## Neutron Stars and NuSTAR

A Systematic Survey of Neutron Star Masses in High Mass X-ray Binaries

&

Characterization of CdZnTe Detectors for NuSTAR

A Thesis by Varun B. Bhalerao Advisors Professors Fiona Harrison & Shri R. Kulkarni

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Varun B. Bhalerao All Rights Reserved Dedicated to my parents, Erawati and Bhalchandra Bhalerao my role models, motivation, and strength.

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### Abstract

My thesis centers around the study of neutron stars, especially those in massive binary systems. To this end, it has two distinct components: the observational study of neutron stars in massive binaries with a goal of measuring neutron star masses and participation in NuSTAR, the first imaging hard X-ray mission, one that is extremely well suited to the study of massive binaries and compact objects in our Galaxy.

The Nuclear Spectroscopic Telescope Array (NuSTAR) is a NASA Small Explorer mission that will carry the first focusing high energy X-ray telescope to orbit. NuSTAR has an order-of-magnitude better angular resolution and has two orders of magnitude higher sensitivity than any currently orbiting hard X-ray telescope. I worked to develop, calibrate, and test CdZnTe detectors for NuSTAR. I describe the CdZnTe detectors in comprehensive detail here—from readout procedures to data analysis. Detailed calibration of detectors is necessary for analyzing astrophysical source data obtained by the NuSTAR. I discuss the design and implementation of an automated setup for calibrating flight detectors, followed by calibration procedures and results.

Neutron stars are an excellent probe of fundamental physics. The maximum mass of a neutron star can put stringent constraints on the equation of state of matter at extreme pressures and densities. From an astrophysical perspective, there are several open questions in our understanding of neutron stars. What are the birth masses of neutron stars? How do they change in binary evolution? Are there multiple mechanisms for the formation of neutron stars? Measuring masses of neutron stars helps answer these questions. Neutron stars in high-mass X-ray binaries have masses close to their birth mass, providing an opportunity to disentangle the role of "nature" and "nurture" in the observed mass distributions. In 2006, masses had been measured for only six such objects, but this small sample showed the greatest diversity in masses among all classes of neutron star binaries. Intrigued by

this diversity—which points to diverse birth masses—we undertook a systematic survey to measure the masses of neutron stars in nine high-mass X-ray binaries. In this thesis, I present results from this ongoing project.

While neutron stars formed the primary focus of my work, I also explored other topics in compact objects. appendix A describes the discovery and complete characterization of a 1RXS J173006.4+033813, a polar cataclysmic variable. appendix B describes the discovery of a diamond planet orbiting a millisecond pulsar, and our search for its optical counterpart.

## Contents

Li	ist of	Figures	xii
Li	ist of	Tables	xv
Li	ist of	Acronyms	vii
Pa	art C	Dne: NuSTAR	1
1	Nu	STAR: The Nuclear Spectroscopic Telescope Array	2
	1.1	Hard X-rays	2
	1.2	Hard X-ray Telescopes	4
	1.3	NuSTAR	9
2	CZ	T Detectors	<b>14</b>
	2.1	Hard X-ray Detectors	14
	2.2	NuSTAR Detector Architecture	16
	2.3	Photon Trigger and Readout	20
	2.4	live-time, dead-time, and Event Rates	25
	2.5	Event Reconstruction	28
	2.6	Pileup	35
3	Cal	ibration	38
	3.1	Requirements	39
	3.2	Detector Screening, Selection, and Calibration Steps	42
		3.2.1 Hybrid Selection and Screening	44
		3.2.2 Pixel Response Calibration	44

		3.2.3	X-ray Pencil Beam Scan	45
		3.2.4	Quantum Efficiency Measurement	45
	3.3	The X	-ray Generator Laboratory	46
		3.3.1	Hardware Design	46
		3.3.2	Control Software	52
	3.4	Calibr	ating the Setup	54
		3.4.1	Beam Shape	54
		3.4.2	Rate Stability	55
		3.4.3	Radioactive Source Fluence	57
	3.5	Pixel (	Centroids and Areas	58
		3.5.1	Procedure	58
		3.5.2	Analysis and Results	61
	3.6	Quant	um Efficiency Measurements	62
		3.6.1	Procedure	63
		3.6.2	Analysis and Results	64
	3.7	Transp	parency	66
		3.7.1	Beryllium Windows	66
		3.7.2	Optics Cover	70
	3.8	Summ	ary	71
Pa	art T	wo: M	asses of Neutron Stars	73
4	Hig	h-Mas	s X-ray Binaries	<b>74</b>
	4.1	Weigh	ing in on Neutron Stars	74
	4.2	High-N	Mass X-ray Binaries	77
	4.3	NS ma	ass measurements in HMXBs	78
		4.3.1	Method	80
		4.3.2	Observations	84
		4.3.3	Data Reduction and Analysis	85
5	X-N	las at	Palomar	88
	5.1	IGR J	17544-2619	90
	5.2	SAX J	2103.5+4545	93

	5.3	$1H2138\pm579$	96
	5.5	CDO 19959 + 49	00
	0.4	GRO J2058+42	98
6	Mas	ss of the Compact Object in XMMU J013236.7+303228	100
	6.1	Introduction	101
	6.2	Observations And Data Reduction	104
	6.3	Donor Star Parameters and Orbit	108
		6.3.1 Stellar Parameters	108
		6.3.2 Orbital Parameters	112
	6.4	Component Masses	115
		6.4.1 The Spectroscopic Method	116
		6.4.2 Masses From Roche Lobe Constraints	121
	6.5	Conclusion	122
-		White Drand Commentary of a 2 M. Northern Sterr	105
1	The	white Dwarf Companion of a 2 $M_{\odot}$ Neutron Star	127
	7.1	PSR J1614–2230	127
	7.2	Observations at the W. M. Keck Observatory	128
	7.3	Detection of an Optical Counterpart	131
	7.4	Pulsar age and birth spin period	135
8	Cor	clusions and Future Work	139
Ũ	001		100
Α	The	Polar Catalysmic Variable 1RXS J173006.4+033813	143
	A.1	Introduction	144
	A.2	Observations	145
		A.2.1 Optical Photometry	145
		A.2.2 Spectroscopy	148
		A.2.3 X-ray and UV Observations	153
	A.3	Nature Of The Components	153
		A.3.1 Red Component	154
		A.3.2 Blue Component	155
	A.4	System Parameters	161
		A.4.1 Orbit	161

A.4.2 Photometric Variability	
A.4.3 Mass Ratio	
A.4.4 Distance	
A.5 Conclusion	
B Transformation of a Star into a Planet in a Millised	cond Pulsar Binary 171
Bibliography	184

## List of Figures

1.1	The electromagnetic spectrum	3
1.2	Imaging with a coded aperture mask	7
1.3	Wolter-I focusing optics	8
1.4	Schematic of NuSTAR	10
1.5	NuSTAR effective area	11
1.6	NuSTAR off-axis response	13
2.1	X-ray absorption in various materials	15
2.2	NuSTAR hybrid	18
2.3	Schematic of a NuSTAR detector	19
2.4	Working principle of CdZnTe detectors	21
2.5	NuSTAR event data packet format	24
2.6	dead-time in detectors	26
2.7	Count rate conversion	27
2.8	Event grades	31
2.9	Sample CdZnTe spectrum	35
3.1	NuSTAR Focal Plane Module	39
3.2	Overview of the calibration procedure	43
3.3	XRG setup: schematic	47
3.4	XRG setup: photograph	48
3.5	Simulated X-ray beam size	49
3.6	XRG setup—cooling system	51
3.7	StageGUI control software	53
3.8	XRG beam shape	55

3.9	XRG stability measurements	56
3.10	XRG spectra	60
3.11	XRG scan procedure	61
3.12	Repeatability of centroid measurements	63
3.13	Absolute QE of hybrids	65
3.14	Relative QE measurements	66
3.15	Attenuation curves for the Be window	67
3.16	Thickness of flight Be windows	69
3.17	Test setup for optics thermal cover	70
4.1	Theoretical mass–radius relationships for neutron stars	75
4.2	Orbital elements	81
5.1	Optical spectrum IGR J17544-2619	90
5.2	Radial velocity fit for IGR J17544-2619	91
5.3	Lower limits on $M$ for IGR J17544-2619	92
5.4	Optical spectrum SAX J2103.5+4545	94
5.5	Radial velocity fit for SAX J2103.5+4545	95
5.6	Optical spectrum 1H 2138+579	96
5.7	Radial velocity measurements for 1H 2138+579	97
5.8	Optical spectrum GRO J2058+42	98
5.9	Representative orbit for GRO J2058+42	99
6.1	Optical counterpart to XMMU J013236.7+303228	103
6.2	Observed spectrum and best-fit model for XMMU J013236.7+303228 $\ldots$ .	106
6.3	Observed red spectrum for XMMU J013236.7+303228	107
6.4	Radius–temperature constraint from the observed luminosity	111
6.5	The radial velocity curve for XMMU J013236.7+303228	113
6.6	Mass–radius relation for the OB star	118
6.7	Compact object mass $(M_{-})$ as a function of OB star mass $(M_{-})$	119
6.8	Evolutionary tracks and isochrones for massive stars	120
6.9	Probability density plot for NS mass as a function of OB star mass	123

