM-S model.

**Figure 4:** (a) Initial particle distribution for the wedge corner region of model SCR. The particles are arranged by composition and by temperature: peridotite (green), altered oceanic crust (black), and serpentinite (blue). The particle density is increased for the mantle wedge, the area of interest. (b) Final particle distribution after run completion for the wedge corner region of model SCR.

**Figure 5:** Development of LVC for model CCR: (a) initial thermal structure and streamfunction (with arrows showing direction of flow), resulting from an uncoupled ConMan calculation approaching steady-state; (b) initial viscosity structure, calculated immediately after the first coupled iteration with pHMELTS such that the water content of the ambient mantle is reflected in the viscosity structure as well as temperature-dependent contributions; (c) increase in water in olivine above the ambient background as fluid from the dehydrating slab rises vertically into the wedge and then reacts with the peridotite to form hydrous phases and hydrated NAM. A thin zone of melting is illustrated at the top of the hydrated channel where the white contour indicates melting > 1%; (d) viscosity structure corresponding to panel c, showing the marked decrease in viscosity of the solid matrix due to water-weakening from hydration of nominally anhydrous olivine; (e) advection of the slab-adjacent wedge peridotite results in the development of a hydrated
channel, bounded at the top by a thin melt lens. The solid flow streamlines shows a marked change in trajectory upon impacting the hydrated channel, with an increasing upward component; (f) the hydrated channel is defined by high concentrations of water in NAM, which influence the viscosity through the flow law, and result in the low-viscosity channel (LVC). Note that the contour interval of the stream function in the slab and descending mantle is twice the value in the wedge.

**Figure 6:** (a) Distribution of hydrous phases within model CCR. Hornblende (red) is present at lower pressures (< 2.5 GPa), while chlorite (green) is stable at pressures up to ~5 GPa, and temperatures < 1000 K. This stability field results in the formation of a continuous channel of hydrous minerals to depths of ~175 km within the LVC and bounding the slab surface. (b) Water in olivine (which defines the LVC). (c) An experiment with melting suppressed within the pHMELTS model, to test the impact of melting as the primary restriction on the thickness of the LVC. Note that the contour interval of the stream function in the slab and descending mantle is twice the value in the wedge.

**Figure 7:** Influence of slab age and convergence velocity on the development of the LVC as shown by the resulting viscosity structure. Models with a 45° slab dip are compared, arranged such that the effects of increasing slab age and increasing slab convergence velocity can be evaluated at constant slab dip angle. Fig. 7a (NIB) and b (ADD1) represent the subduction of old, cold slabs (thermal age 135 Ma), differentiated primarily by slow (50 mm/yr) and fast (87 mm/yr) convergence velocity. Fig. 7c (ADD2) and d (CCR)
represent the subduction of young, warm slabs (thermal age 18 Ma), and slow and fast velocities, respectively (Table 3).

**Figure 8:** Influence of the impact of changing slab dip on the geometry of the LVC. (a-b) CCR-SCR: shallowing slab dip from 45° to 30°. (c-d) NIB-NMAR: steepening slab dip from 45° to 60°.

**Figure 9:** Instantaneous melt fraction (color) and fluid release from the slab (blue contours), showing that melting is generally restricted to a thin (~6 km) lens immediately above fluid release locations within the slab for models (a) CCR, (b) NIB, (c) ADD2, (d) NMAR, (e) SCR, and (f) ADD1. Panels (g-i) illustrate the evolution of the melting region and the changing fluid release locations over time for model ADD1.

**Figure 10:** Thickness of the LVC vertically from the slab surface as a function of distance along the slab for (a) CCR (red), NIB (blue), ADD1 (black), ADD2 (purple), (b) NMAR (green), and (c) SCR (pink) models.

**Figure 11:** Schematic of the low-viscosity channel (LVC) geometry, including hydrous melt layer for the NIB model case. Dehydration reactions in the down-going slab release water, which rises into the overlying mantle wedge and reacts with peridotite to form hydrous phases and to hydrate nominally anhydrous minerals (NAM), such as olivine. Locations of water release from slab dehydration reactions showing the discontinuous nature of the water release due to crossing of reaction boundaries. The shallower
dehydration reactions are due to reaction boundaries in the altered oceanic crust, while the deeper reactions are in the lithospheric serpentininite layer. Once saturated, water can rise through the hydrated NAM layer into the hotter regions of the wedge, where it induces water-fluxed melting.

Figure 12: Pressure-temperature trajectories of the slab-wedge interface for the six models with the water-saturated MORB solidus from [19]. We neglect slab melting in our models, which refers to melting of the altered oceanic crust, as sediments are not included. The only model that approaches the water-saturated MORB solidus is ADD2, around 4.0 GPa.

Figure 13: Solidus relations for the model peridotite wedge starting composition (Table 1) with variable H$_2$O contents predicted by pHMELTS and the estimates of solubility of water in nominally anhydrous minerals (NAM) given by [30], similar to the construction of Figure 1 from [19], but with the primary difference being the higher estimates of water able to go into NAM relative to values originally given by [10]. The upper heavy black curve is the anhydrous solidus ($a_{H_2O} = 0.0$); the lowermost heavy black curve is the water-saturated solidus ($a_{H_2O} = 1.0$). The blue contours are lines of constant activity of water on the solidus in increments of 0.1 in $a_{H_2O}$. The black curves labeled 50, 300, 700, 1200, and 2000 show the solidus predicted for these bulk H$_2$O contents in parts per million by weight. The gray lines indicates the stability limits of garnet and plagioclase on the solidus, respectively. The green boundary shows the stability of hornblende on the solidus.
Figure 1.

increasing model temperatures
(0-1500°C in 100°C increments)
**Figure 2a.**

White areas have stationary particles on the nodes while gray areas have randomized particles that follow the flow field.

- $T_0(z)$ lithospheric geotherm
- Convecting asthenosphere
  - 110 ppm $H_2O$
- $S_0(z) =$ constant

Subducting plate
- Particle introduction
- Particle exit

Variable width (see Table 1)

- 5.0 wt.% $H_2O$
- 14.8 wt.% $H_2O$

- Basalt (2 km)
- Gabbro (5 km)
- Serpentinite (5 km)
Figure 2b.

T = 273 K constant temperature

rigid lithosphere, $u = v = 0$

velocities free

velocities kinematically imposed

incoming mantle flow

outgoing mantle flow
Figure 3.

**pHMLTS**
- Updates entropy and volume for water transport
- Solves isentropic calculation for equilibrium chemistry
- Extracts melt and updates variables accordingly

**ConMan**
- Advection of entropy and particles along updated velocity field
- New viscosity solution based on temperature and water content in NAM

**Water Advection**
- Vertical movement of water assuming Darcy flow
- Uses solid density

Water available for partitioning

Updated water content field

Updated temperature field

Solid density in NAM
Figure 4.

A.

B.
Figure 6.
Figure 7.
Figure 8.
Figure 9.
Figure 10.
Figure 11.
Figure 12.
Figure 13.
Table 1: Model parameters held constant

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* indicates non-dimensional quantity
square brackets indicate references
Table 2a: pHMELTS starting composition

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Adapted from Workman and Hart [26]
Table 2b: Altered MORB starting composition

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*After Hacker et al. [25]*
**Table 3: A summary of subduction zone model parameters**

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*numbers in square brackets are references*