5.1 Introduction

In the last century, several large (M > 7) earthquakes have occurred on the megathrust interface along the Japan Trench, offshore of Japan's Tohoku region. Published earthquake source inversions based on seismological and high-rate GPS data suggest that the earthquakes off Miyagi [Miura et al., 2006; Umino et al., 2006], Sanriku [Tanioka et al., 1996; Nakayama and Takeo, 1997], and Tokachi [Robinson and Cheung, 2003; Hamada and Suzuki, 2004; Miyazaki et al., 2004; Satake et al., 2006] occurred repeatedly over roughly the same region of the subduction megathrust. In contrast, inversions of geodetic data from interseismic periods produce models that are locked over more spatially extensive regions [e.g., Bürgmann et al., 2005; Suwa et al., 2006; Chlieh et al., 2008b]. These broad and smooth regions are in contrast to the smaller discrete asperities indicated by earthquake source studies, and may be a consequence of lack of model resolution and a resulting need for regularization that is inherent to the use of onshore geodetic data. Alternatively, the differences may imply the potential for a large earthquake in the future. Thus, the different levels of apparent coupling implied by these two classes of models have very different implications for regional seismic hazard (Figure 1-1). Here, we explore whether post-seismic slip resulting from mechanical coupling of the inferred seismic asperities alone can reconcile this apparent difference in seismic hazard estimates. We do not seek to model the complex dynamics of rupture nucleation, interaction between asperities, or rupture propagation [see for e.g., Rice, 1993; Lapusta and Rice, 2003; Hori, 2006; Kato, 2008; Perfettini and Ampuero, 2008].
Several studies have recently attempted to constrain post-seismic creep on faults from inversions of high-rate geodetic data. These studies either tested the inferred postseismic creep for consistency with specific fault rheologies [e.g., Miyazaki et al., 2004; Hsu et al., 2006], or by modeling this inferred creep as a response of the fault to coseismic tractions, inferred its rheological properties [e.g., Johnson et al., 2005; Perfettini and Avouac, 2007]. However, the latter modeling studies were restricted to planar faults with rate-state frictional rheologies, and used ad hoc, but physically based initial conditions — for example, both studies assume that the entire fault slips at the plate convergence rate just before an earthquake. Below, we show that this assumption is not true, especially within the “stress-shadow” regions surrounding the asperities. While Perfettini and Avouac [2007] assumed that fault behavior was partitioned between an upper seismogenic zone and a lower brittle creep zone, Johnson et al. [2005] allowed coseismic and post-seismic slip to occur along the entire modeled fault surface.

Using a Boundary Element Method (BEM) model, Bürgmann et al., [2005] tested the effect of stress-shadows from “pinned” asperities on horizontal velocity predictions for the subduction zone off Kamchatka for several asperity models. They assumed that all areas outside the asperities slip freely (i.e., with zero driving shear stress, which is unphysical), resulting in a stress-shadow that is primarily located up-dip from each asperity. Since they ignore fault friction, they cannot model slip evolution around the asperities over the seismic cycle — especially down-dip of, and laterally (along strike) from, the asperity. Recently, Hetland et al. [2010] and Hetland and Simons [2010] developed an internally consistent 3D mechanical model of stress-dependent interseismic creep along the megathrust, considering both frictional and viscous fault rheologies. The stresses in this model evolve as a consequence of long-term deformation of the system (“spin-up”), and are determined by cumulative slip on the fault over this evolutionary period. Further, their model allows localized regions (“asperities”) of the fault surface to only slip coseismically at pre-assigned rupture times, thus allowing them to model the known spatio-temporal distribution of large earthquakes (similar to Bürgmann et al., [2005]). Unlike Bürgmann et al., [2005], however, slip in the regions surrounding these asperities is controlled by the specific fault rheology being assumed. They used “toy”
models to show that asperities are surrounded by a “halo” of very low creep-rates (a “stress-shadow” effect) late in the seismic cycle, which can potentially result in a relatively smooth and long wavelength surface velocity field.