7.1	LRIS images of PSR J1614–2230	133
7.2	Inferred parameters of PSR J1614–2230 as a function of distance $\ldots$ .	134
7.3	Pulsar $P - \dot{P}$ diagram	136
8.1	HMXBs with measured NS masses	139
8.2	Masses of Black Holes	141
A.1	Finder chart for 1RXS J1730+03	149
A.2	P60 photometry of 1RXS J1730+03	151
A.3	i' band P60 photometry: Epochs 1 to 28	152
A.4	$i'$ band LFC photometry of 1RXS J1730+03 in quiescence $\hdots \hdots $	154
A.5	Photometric evolution of 1RXS J1730+03 in $i'$ band $\ldots \ldots \ldots \ldots$	156
A.6	Temporal evolution of 1RXS J1730+03 spectra	157
A.7	Keck NIRSPEC spectrum of 1RXS J1730+03	158
A.8	Comparison with M-dwarf spectra	159
A.9	Cyclotron harmonics in blue spectrum	160
A.10	Velocity measurements 1RXS J1730+03	162
A.11	Velocity modulation of H $\alpha$ and the 8184/8195 Å Na I doublet	163
A.12	Fourier transform of $i'$ photometric data	165
A.13	Range of masses for components of 1RXS J1730+03	168
B.1	Pulse timing residuals for PSR J1719–1438	181
B.2	Locus of the companion mass and Roche Lobe radii for PSR J1719 $-1438$ .	182
B.3	Keck/LRIS 20 minute $R$ -band image of the PSR J1719-1438 field	183

## List of Tables

1.1	Currently operating X-ray telescopes compared to NuSTAR $\ldots$	6
1.2	Sensitivity of hard X-ray telescopes	10
1.3	A representative list of NuSTAR science targets	12
2.1	NuSTAR focal plane configuration summary	17
2.2	Observed count rate $(R_o)$ as a function of incident count rate $(R_i)$	28
2.3	Data-processing overview	29
3.1	Instrument-level calibration requirements	41
3.2	X-ray generator settings for hybrid scans	59
3.3	Be window composition	68
3.4	Be window transmission	68
4.1	Masses of neutron stars in high-mass X-ray binaries	79
5.1	DBSP observations	89
6.1	Details of individual exposures	105
6.2	System parameters for XMMU J013236.7+303228	114
6.3	System parameters for SMC X-1 and LMC X-4	124
7.1	Positions and magnitudes of reference stars	129
7.2	Coordinates of PSR J1614–2230 at different epochs	130
A.1	Photometry of 1RXS J1730+03	146
A.2	Photometry of reference stars for 1RXS J1730+03	147
A.3	Observation log for <i>Swift</i> ToO observations of 1RXS J1730+03	150

A.4	Locations of cyclotron harmonics.	155
A.5	Radial velocity of the M-dwarf.	164
A.6	Orbital velocity parameters of the M-dwarf.	165

## List of Acronyms

ADC: analog-to-digital convertor AGN: active galactic nuclei ASIC: application-specific integrated circuit BH: black hole cps: counts per second DBSP: double beam spectrograph EOS: equation of state ESD: electrostatic discharge FITS: flexible image transport system FOV: field of view FPGA: field programmable gate array FPM: focal plane module FWHM: Full Width at Half Maximum GUI: graphical user interface HEASARC: high energy astrophysics science archive research center HMXB: high-mass X-ray binary HPD: half power diameter HV: high voltage IC: integrated circuit IR: infrared LRIS: low resolution imaging spectrograph MISC: minimum instruction set computer MOC: mission operations center NRL: naval research laboratory

NS: neutron star

NuSTAR nuclear spectroscopic telescope array

NuSTARDAS: NuSTAR data analysis software

OGIP: office of guest investigator programs

PH: pulse height

PI: pulse invariant

PMT: photomultiplier tube

PSF: point-spread function

RMF: redistribution matrix file

QE: quantum efficiency

RV: radial velocity

SAA: south atlantic anamoly

SFXT: supergiant fast X-ray transient

SMBH: super massive black hole

SMEX: small explorer

SNR: signal-to-noise ratio

SOC: science operations center

SRL: space radiation laboratory

ToO: target of opportunity

XRB: X-ray binary

# Part One: NuSTAR



# Characterization of CdZnTe Detectors for NuSTAR

Image: NuSTAR satellite at Orbital Sciences Corporation

# NuSTAR

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## Part Two: Masses of Neutron Stars



# X-Mas: A Search for eXtra Massive Neutron Stars

Image: Artists illustration of a galactic Black Hole High-Mass X-ray Binary Cygnus X-1. Credit: ESA/Hubble, via Wikimedia Commons.

# Neutron Stars

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### Appendix A

## The Polar Catalysmic Variable 1RXS J173006.4+033813

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### Abstract

We report the discovery of 1RXS J173006.4+033813, a polar cataclysmic variable with a period of 120.21 min. The white dwarf primary has a magnetic field of  $B = 42_{-}$  MG, and the secondary is a M3 dwarf. The system shows highly symmetric double peaked photometric modulation in the active state as well as in quiescence. These arise from a combination of cyclotron beaming and ellipsoidal modulation. The projected orbital velocity of the secondary is  $K = 390 \pm 4 \text{ km s}^{-}$ . We place an upper limit of 830 ± 65 pc on the distance.

*Keywords:* binaries: close—binaries: spectroscopic—novae, cataclysmic variables—stars: individiual (1RXS J173006.4+033813)—stars: variables: other

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### A.1 Introduction

Cataclysmic Variables (CVs) are close interacting binary systems in which a white dwarf (WD) accretes material from a Roche lobe filling late-type secondary star (Warner, 1995; Hellier, 2001). In most non-magnetic CVs (B < 10 G), the material lost from the secondary does not directly fall onto the WD because of its large specific orbital momentum: instead, it settles down in an accretion disc around the WD.

The accretion disc is the brightest component of the CV due to the large gravitational energy release in viscous accretion. The disc dominates the emission from the WD and donor over a wide wavelength range.

On the other hand, the accretion geometry in magnetic CVs is strongly influenced by the WD magnetic field. Magnetic CVs are broadly divided into two subclasses: Polars and Intermediate Polars (IPs). Polars usually show a synchronous or near synchronous rotation of WD with the orbital motion of the binary system and have high magnetic fields (B > 10 MG) (for a review, see Cropper, 1990). In IPs the WD rotation is far from synchronous and typically have magnetic field, B < 10 MG (for a review, see Hellier, 2002). The strong magnetic field in polars deflects the accretion material from a ballistic trajectory before an accretion disc can form, channeling it to the WD magnetic pole(s). The infalling material forms a shock near the WD surface, which produces radiation from X-rays to infrared wavelengths. Electrons in the ionized shocked region spiral around the magnetic field lines and emit strongly polarized cyclotron radiation at optical and infrared wavelengths. Polars exhibit X-ray on (high) and off (low) states more frequently than the other variety of CVs (Ramsay et al., 2004).

1RXS J173006.4+033813 (hereafter 1RXS J1730+03) is a Galactic source that is highly variable in the optical and X-ray, exhibiting dramatic outbursts of more than 3 magnitudes in optical. It was discovered by the ROSAT satellite during its all-sky survey (Voges et al., 1999). Denisenko et al. (2009), in the course of their investigation of poorly studied ROSAT sources, reported that USNO-B1.0 object 0936-00303814 which is within the 10" (radius) localization of the X-ray source showed great variability ( $\Delta R$  of up to 3 mag) in archival data (Palomar Sky Survey; SkyMorph/NEAT). During certain epochs the source appears to have been undetectable ( $m_R > 20$  mag). Denisenko et al. (2009) undertook observations with Kazan State University's 30-cm robotic telescope and found variability on rapid timescales of 10 minutes.

In this paper, we report the results of our photometric, spectroscopic and X-ray followup of 1RXS J1730+03.

### A.2 Observations

#### A.2.1 Optical Photometry

We observed 1RXS J1730+03 with the Palomar Robotic 60-inch telescope (P60; Cenko et al., 2006) from UT 2009 April 17 to UT 2009 June 5, and with the Large Format Camera (LFC; Simcoe et al., 2000) at the 5 m Hale telescope at Palomar on UT 2009 August 26. Here we give details of the photometry.

We define a photometric epoch as observations from a single night when the source could be observed. We obtained 28 epochs with the P60, subject to scheduling and weather constraints. A typical epoch consists of consecutive 90–120 s exposures spanning between 30–300 minutes (Table A.1). We obtained g', r', i' photometry on the first and third epochs. After the third epoch, we continued monitoring the source only in i' band.

We reduced the raw images using the default P60 image analysis pipeline. LFC images were reduced in IRAF. We performed photometry using the IDL DAOPHOT package (Landsman, 1993). Fluxes of the target and reference stars (Figure A.1) were extracted using the APER routine. For aperture photometry, the extraction region was set to one seeing radius, as recommended by Mighell (1999). The sky background was extracted from an annular region 5–15 seeing radii wide. We used flux zero points and seeing values output by the P60 analysis pipeline. Magnitudes for the reference stars were calculated from a few images. The magnitude of 1RXS J1730+03 was calculated relative to the mean magnitude of a 9 reference stars for LFC images, and 15 reference stars for P60 images (Table A.2). The LFC images (Figure A.1) resolve out a faint nearby star ( $m_{i'} = 20.8$ ), 3".4 from the target. The median seeing in P60 data is 2".1 (Gaussian FWHM): so there is a slight contribution from the flux of this star to photometry of 1RXS J1730+03. We do not correct for this contamination. The statistical uncertainty in magnitudes is ~ 0.2 mag for P60 and

<sup>&</sup>lt;sup>1</sup>http://iraf.noao.edu/

<sup>&</sup>lt;sup>2</sup>http://www.ittvis.com/ProductServices/IDL.aspx

Date (UT)	HJD	Filter name	Exposure time (sec)	Magnitude	Error
20090417	54938.832278	$g^{\prime}$	120	20.8	0.13
20090417	54938.835488	i'	90	19.39	0.05
20090417	54938.838696	$g^{\prime}$	90	20.75	0.13
20090417	54938.839953	i'	90	19.17	0.05
20090417	54938.841212	$g^{\prime}$	90	20.67	0.13
20090417	54938.842469	i'	90	19.1	0.05
20090417	54938.843727	$g^{\prime}$	90	20.63	0.12
20090826	55069.691401	lfci'	60	20.4	0.05
20090826	55069.693218	lfci'	60	20.04	0.06

Table A.1. Photometry of 1RXS J1730+03

Note. — This table is available in a machine readable form online. A part of the table is reproduced here for demonstrating the form and content of the table.

Filters g', r' and i' denote data acquired at P60 in the respective filters, lfci' denotes data acquired in the i' band with the Large Format Camera at the Palomar 200" Hale telescope

Relative photometry error. Values do not include an absolute photometry uncertainty of 0.16 mag in the g' band, 0.14 mag in the r' band and 0.06 mag in the i' band. Absolute photometry is derived from default P60 zero point calibrations.

Identifier <sup>a</sup>	Right Ascension	Declination	g' magnitude	r' magnitude	i' magnitude
А	262:30:21.99	03:38:37.5	$15.861 \pm 0.003$	$15.600 \pm 0.003$	$15.341 \pm 0.003$
В	262:30:14.57	03:37:11.0	$17.372 \pm 0.009$	$17.153 \pm 0.006$	$16.872 \pm 0.008$
C, 10	262:32:45.57	03:37:17.0	$16.879 \pm 0.006$	$16.691 \pm 0.005$	$16.423 \pm 0.006$
D, 9	262:32:13.84	03:38:03.0	$18.161 \pm 0.016$	$17.929 \pm 0.010$	$17.660 \pm 0.013$
E	262:31:00.31	03:38:31.3	$18.518 \pm 0.020$	$17.462 \pm 0.007$	$16.811 \pm 0.007$
F	262:30:55.06	03:37:26.4	$18.530 \pm 0.022$	$18.158 \pm 0.012$	$17.816 \pm 0.016$
G, 8	262:31:57.98	03:38:03.9	$18.621 \pm 0.022$	$18.259 \pm 0.012$	$17.905 \pm 0.016$
Н	262:30:41.22	03:38:32.8	$16.770 \pm 0.006$	$16.081 \pm 0.004$	$15.688 \pm 0.004$
Ι	262:29:45.31	03:38:43.7	$17.661 \pm 0.011$	$17.302 \pm 0.007$	$16.969 \pm 0.008$
1	262:32:01.97	03:40:28.3			$17.059 \pm 0.035$
2	262:31:44.94	03:39:48.6			$19.855 \pm 0.043$
3	262:32:31.60	03:39:32.4			$19.148 \pm 0.039$
4	262:32:33.94	03:38:59.4			$17.622 \pm 0.033$
5	262:32:11.15	03:38:39.0			$20.777 \pm 0.049$
6	262:31:35.94	03:38:29.5			$19.843 \pm 0.026$
7	262:31:07.21	03:37:57.9			$19.057 \pm 0.026$
11	262:31:55.09	03:36:45.4			$17.471 \pm 0.030$
12	262:31:40.33	03:36:34.5			$16.339 \pm 0.044$
13	262:33:19.44	03:36:21.2			$18.006 \pm 0.030$
14	262:31:45.44	03:36:12.4			$18.085 \pm 0.048$
15	262:32:18.64	03:35:48.1			$17.392 \pm 0.055$

Table A.2. Photometry of reference stars for 1RXS J1730+03

а

Ь

r'

i'

g'

~ 0.05 mag for LFC, and the systematic uncertainty is 0.16 mag in the g' band, 0.14 mag in the r' band and 0.06 mag in the i' band.

The resultant lightcurves are shown in Figures A.2, A.3 & A.4. Table A.1 provides the photometry.

#### A.2.2 Spectroscopy

We obtained optical and near-infrared spectra of 1RXS J1730+03 at various stages after outburst (Figure A.5). The first optical spectra were taken 13 days after the first photometric epoch. We used the Low Resolution Imaging Spectrograph on the 10 m Keck-I telescope (LRIS; Oke et al., 1995), with upgraded blue camera (McCarthy et al., 1998; Steidel et al., 2004), covering a wavelength range from 3,200 Å – 9,200 Å. We acquired more optical data 34 days after outburst, with the Double Beam Spectrograph on the 5 m Hale telescope at Palomar (DBSP; Oke & Gunn, 1982). We took 5 exposures spanning one complete photometric period, covering the 3,500 Å – 10,000 Å wavelength range. We took late time spectra covering just over one photometric period for the quiescent source with the upgraded LRIS . At this epoch, we aligned the slit at a position angle of 45 degrees to cover both the target and the contaminator, 3".4 to its South West (Figure A.1). We also obtained low resolution J-band spectra with the Near InfraRed Spectrograph on the 10 m Keck-II telescope (NIRSPEC; McLean et al., 1998). 12 spectra of 5 minutes each were acquired, covering the wavelength region from 11,500 Å – 13,700 Å. For details of the observing set up, see the notes to Table A.5.

We analyzed the spectra using IRAF and MIDAS and flux calibrated them using appropriate standards. Wavelength solutions were obtained using arc lamps and with offsets determined from sky emission lines. Figure A.6 shows an optical spectrum from each epoch, while the IR spectrum is shown in Figure A.7.

The second LRIS epoch had variable sky conditions. Here, we extracted spectra of the aforementioned contaminator. This object is also a M-dwarf, hence both target and contaminator spectra will be similarly affected by the atmosphere. We estimate the i'magnitude of the contaminator in each spectrum, and compare it to the the value measured

<sup>&</sup>lt;sup>3</sup>http://www2.keck.hawaii.edu/inst/lris/lris-red-upgrade-notes.html

<sup>&</sup>lt;sup>4</sup>Munich Image Data Analysis System; http://www.eso.org/sci/data-processing/software/esomidas/



Figure A.1. Finder chart for 1RXS J1730+03 (α = 17<sup>h</sup>30<sup>m</sup>06<sup>s</sup>.19, δ = +03°38'18".8). This i' band image was acquired with the Large Format Camera (LFC) at the 5 m Hale telescope at Palomar. Stars numbered 1–15 in red are used for relative photometry in LFC data. Stars labeled A–I in blue are used for relative photometry in P60 data (Section A.2.1). The green circle shows the 5" extraction region used for calculating UVOT fluxes. The circle includes a contaminator, 3".4 to the South-West of the target.