As described in detail in the previous chapter, we extend this approach to an arbitrary 3D fault surface experiencing an arbitrary sequence of ruptures. We apply this extended model to northern Japan, to investigate whether this “physical” smoothing preserves any signature of the original asperities, in comparison to the artificial smoothing produced by model regularization in inversions of interseismic geodetic data. Here, we test the hypothesis that on inferred asperities along the Japan Trench megathrust, mechanical coupling alone is sufficient to explain available geodetic observations or alternatively, that these data require additional regions on the megathrust to be coupled. Underlying our analysis is the assumption that known asperities persist across multiple earthquake cycles.

In the following sections, we briefly review the forward modeling approach (see Hetland et al. [2010] for details), discuss the criteria used to determine the extent and rupture interval of each asperity chosen, present model “spin-up” and “convergence”, and finally, present results of our hypothesis test. The results presented here are meant to demonstrate the applicability of our approach for simulating realistic 3D fault surfaces. More thorough parameter-space searches are planned to be carried out in the near future to refine the analysis presented here.

5.2 Summary of the forward modeling approach

As discussed in Chapter 4, Hetland et al. [2010] cast the relationship between slip-rate and fault tractions for various rheologies in the following dimensionless form:

\[ \dot{s}^r = f(\tau^r, \alpha^r) \]  

where, \( \alpha^r \) is a strength parameter that depends on the rheology. For linear viscous rheology,
\[ s^* = f(\tau^*, \alpha') = \frac{\tau^*}{\alpha'} . \]  

(2)

Thus, late in the cycle, when most of the fault is slipping at the loading rate, the mean dimensionless shear tractions along the fault surface will equal the dimensionless strength parameter, \( \alpha' \). In Chapter 4, we estimated a typical range of values for \( \alpha' \) as 0.1 to 10.

For rate-dependent rheology,

\[ s^* = e^{-\rho} \sinh \left( \frac{\tau^*}{\rho} \right) \]  

(3)

where, \( \rho = \frac{f_0}{(a-b)} \), and \( \alpha = (a-b)\sigma_0^* \). For the results presented below, we assume a uniform \( \sigma_0^* \). Hetland and Simons [2010] demonstrated that the effect of including variable normal tractions (that is, normal tractions due to the evolving slip distribution over the fault surface) was negligible, unless the static strength of the fault is assumed to be large (cf. Figure 3 of Hetland and Simons [2010]). Even in the case where the fault is statically strong, the effect of variable tractions is significant only updip of the asperity, far from typical geodetic observations. However, they consider an effective (or reference) stress, \( \sigma_0^* \), that is much higher than the imposed coseismic traction perturbation. If \( \sigma_0^* \) is small, as is thought to be typical of most subduction zones (owing to pore-pressure effects [e.g., Kanamori, 1971; Hyndman and Wang, 1993]), then variable normal tractions will significantly influence slip-evolution over the fault surface. But their effect will be pronounced in the vicinity of the asperities and especially during the period immediately following a rupture.

From Equation 3 we can deduce that late in the cycle, when most of the fault is slipping at the loading rate, the mean dimensionless shear tractions along the fault surface will equal the product of \( \rho \) and the dimensionless strength parameter, \( \alpha' \) — that is,

\[ \tau_{ss}^* = \rho \alpha' \]  

(4)