Obs ID	Start Date & Time	Stop Time	Exposure (s)	Filter	Wavelength (Å)	Magnitude	Flux	$ m Flux$ $(\mu Jy)$
00035571001	2006 Feb 9 16:56:43	18:42:00	1106	UVM2	2231	$17.9 \pm 0.1$	31±2	51±3
00031408001	2009 May 3 18·28·56	19.02.12	1964	XRT UVM2	2231	20 44+0 21	0.02 3 04+0 59	0.06 (5  keV) $5.05\pm0.99$
00031408002	2009 May 4 18:34:04	22:12:54	4896	UVW1	2634	$20.14 \pm 0.10$	$3.47 \pm 0.32$	$8.04 \pm 0.75$
00031408003	2009 May 6 03:02:21	15:36:33	5621	UVW2	2030	$21.48 {\pm} 0.17$	$1.38 {\pm} 0.22$	$1.93 {\pm} 0.30$
				XRT			< 0.002	< 0.006 (5  keV)

Table A.3. Observation log for *Swift* ToO observations of 1RXS J1730+03.

Effective wavelength for each filter for a Vega-like spectrum (Poole et al., 2007).

Flux in the units of  $10^-$  erg cm<sup>-</sup> s<sup>-</sup> A<sup>-</sup>.

Counts  $s^-$  in 0.5-10 keV.



Figure A.2. P60 photometry of 1RXS J1730+03. Top panel: Epoch 1 photometry in g' and i' bands. Bottom panel: Epoch 3 photometry in r' and i' bands.



Figure A.3. i' band P60 photometry of 1RXS J1730+03, for Epochs 1 to 28. The source was in outburst in Epoch 1 and slowly faded into quiescence. The error bars denote relative photometry errors and do not include an absolute zero point error of 0.064 mag (§ A.2.1). The solid blue line denotes the best fit sinusoid to the photometric data. The dashed green line is added to show the relative phase of the source in outburst, these epochs were not used for fitting the lightcurve.

from the LFC images to estimate and correct for the extinction by clouds.

#### A.2.3 X-ray and UV Observations

We observed the 1RXS J1730+03 with the X-ray telescope (XRT) and the UV-Optical Telescope (UVOT) onboard the *Swift* X-ray satellite (Gehrels et al., 2004) during UT 2009 May 3-6 for a total of about 12.5 ks. The level-two event data was processed using *Swift* data analysis threads for the XRT (Photon counting mode; PC) using the HEASARC FTOOLS software package. The source was not detected in the X-ray band.

We follow the procedures outlined by Poole et al. (2007) for analyzing the UVOT data. The measured fluxes are given in Table A.3. The contaminator is within the recommended 5" extraction radius. Hence, flux measurements are upper limits.

Shevchuk et al. (2009) had observed 1RXS J1730+03 on UT 2006 February 9 with the *Swift* satellite as a part of investigations of unidentified ROSAT sources. They detected the source with a count rate of 0.02 counts s<sup>-</sup>. The best-fit power law has a photon index  $\Gamma = 1.8 \pm 0.5$  and a 0.5–10 keV flux of  $1.2 \times 10^{-10}$  erg cm<sup>-</sup> s<sup>-</sup>. After converting to the ROSAT bandpass assuming the XRT model parameters, this value is approximately a factor of two lower than the archival ROSAT flux. They report a much higher UV flux in their observations, which suggests that the source was in an active state during their observations.

The column density inferred from the XRT data is low,  $N \sim 7 \times 10$  cm<sup>-</sup>. From ROSAT data, this column density corresponds to A = 0.39, which gives A = 0.84 (Cox, 2000). For comparison, Schlegel et al. (1998) give the Galactic dust extinction towards this direction ( $l = 26.^{\circ}7$ ,  $b = 19^{\circ}.7$ ) to be E(B - V) = 0.141 mag (A = 0.44), corresponding to a column density of about  $8 \times 10$  cm<sup>-</sup>.

### A.3 Nature Of The Components

The optical spectra (Figure A.6) show rising flux towards the red and blue ends of the spectrum: indicative of a hot (blue) and cool (red) component. The red part of the spectrum shows clear molecular features, characteristic of late type stars. The blue component is

<sup>&</sup>lt;sup>5</sup>http://heasarc.gsfc.nasa.gov/ftools/; Blackburn (1995)



Figure A.4. i' band LFC photometry of 1RXS J1730+03 in quiescence, 131 days after we first saw high variability. The variations have the same phase and period as observed during outburst. See Figure A.3 for details.

devoid of any prominent absorption/emission features. From the overall spectral shape we infer that 1RXS J1730+03 is a CV.

#### A.3.1 Red Component

The red component of 1RXS J1730+03 is typical of a late type star. In Figure A.8, we compare the red side spectrum of 1RXS J1730+03 with several M-dwarfs. From the shape of the TiO bands at 7053 Å – 7861 Å, we infer that the spectral type to be M3 $\pm$ 1. This is consistent with the relatively featureless J band spectrum (McLean et al., 2003). The spectral type indicates an effective temperature of 3400 K (Cox, 2000). The presence of a sodium doublet at 8183/8195 Å implies a luminosity class V.

We also fit the spectrum with model atmospheres calculated by Munari et al. (2005). For late type stars, these models are calculated in steps of  $\Delta T = 500$  K,  $\Delta \log g = 0.5$  and  $\Delta$ [M/H] = 0.5. We use model atmospheres with no rotational velocity (V = 0 km s<sup>-</sup>) and convolve them with a kernel modeled on the seeing, slit size and pixel size. We ignore the regions contaminated by the telluric A and B bands (7615 Å and 6875 Å). The unknown contribution from the white dwarf was fit as a low order polynomial. We correct for extinction using A = 0.39 from X-ray data (Section A.2.3). To measure log g, we use the

Harmonic number	Measured Wavelength (Å)	Measured Frequency (Hz)	Inferred Wavelength (Å)
7	3540	$8.4 \times 10$	3664
6	4440	$6.7 \times 10$	4275
5	5180	$5.7 \times 10$	5130
4	6770	$4.4 \times 10$	6413
3	8225	$3.6 \times 10$	8551
2			12826
1			25653
a			В

Table A.4. Locations of cyclotron harmonics.

spectrum in the 8,000 Å – 8,700 Å region, which is expected to have fairly little contamination from the blue component. This region includes the Ca II lines at 8498, 8542 Å and the Na I doublet, which are sensitive to log g. We then fit the spectra in the 6,700 Å – 8,700 Å range to determine the temperature and metallicity. The best fit model has T = 3500 K, log g = 5.0 and solar metallicity, consistent with our determination of the spectral type.

Kolb et al. (2001) state that unevolved donors in CVs follow the spectral type-mass relation of the zero age main sequence, as the effects of thermal disequilibrium on the secondary spectral type are negligible. For a M3 star, this yields a mass of 0.38  $M_{\odot}$ . As the secondaries evolve, the spectral type is no longer a good indicator of the mass and gives only an upper limit on the mass. The lower limit can simply be assumed to be the Hydrogen-burning limit of 0.08  $M_{\odot}$ .

#### A.3.2 Blue Component

The blue component of 1RXS J1730+03 is consistent with a highly magnetic white dwarf. The blue spectrum is suggestive of a hot object, but does not show any prominent absorp-



Figure A.5. Photometric evolution of 1RXS J1730+03 in i' band. Data for each epoch was fit with a sinusoid with the same period for all epochs. In contrast to Figures A.3 & A.4, the phase was allowed to vary independently for each epoch. Top: average i' magnitude for each P60 observation epoch, as a function of time. Blue arrows mark spectroscopy epochs. Bottom: semi-amplitude of sinusoidal variations as a function of the corresponding mean i' magnitudes for each epoch.