Plate loading and frictional stresses are then in equilibrium over most of the “active” fault surface (over which slip evolves), except around the regularly rupturing asperities. This
product is nothing but \( f_0 \sigma_0^*/\tau_0 \), where the denominator is the characteristic rupture stress, \( \mu S_0/D_0 \), the mean frictional resistance over the fault surface (see Chapter 4). So, \( \alpha' \) determines the relative static strength of the fault surface relative to the induced coseismic stresses. In Chapter 4, we estimated a typical range of values for \( \rho \approx 10^{–10} – 100 \), and \( \alpha \approx 10^5 – 10^6 \) Pa. Assuming the same values as before for the non-dimensionalization of stresses, and \( \mu \approx 10^{10} \) Pa, \( \alpha' \approx 0.01 – 0.1 \). At the lower end, we have a fault that is “weak” \( (f_0 \sigma_0^* \ll \tau_0) \) compared to the imposed coseismic tractions, and the model spins up quickly. On the other hand, a fault that is “strong” in comparison to the imposed coseismic tractions results in slow spin-up of fault tractions. For \( \alpha' \approx 1 \), and the fault strength is comparable to the imposed coseismic stress pulses. For realistic values of the “damping-parameter”, \( \rho \), noted above, the effect of the first factor on the right hand side of equation (3) has only a minor influence on the evolution of post-seismic slip compared to that of the second factor. However, tractions late in the seismic cycle (i.e., when the mean fault slip-rate is close to the imposed plate velocity) are strongly dependent on both \( \rho \) and \( \alpha' \) (Equation 4, also see Figure 14 of Hetland et al. [2010]). Thus, changing these two parameters allows us to explore the effect of background stresses on slip-evolution over a spun-up seismic cycle.

In order to solve for slip evolution on the fault surface, the tractions, \( \tau' \), everywhere on the fault surface at any given time have to be related to coseismic slip, the far-field plate loading rate, and any ongoing post-seismic slip along the fault itself. This is accomplished by a discretized traction evolution equation, that can be represented in indicial notation as,

\[
\tau'_i = (s'_j - t'V'_j)K'_ji + \sum_a S'_{jia}K'_{ji}
\]  

where, \( K'_ji \) are the traction kernels (i.e., tractions at patch \( i \) due to slip on patch \( j \)), and traction (\( \tau' \)), and slip (\( s' \)) vary both in space and in time. Also, as discussed extensively in Chapter 2, in order to be kinematically consistent, we use a backslip rate distribution that is everywhere tangential to the 3D fault surface (i.e., backslip with spatially varying rake; Figure 4-6). The first term in Equation 5 accounts for ongoing fault slip and continuous far-field plate loading, while the second term is the cumulative effect of
coseismic slip (\( S' \)) on all asperities. Due to the kinematic nature of the imposed ruptures, we cannot consistently model the effect of coseismic tractions due to the rupture of one asperity on subsequent coseismic slip on an adjacent asperity. A relationship similar to Equation 5 defines surface displacement evolution. Using indicial notation,

\[
\text{\( u'_k = (s'_j - t'V')_jG'_{jk} + \sum_a S'_{ja} G'_{jk} \) (5)}
\]

where, \( G'_{jk} \) are the surface displacement kernels (or Green’s functions, i.e., displacements at observation station \( k \) due to slip on patch \( j \)).

As discussed in Chapter 4, we use the triangular dislocation solutions [as compiled in Meade, 2007] to compute K and G for a spatially discretized 3D fault in a homogeneous Poissonian half-space. The traction evolution Equation 5 is solved together with the appropriate constitutive relation (e.g., Equation 3), by marching in time using adaptive time-stepping. The time-step at any given time in such an adaptive scheme is controlled by the slip rate at that time, with larger slip rates resulting in smaller time-steps.

5.3 **Asperity parameters for the Japan Trench megathrust**

In this section, we discuss in detail the methodology used to estimate the location and extent of each inferred characteristic asperity on the Japan Trench megathrust surface, as well as its characteristic rupture interval. We are inherently assuming there is no variability between individual ruptures on each asperity (that is, the rupture sequence is both time- and slip-predictable), and therefore there is a characteristic rupture dimension, characteristic coseismic slip, and hence, a characteristic rupture interval. In determining these parameters, we try to honor, at a minimum, the latest significant (\( M_w > 7.5 \)) ruptures inferred to have occurred on these asperities during the past century. Depending on the characteristic rupture interval determined for each asperity, some of the previous ruptures may not occur exactly at the same time as historical events. However, usually, they occur within 5 years of their actual date – the effect of such small shifts in earlier ruptures was
not found to have a significant impact on surface displacement predictions, especially because of the much stronger influence of the more recent event. We proceed from the southernmost asperity of our modeling domain (Fukushima) to the northernmost (Nemuro). A summary of estimated parameters is presented in Table 5-1.