Figure A.6. Temporal evolution of 1RXS J1730+03 spectra. Some spectra are not corrected for Telluric absorption, the affected regions are diagonally hatched. The first spectrum was obtained 13 days after we measured high variability, the second after 34 days, and the lowermost spectrum after 60 days. The spectra show broad Balmer features which evolve with time. The M-dwarf features (TiO, Na I) are clearly seen at all times.

tion/emission features. H $\alpha$  is seen in emission, but other Balmer features are not detected. The spectrum (Figure A.6) shows cyclotron humps, suggesting the presence of a strong magnetic field. The polar nature of the object is supported by the absence of an accretion disc, and the transition from an active state to an off state in X-rays (Section A.1, Section A.2.3).



Figure A.7. Keck NIRSPEC spectrum of 1RXS J1730+03. The spectrum is flat and nearly featureless, as expected for early M stars.

For analyzing the WD spectrum, we subtracted a scaled spectrum of the M-dwarf GL 694 from the composite spectrum of 1RXS J1730+03. The resultant spectrum (Figure A.9) clearly shows cyclotron harmonics. The hump seen in the J-band spectrum (Figure A.7) is also inferred to be a cyclotron harmonic. A detailed modeling of the magnetic field is beyond the scope of this work, but we use a simple model to estimate the magnetic field. We fit the cyclotron humps with Gaussians and measure the central wavelengths (Table A.4). We then fit these as a series of harmonics, and infer that the cyclotron frequency is  $\nu = 1.17 \times 10$  Hz. The magnetic field in the emission region is given by,  $B = (\nu / 2.8 \times 10 \text{ Hz}) \cdot 10$  G = 42 × 10 G.

As a conservative error estimate, we consider the worst case scenario where our identified locations for the cyclotron humps are off by half the spacing between consecutive cyclotron harmonics. Using this, we estimate the errors on the magnetic field:  $B = 42_{-}$  MG.



Figure A.8. Comparison of red part of 1RXS J1730+03 spectrum with M-dwarf spectra. Some spectra are not corrected for Telluric absorption, the affected regions are diagonally hatched. Prominent bands (TiO, CaH) and lines (Hα, Na I) are marked. Comparing the shape of the TiO bands at 7053–7861 Å and the shape of the continuum redwards of 8200 Å, we infer that spectral type of the red component to be M3. The presence of a sodium doublet at 8183/8195 Å implies a luminosity class V.



Figure A.9. Blue component spectra of 1RXS J1730+03, showing the 12 late-time LRIS exposures (Section A.2.2, Table A.5). The spectroscopic phase at mid-exposure is indicated for each spectrum. Dotted lines show spectra are obtained by subtracting a scaled spectrum of GL 694 from spectra of this binary. The overlaid solid lines are smoothed versions of the same spectra. Vertical dashed cyclotron humps at 4440 Å, 5180 Å, 6770 Å & 8225 Å. The cyclotron harmonic numbers (#3 – #6) are indicated in bold red. Two more cyclotron humps are seen in other spectra: a feature at 3540 Å (Figure A.6), and a J-band feature (Figure A.7).

## A.4 System Parameters

#### A.4.1 Orbit

We use the best fit Munari et al. (2005) model atmosphere to measure radial velocities of the M-dwarf. We vary the radial velocity of the model, and minimize the  $\chi$  over the 6,500 Å – 8,700 Å spectral region, excluding the telluric O bands. After a first iteration, the spectra are re-fit to account for motion of the M-dwarf during the integration time. For the 12 spectra taken at the second LRIS epoch, we also measure the radial velocity for the contaminator star on the slit, and find it to be constant. This serves as a useful test for our radial velocity measurement procedure. The barycentric corrected velocities are given in Table A.5.

We fit a circular orbit  $(v = \gamma + K \sin([2\pi(t-t)]/P))$  to the measured velocities. We define the superior conjunction of the WD as phase 0.

The 2009 June 16 spectroscopic data (Table A.5) give an orbital period  $P = 123 \pm 3$  min. We then use the photometric variability (Section A.4.2) to determine an accurate period in this range. Next, we refine the solution with velocity measurements from the other two spectroscopic epochs. The best-fit solution gives a period  $P = 120.2090 \pm 0.0013$  min and  $K = 390 \pm 4$  km s<sup>-</sup> (Table A.6, Figure A.10).

Figure A.11 shows sections of the last epoch spectra around H $\alpha$  and the Na I doublet at 8184/8195 Å. The Na I doublet clearly matches the velocity of the M-dwarf in the orbit, but the H $\alpha$  emission seems to have a smaller velocity amplitude. A possible explanation for this is that the H $\alpha$  emission comes from the M-dwarf surface that is closest to the WD, which may be heated by emission from the white dwarf or the accretion region.

#### A.4.2 Photometric Variability

The lightcurve of 1RXS J1730+03 shows clear periodicity (Figures A.2–A.4), with two peaks per spectroscopic period. Most of the photometric data was acquired in the i' band, which contains contribution from both the M-dwarf and a cyclotron harmonic from the emission region near the WD.

A Fourier transform of the data (Figure A.12) shows a strong peak at sixty minutes.

 $<sup>^6\</sup>mathrm{When}$  the WD is furthest from the observer along the line of sight.



Figure A.10. Velocity measurements 1RXS J1730+03. The best-fit solution gives  $P = 120.2090 \pm 0.0013 \text{ min}$ ,  $\gamma_2 = -48 \pm 5 \text{ km s}^{-1}$  and  $K_2 = 390 \pm 4 \text{ km s}^{-1}$  (Section A.4.1)



Figure A.11. Velocity modulation of  $H\alpha$  and the 8184/8195 Å Na I doublet. The spectra are offset by  $2 \times 10^{-17}$  erg cm<sup>-2</sup> s<sup>-1</sup> for clarity. The wavelengths are converted into velocities using the rest wavelengths 6563 Å and 8195 Å respectively. The vertical dotted line marks the radial velocity of the binary barycenter. The short dashed lines mark the radial velocities measured by fitting the complete spectrum. The Na I absorption follows the radial velocity of the M-dwarf, but  $H\alpha$  seems to have a smaller velocity amplitude.

	-1	
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Table A.5. Radial velocity of the M-dwarf.

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Table	e A.6.	Orbital	velocity	parameters	of	the	M-0	lwarf	Ľ
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Parameter	Value
$\gamma~(~{ m km~s^-}~)$	$-48 \pm 5$
$K \pmod{\text{s}^{-}}$	$390 \pm 4$
t (HJD)	$54998.9375 \pm 0.0003$
P (min)	$120.2090 \pm 0.0013$



Figure A.12. Upper panel: Fourier transform of all i' data. Lower panel: expected Fourier transform for a pure sinusoidal variations with a period of 60.11 min, obtained by scaling and convolving the Fourier transform of the window function with a delta function corresponding to the best-fit period.

We interpret this as a harmonic of the orbital period. To determine the exact period, we analyze the data as follows. As the object has a short orbital period, we convert all times to Heliocentric Julian Date for analysis. We fit a sinusoid  $(m + m_A \sin([2\pi(t - t )]/P)))$  to each epoch, allowing m and  $m_A$  to vary independently for each epoch, but we use the same reference time t and period P for the entire fit. The mean magnitude is correlated with the amplitude (Figure A.5). Note that the amplitude measured for the sinusoidal approximation for each epoch is always less than the actual peak-to-peak variations of the source during that epoch, as expected. The source is in the active state in the first few epochs, and we exclude epochs 1-5 from the fit, to avoid contamination from the accretion stream and/or the accretion shock.

The best-fit solution is overplotted in blue in Figures A.3 & A.4. Since epochs 1-5 were not included in the fit, a sinusoid is overplotted in dashed green to indicate the expected phase of the variations. The best-fit period is  $60.1059 \pm 0.0005$  minutes. This formally differs from the spectroscopically determined orbital period by  $2.1\sigma$ . However, this error estimate includes only statistical errors. There is some, difficult to determine, systematic error component in addition, so we do not claim any significant inconsistency.

Periodic photometric variability for 1RXS J1730+03 can be explained as a combination of two effects: cyclotron emission from the accretion region and ellipsoidal modulation. The active state is characterized by a higher mass transfer rate from the donor to the WD, and results in higher cyclotron emission. This emission is beamed nearly perpendicular to the magnetic field lines, creating an emission fan beam. For high inclination systems, the observer crosses this fan beam twice, causing two high amplitude peaks per orbit (Figure A.2). In the active state when the emission is dominated by cyclotron radiation, the minimum leads the superior conjuntion by  $\sim 47^{\circ}$ .

In ellipsoidal modulation, and the photometric minima coincide with the superior conjunction. It is observed that in quiescence, the photometric minimum leads the superior conjunction of the white dwarf by  $\sim 14^{\circ}$ . This suggests that the  $0.29 \pm 0.13$  mag variation is caused by a combination of ellipsoidal modulation and cyclotron emission from the accretion region.

## A.4.3 Mass Ratio

The semi-amplitude of the M-dwarf radial velocity, K2, gives a lower limit on the mass of the white dwarf. For a circular orbit, one can derive from Kepler's laws that:

$$M_{,} = \frac{PK}{2\pi G} = 0.52 \ M_{\odot}$$
 (A.1)

Tighter constraints can be placed on the individual component masses M, M by considering the geometry of the system. Eggleton (1983) expresses the volume radius R of the secondary in terms of the mass ratio q = M / M:

$$\frac{R}{a} = \frac{0.49q}{0.6q} \frac{1}{1 + \ln(1 + q^{-1})}$$
(A.2)

where the separation of the components is given by  $a = [P \ G(M + M)/4\pi]^{-1}$ . Thus for a fixed period  $P, R^{-1}$  depends only on  $M^{-1}$ . The radius of the white dwarf is much smaller than that of the M-dwarf. Hence, the M-dwarf will eclipse the accretion region if the inclination of the system is  $i < \sin^{-1} (R^{-1}/a)$ . Figures A.3, A.4 show that we do not detect any eclipses in the system.

Figure A.13 shows the allowed region for 1RXS J1730+03 in a WD mass-M-dwarf mass phase space. The orange dotted region is excluded as the orbital velocity would be greater than the measured projected velocity. The red hatched region is excluded by nondetection of eclipses. The allowed mass of the primary ranges from the minimum mass  $(M > 0.52 M_{\odot})$  to the Chandrashekhar limit. The mass of the secondary is bounded above by the ZAMS mass for a M3 dwarf  $(M = 0.38 M_{\odot})$ .

For a given M and a known orbital period, we can determine the radius of the secondary using Equation (A.2), and can calculate the surface gravity (log g). For 0.38  $M_{\odot} \gtrsim M \gtrsim$ 0.05  $M_{\odot}$ , log g ranges from 5.1 to 4.8. This is consistent with log g = 5.0 for the best fit M-dwarf spectrum (Section A.3.1).

The donor stars in CVs are expected to co-rotate. For 1RXS J1730+03, the highest possible rotational velocity  $v \sin i$  is ~ 160 km s<sup>-</sup> for a 0.38  $M_{\odot}$ , 0.27  $R_{\odot}$  M-dwarf and a 1.1  $M_{\odot}$  WD (Figure A.13).  $v \sin i$  will be lower if the WD is heavier or if the M-dwarf is lighter. To measure rotational broadening in the spectra, we use a higher resolution (R = 20,000) template of the best-fit model from Zwitter et al. (2004). We take a tem-



Figure A.13. The allowed range of masses (clear white region) for components of 1RXS J1730+03. The orange dotted region is excluded by the minimum inferred masses from radial velocity measurements. The red hashed region is excluded by non-detection of eclipses (Figures A.3, A.4). The black dash-dot lines show contours of constant log g. The best fit spectra yield log g = 5.0. The solid blue lines are calculated contours for the rotation velocity (km s<sup>-1</sup>) of the M-dwarf. A measurement of  $v \sin i$  will help to constrain masses of the components.

plate with zero rotation velocity and broaden it to different rotational velocities using the prescription by Gray (2005). Then we use our fitting procedure (Section A.3.1) to find the best-fit value for  $v \sin i$ . For this measurement, we use only the 12 relatively high resolution spectra from the second LRIS epoch (UT 2009 June 16). The weighted  $v \sin i$  from the twelve spectra is  $97 \pm 22$  km s<sup>-</sup>, but the measurements show high scatter, with a standard deviation of 54 km s<sup>-</sup>. We compared our broadened spectra with rotationally broadened spectra computed by Zwitter et al. (2004), and found that our methods systematically underestimate  $v \sin i$  by  $\sim 20$  km s<sup>-</sup>. We do not understand the reason for this discrepancy, hence do not feel confident enough to use this value in our analysis. A reliable measurement of  $v \sin i$  will help better constrain the masses of the two components.

#### A.4.4 Distance

We estimate the distance to 1RXS J1730+03 as follows. Our fitting procedure (Section A.3.1) corrects for extinction and separates the WD and M-dwarf components of the spectra. We correct for varying sky conditions by using a reference star on the slit. The ratio of measured flux to the flux of the best fit model atmosphere (T = 3500 K,  $\log g = 5.0$ ) is,

$$\frac{f}{f} = \left(\frac{R}{d}\right) = (6.1 \pm 1.6) \times 10^{-} \tag{A.3}$$

where d is the distance to the source, and R is given by Equation (A.2).

For 1RXS J1730+03, the maximum mass of the M-dwarf is 0.38  $M_{\odot}$ , and the corresponding radius is  $R = 0.27 R_{\odot}$ . Equation (A.3) then gives  $d = 800 \pm 110$  pc. This calculation assumes the largest possible M-dwarf radius, hence is an upper limit to distance. If the M-dwarf is lighter, say 0.1  $M_{\odot}$ , we get  $R = 0.17 R_{\odot}$ , yielding  $d = 500 \pm 70$  pc.

## A.5 Conclusion

1RXS J173006.4+033813 is a polar cataclysmic variable, similar to known well-studied systems like BL Hyi, ST LMi and WW Hor in terms of the orbital period, magnetic field and variability between active and quiescent states. This source is notable for the highly symmetric nature and high amplitude of the double–peaked variation in the active state. This suggests a relatively high angle between the rotation and magnetic axes. Polarimetric observations of the source would help to better constrain the magnetic field geometry of the system.

Most polars are discovered due to their highly variable X-ray flux. However, we mounted a followup campaign for 1RXS J1730+03 due to its unusual optical variability properties. This suggests that current and future optical synoptic surveys, such as PTF (Law et al., 2009) and LSST can uncover a large sample of polars by cross-correlating opticaly variable objects with the ROSAT catalog.

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Facilities: PO:1.5m. Hale (LFC, DBSP), Keck:I (LRIS), Keck:II (NIRSPEC), Swift

<sup>&</sup>lt;sup>7</sup>http://www.astro.caltech.edu/ptf

## Appendix B

# Transformation of a Star into a Planet in a Millisecond Pulsar Binary

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Retreived May 6, 2012. My role was restricted to optical observations and data analysis of the counterpart. <sup>1</sup>To whom correspondence should be addressed. Email: mbailes@swin.edu.au

Millisecond pulsars are thought to be neutron stars that have been spun-up by accretion of matter from a binary companion. Although most are in binary systems, some 30% are solitary, and their origin is therefore mysterious. PSR J1719–1438, a 5.7 ms pulsar, was detected in a recent survey with the Parkes 64 m radio telescope. We show that it is in a binary system with an orbital period of 2.2 h. Its companion's mass is near that of Jupiter, but its minimum density of 23 g cm<sup>-</sup> suggests that it may be an ultra-low mass carbon white dwarf. This system may thus have once been an Ultra Compact Low-Mass X-ray Binary, where the companion narrowly avoided complete destruction.

Radio pulsars are commonly accepted to be neutron stars that are produced in the supernova explosions of their progenitor stars. They are thought to be born with rapid rotation speeds ( $\sim 50$  Hz) but within a few 100,000 yr slow to longer periods because of the braking torque induced by their high magnetic field strengths ( $\sim 10$  G). By the time their rotation periods have reached a few seconds the majority have ceased to radiate at radio wavelengths. The overwhelming majority ( $\sim 99\%$ ) of slow radio pulsars are solitary objects. In contrast  $\sim 70\%$  of the millisecond pulsars (MSPs) are members of binary systems and possess spin frequencies of up to 716 Hz (Hessels et al., 2006). This is consistent with the standard model for their origin in which an otherwise dead pulsar is spun-up by the accretion of matter from a companion star as it expands at the end of its life (Bhattacharya & van den Heuvel, 1991). Through some process yet to be fully understood, the recycling not only spins up the neutron star but leads to a large reduction of the star's magnetic field strength to  $B \sim 10^{\circ}$  G and usually leaves behind a white dwarf companion of typically 0.2-0.5  $M_{\odot}$ . The lack of a compelling model for this reduction of the magnetic field strength with continuing mass accretion, and issues between the birthrates of MSPs and their putative progenitors, the low-mass X-ray binaries (LMXBs) led to an early suggestion (Grindlay & Bailyn, 1988) that accretion induced collapse of a white dwarf might form MSPs "directly" in the cores of globular clusters, and possibly in the Galactic disk.

In the standard model, the reason why some MSPs possess white dwarf companions and others are solitary is unclear. Originally it was proposed that solitary MSPs might be formed from a different channel, in which a massive  $(M > 0.7 M_{\odot})$  white dwarf coalesces with a neutron star (van den Heuvel & Bonsdema, 1984). The binary pulsar-white dwarf system PSR J1141-6545 (Kaspi et al., 2000) is destined to merge in < 2 Gyr and thus is a potential progenitor for this scenario. At lower white dwarf masses, the final product is less clear, as the mass transfer can stabilise (Bonsema & van den Heuvel, 1985). From an observational point of view, the "black widow" MSPs may give some insights. In these systems an MSP is usually accompanied by a low-mass ~ 0.02-0.05 M<sub> $\odot$ </sub> companion in close orbits of a few hours. It was initially believed these systems might evaporate what was left of the donor star (Fruchter et al., 1988), but other examples (Stappers et al., 1998) meant that the timescales were too long.

The MSP population was further complicated by the detection of an extra-solar planetary system in orbit around the fifth MSP found in the Galactic disk, PSR B1257+12 (Wolszczan & Frail, 1992). This system has two ~3 Earth-mass planets in 67- and 98-day orbits, and a smaller body of lunar mass in a 25 d orbit. The planets were probably formed from a disk of material. The origin of this disk is however the subject of much speculation, ranging from some catastrophic event in the binary that may have recycled the pulsar (Wijers et al., 1992) to ablation (Rasio et al., 1992) and supernova fall-back (Hansen et al., 2009). A large number of potential models for the creation of this system have been proposed, and are summarised in the review by Podsiadlowski (1993). Although more than another 60 MSPs (P < 20 ms) have been detected in the Galactic disk since PSR B1257+12, until now none have possessed planetary-mass companions.

PSR J1719-1438 was discovered in the High Time Resolution Universe survey for pulsars and fast transients (Keith et al., 2010). This P = 5.7 ms pulsar was also detected in archival data from the Swinburne intermediate latitude pulsar survey (Edwards et al., 2001). Its mean 20 cm flux density is just 0.2 mJy but at the time of discovery was closer to 0.7 mJy due to the effects of interstellar scintillation. We soon commenced regular timing of the pulsar with the Lovell 76-m telescope that soon revealed that the pulsar was a member of a binary with an orbital period of 2.17 h and a projected semi-major axis of just  $a \sin i=1.82$  ms (Figure B.1). Since then we have performed regular timing of the pulsar at the Parkes and Lovell telescopes that have enabled a phase-coherent timing solution over a one year period. There is no evidence for any statistically significant orbital eccentricity with a formal 2- $\sigma$  limit of e < 0.06.

With these observations, we can explore the allowed range of companion masses from the binary mass function that relates the companion mass m, orbital inclination angle iand pulsar mass m to the observed projected pulsar semi-major axis a, orbital period Pand gravitational constant G:

$$f(m_c) = \frac{4\pi}{G} \frac{(a \sin i)}{P} = \frac{(m_c \sin i)}{(m_c + m_p)} = 7.85(1) \times 10^- \quad M_{\odot}$$
(B.1)

Only a few MSPs in the Galactic disk have accurate masses (Jacoby et al., 2005; Verbiest et al., 2008; Demorest et al., 2010), and these range from 1.4–2.0 M<sub> $\odot$ </sub>. Assuming an edge-on orbit (sin i = 1) and pulsar mass  $m = 1.4 \text{ M}_{\odot} m > 1.15 \times 10^{-1} \text{ M}_{\odot}$ , ie approximately the mass of Jupiter.

We can accurately determine the component separation (a = a + a) for the PSR J1719–1438 binary given the observed range of MSP masses using Kepler's third law and because,  $m \ll m$ , to a high degree of accuracy,

$$a = 0.95 R_{\odot} \left(\frac{m}{1.4 M_{\odot}}\right) \tag{B.2}$$

making it one of the most compact radio pulsar binaries. For large mass ratios, the Roche Lobe radius of the companion (Paczynski, 1971) is well approximated by

$$R = 0.462a \left(\frac{m}{m+m}\right)$$
 (B.3)

and dictates the maximum dimension of the companion star. For  $i = 90^{\circ}$  and a 1.4 M<sub> $\odot$ </sub> neutron star, the minimum  $R = 2.8 \times 10$  km, just 40% of that of Jupiter. On the other hand, for a pulsar mass m = 2 M<sub> $\odot$ </sub>, and  $i = 18^{\circ}$  (the chance probability of  $i > 18^{\circ}$  is ~95%), then  $R = 4.2 \times 10$  km.

A lower limit on the density  $\rho$  (the so-called mean density-orbital period relation, Frank et al., 1985) can be derived by combining the above equations.

$$\rho = \frac{3\pi}{0.462 \ GP} = 23 \ \text{g cm}^- \tag{B.4}$$

This density is independent of the inclination angle and the pulsar mass and far in excess

of that of Jupiter or the other gaseous giant planets whose densities are  $< 2 \text{ g cm}^-$ .

The mass, radius and hence the nature of the companion of PSR J1719–1438 are critically dependent upon the unknown angle of orbital inclination. After PSR J1719–1438, PSR J2241–5236 (Keith et al., 2011) has the smallest mass function of the other binary pulsars in the Galactic disk, albeit 1000 times larger (Figure B.2). The sin *i*-dependence of the mass function could mean that PSR J1719–1438 is a physically similar system, but just viewed face-on. This would require an inclination angle of just  $i = 5.7^{\circ}$ , for which the chance probability is 0.5%. The only binary pulsar with a similar orbital and spin period is PSR J2051–0827, but the inclination angle required for mass function equivalence in this case has a chance probability of only 0.1%. Of course, as the known population of black widow systems increases, we will eventually observe examples of face-on binaries that mimic those with planetary-mass companions. The current distribution of mass functions among the known population is such that this is still unlikely.

If the pulsar were energetic and the orbit edge-on, we might hope to detect orbital modulation of the companion's light curve in the optical because the pulsar heats the near-side. Our pulsar timing indicates the pulsar's observed frequency derivative  $\dot{\nu}$  is  $-2.2(2)\times10^{-}$  s<sup>-</sup>, not atypical of MSPs. However  $\dot{\nu}$  is only an upper limit on the intrinsic frequency derivative (Camilo et al., 1994) ( $\dot{\nu}$ ), which is related to the pulsar's distance d and transverse velocity V by the Shklovskii relation.

$$\dot{\nu} = \dot{\nu} - \nu V / (dc) \tag{B.5}$$

MSPs have relatively high velocities (Toscano et al., 1999) of 50-200 km s<sup>-</sup>. At the nominal distance of the pulsar from its dispersion measure (1.2 kpc; Cordes & Lazio, 2002) it would take an MSP transverse velocity of only 100 km s<sup>-</sup> for almost all of the observed  $\dot{\nu}$  to be caused by the proper motion of the pulsar.

In the case of negligible proper motion, we can derive the most optimistic impact of the pulsar's radiation for optical detectability by assuming isotropic pulsar emission, a companion albedo of unity, that the companion is a blackbody, and that the orbit is edgeon, thus maximising the illuminated region of the companion. The spin-down energy of a pulsar is  $\dot{E} = -4\pi I \nu \dot{\nu}$ , where I is the moment of inertia of a neutron star and  $\nu$  is the spin frequency. We find a maximum effective temperature of 4500 K and a peak R- band magnitude of 26-28, depending upon the assumed 1.2(3) kpc distance to the pulsar (Cordes & Lazio, 2002) and the unknown radius of the companion, which we assume is close to the Roche Lobe radius.

We observed the field surrounding PSR J1719–1438 with the Keck 10-m telescope in the g, R and I bands using the LRIS instrument. If the binary was a face-on analogue of PSR J2051–0827 we might expect to see a star at the location of the pulsar because the R-band magnitude of the binary pulsar companion in the PSR J2051–0827 system is  $R \sim 22.5$  (Stappers et al., 1999) and it is at a similar distance d from the Sun. The spin-down luminosity of PSR J1719–1438 is however only 0.4 L<sub> $\odot$ </sub> which is about 30% of that of PSR J2051–0827, and a face-on orbit would mean only half of the bright side of the companion was ever visible. This would mean the expected R-band magnitude would be reduced to  $R \sim 24.5$ , however at the position of the pulsar there is no visible companion down to a 3-sigma limiting magnitude of R=25.4 (1250s), g=24.1 (1000s) and I=22.5 (1000s) at the anticipated maximum light, where the values in parentheses indicate the integration times (Figure B.3). The magnitude limit would appear to reduce the probability that PSR J1719–1438 is an extremely face-on analogue of PSR J2051–0827, with the caveat that the assumed spin-down energy of the pulsar is still an upper limit because of Equation B.5.

We now consider the more statistically likely possibility that the orbit is nearly edgeon. In this case the relative velocity of the two constituents is > 500 km s<sup>-</sup> and could potentially lead to a solid-body eclipse for 60 s or so, or if the companion was being ablated we might see excess dispersive delays at orbital phase 0.25 when the pulsar is on the far side of the companion at superior conjunction. Ordinarily the 20 cm mean flux density of 0.2 mJy would make these effects difficult to detect, but a bright scintillation band occurred during one of our long integrations on the source, increasing the flux density sufficiently for us to assert that there are no excess delays or solid-body eclipses occurring in the system (Figure B.1). The extremely small dimension of the Roche lobe of the companion only precludes inclination angles of  $i > 87^{o}$ . Inspection of Figure B.2 shows that it is completely impossible to fit a hydrogen-rich planet such as Jupiter into the Roche Lobe of the planetarymass companion. Although difficult, He white dwarfs might just fit if the computational models (Deloye & Bildsten, 2003) are slightly in error (~ 10%), or the orbit is moderately face on. A carbon white dwarf on the other hand can easily fit inside the Roche Lobe for any assumed inclination angle. We thus conclude that the companion star(planet) is likely to be the remains of the degenerate core of the star that recycled the pulsar, and probably comprised of He or heavier elements such as carbon.

In the standard model, this MSP would have been spun-up by the transfer of matter from a nearby companion star to near its current period. The UC LMXBs such as XTE J0929–314 (Galloway et al., 2002) are good potential progenitors of PSR J1719–1438. These systems have orbital periods of tens of minutes and higher ( $\sim 10 \times$ ) companion masses. They have also been found to exhibit Ne and O lines in their spectra (Juett et al., 2001), suggesting that their companions are not He white dwarfs. Importantly, their spin periods are comparable to that of PSR J1719–1438. As matter is transferred from the degenerate companions to the neutron star, the orbits widen and the radius of the white dwarf expands due to the inverse mass-radius relationship for degenerate objects. Deloye & Bildsten (2003) predicted how the known UC LMXBs would evolve in the future. They demonstrated that the UC LMXB companions could be comprised of either He or Carbon white dwarfs and after 5-10 Gyr might be expected to end up as binary pulsars with orbital periods of  $\sim$ 1.5h.

If PSR J1719-1438 was once a UC LMXB, mass transfer would have ceased when the radius of the white dwarf became less than that of the Roche Lobe due to mass loss and out-spiral. In the models by Deloye and Bildsten, the He white dwarfs deviate from the  $M^-$  / law very near to the Roche Lobe radius and approximate mass of our companion star for an edge-on orbit. On the other hand, another mass-radius relationship for Carbon white dwarfs of very low mass (Lai et al., 1991) suggests that it is Carbon white dwarfs that have  $dR/dM \sim 0$  near  $M = 0.0025 M_{\odot}$  (Figure B.2). It thus seems difficult to unambiguously determine the nature of the pulsar companion, but a scenario in which PSR J1719-1438 evolved from a Carbon white dwarf in an UC LMXB has many attractive features. It explains the compact nature of the companion, the spin period of the pulsar and the longer orbital period due to spiral out as a consequence of the mass transfer that spun-up the pulsar. PSR J1719-1438 might therefore be the descendent of an UC LMXB.

However, the question still remains: why are some MSPs solitary while others retain white dwarf companions, and some, like PSR J1719–1438 have exotic companions of planetary mass that are possibly carbon rich? We suggest that the ultimate fate of the binary is determined by the mass and orbital period of the donor star at the time of mass transfer. Giants with evolved cores that feed the neutron star at a safe  $(d > \text{few } R_{\odot})$  distance leave behind white dwarfs of varying mass in circular orbits, with a tendency for the heavier white dwarfs to be accompanied by pulsars with longer pulsar spin periods (P > 10 ms). Close systems that transfer matter before a substantial core has formed might be responsible for the black-widow MSPs. A subset of the LMXBs are driven by gravitational radiation losses, and form the ultra-compact systems during a second stage of mass transfer. Their fate is determined by their white dwarf mass and chemical composition at the beginning of this phase. High mass white dwarfs do not overflow their Roche Lobes until they are very close to the neutron star with orbital periods of a few minutes. If the orbit cannot widen fast enough to stop runaway mass transfer we will be left with a solitary MSP or possibly an MSP with a disk that subsequently forms a planetary system. Low mass white dwarf donors transfer matter at longer orbital periods and naturally cease Roche Lobe overflow near the current orbital period and implied mass of the companion of PSR J1719-1438. The rarity of MSPs with planetary-mass companions means that the production of planets is the exception rather than the rule, and requires special circumstances, like some unusual combination of white dwarf mass and chemical composition.

PSR J1719–1438 demonstrates that special circumstances can conspire during binary pulsar evolution that allows neutron star stellar companions to be transformed into exotic planets unlike those likely to be found anywhere else in the Universe. The chemical composition, pressure and dimensions of the companion make it certain to be crystallized (ie diamond).

Parameter	Value				
Right Ascension (J2000) (hh:mm:ss)	17:19:10.0730(1)				
Declination (J2000) (dd:mm:ss)	-14:38:00.96(2)				
$\nu (s^-)$	172.70704459860(3) Hz				
$\dot{ u}~(\mathrm{s}^-$ )	$-2.2(2) \times 10^{-1}$				
Period Epoch (MJD)	55411.0				
$DM (pc cm^-)$	36.766(2)				
<i>P</i> (d)	0.090706293(2)				
$a \sin i$ (lt-s)	0.001819(1)				
T (MJD)	55235.51652439				
e	< 0.06				
Data Span (MJD)	55236-55586				
Weighted RMS residual ( $\mu s$ )	15				
Points in fit	343				
Mean 0.73 GHz Flux Density $(mJy)$	$0.8^{*}$				
Mean 1.4 GHz Flux Density (mJy)	0.2				
Derived parameters					
Characteristic Age (Gyr)	>12.5				
B (G)	<2×10				
Dispersion Measure Distance (kpc)	1.2(3)				
Spin-down Luminosity ${\rm L}_{\odot}$	< 0.40(4)				

\* Derived from a single observation.

**Note.** Differencing of two summed images at the expected maximum and minimum light of the companion also failed to reveal any modulation of flux from any potential candidates near the nominal pulsar position.

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179

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Figure B.1. Upper panel: Pulse timing residuals for PSR J1719-1438 as a function of orbital phase using the ephemeris in Table 1. Lower panel: Residuals after setting the semi-major axis to zero to demonstrate the effect of the binary motion. There is no significant orbital eccentricity. At superior conjunction (orbital phase 0.25) there is no evidence for solid-body eclipses or excess dispersive delays. The arrival times and ephemeris are provided in the supporting online material.



Figure B.2. The locus of the companion mass and Roche Lobe radii for PSR J1719–1438, selected ultra-compact LMXBs and black widow millisecond pulsars for different assumed orbital inclinations. The minimum companion mass and Roche Lobe radii correspond to  $i = 90^{\circ}$ and a pulsar mass of 1.4 M<sub> $\odot$ </sub>. As the unknown angle of inclination decreases, the companion mass and radius increase, becoming increasingly improbable. The bullets from lowest to highest mass represent the minimum ( $i = 90^{\circ}$ ), median( $i = 60^{\circ}$ ), 5% and 1% a priori probabilities that a randomly-oriented inclination would result in the mass and radii at least as high as that indicated. The zero-temperature mass-radius relations from Deloye & Bildsten (2003) are also shown for low-mass He and Carbon white dwarfs. The dotted line represents the mass-radius relation for low-mass Carbon white dwarfs computed by Lai et al. (1991). For reference the mass and radius of Jupiter is shown with an X.



Figure B.3. Keck/LRIS 20 minute *R*-band image centred on the location of PSR J1719-1438. The image was constructed from 5 exposures taken during the expected maximum luminosity of the companion in a total integration time of 1200s.

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