5.3.1 *Fukuyshima-oki — ruptures of 1938*

In the megathrust interface off Fukushima, three large events - $M_w 7.4$ (May, 1938), $M_w 7.7$ and $M_w 7.8$ (both in Nov 1938) — occurred in close succession. On the scale of simulating an whole seismic cycle (~ 100 yrs), the moment release from these three events can be considered “instantaneous”. So, combining the moment release from these three events (estimated from long-period surface waves [Abe, 1977]) yields a moment, $M_0$, of $1.6 \times 10^{21}$ N.m, equivalent to a moment-magnitude, $M_w$, of 8.1. Using only the locally high-slip patches, Abe [1977] estimated stress-drop, $\Delta \sigma$, to be in the range ~ 2.8–5.6 MPa. However, if we assume an equivalent single characteristic elliptical asperity (assuming for purposes of mesh-quality, an aspect-ratio, $f = (r_{\min}/r_{maj}) = 0.8$), with $\Delta \sigma_{\text{mean}} \sim 1$ MPa (10 bar), then the characteristic semi-major axis dimension can be estimated as:

$$r_{maj} = \Theta(1) \left( \frac{M_0}{\Delta \sigma} \right)^{\frac{1}{3}} \approx 1.26 \times 10^5 m = 126 km$$

resulting in a characteristic asperity area ($= \pi r_{maj} r_{min} = \pi f r_{maj}^2$) ~ $4 \times 10^4$ km$^2$. In comparison, Abe [1977] estimated the combined total area for these three events (based on first-motion data) to be ~ $1.5 \times 10^4$ km$^2$. However, the corresponding rupture interval turns out to be:

$$\Delta T_R = \left( \frac{M_0}{\mu f (r_{maj})^2 V_p} \right) \approx 16 \text{ yrs} (1)$$

because we are assuming the same characteristic slip for every rupture event on this asperity. Since there hasn’t been a $M_w > 7$ earthquake off Fukushima since 1938, we assume a recurrence interval of ~ 75 yrs for a characteristic earthquake similar to the value assumed for the Tokachi-Oki region [Yamanaka and Kikuchi, 2003]. With this assumption, the characteristic semi-major axis dimension becomes:
\[ r_{maj} = \left( \frac{M_0}{\mu \pi V_p (\Delta T_R)} \right)^{\frac{1}{2}} = 6 \times 10^4 \text{ m} = 60 \text{ km} \]  

(8)

implying a stress drop of:

\[ \Delta \sigma = \Theta(1) \left( \frac{M_0}{\mu \pi V_p (\Delta T_R)} \right)^{\frac{1}{2}} \approx 1.0 \times 10^7 \text{ Pa} = 10 \text{ MPa} , \]

(9)

which is at the upper-bound of observed seismic stress-drops [Kanamori and Anderson, 1975]. To get a feel for the sensitivity of the above estimates to the exact value of the plate velocity vector (which has been assumed to be between 8 and 9 cm/yr by different researchers), we find that:

\[ \frac{\partial r_{maj}}{\partial V_P} = - \frac{1}{2V_P} \left( \frac{M_0}{\mu \pi V_p (\Delta T_R)} \right)^{\frac{1}{2}} = - \frac{r_{maj}}{2V_P} \Rightarrow \frac{\Delta r_{maj}}{r_{maj}} = - \frac{\Delta V_P}{2V_P} \]

(10)

and,

\[ \frac{\partial r_{maj}}{\partial (\Delta \sigma)} = - \frac{1}{3(\Delta \sigma)} \left( \frac{M_0}{\Delta \sigma} \right)^{\frac{1}{2}} = - \frac{r_{maj}}{3(\Delta \sigma)} \Rightarrow \frac{\Delta r_{maj}}{r_{maj}} = - \frac{\Delta (\Delta \sigma)}{3(\Delta \sigma)} \]

(11)

so, for a ~ 10% larger \( V_P \) (9.2 cm/yr), \( r_{maj} \) will be 5% (or ~ 3 km) smaller, slip 10% (or ~ 0.6 m) larger, and stress-drop, 15% (1.5 MPa) higher.

### 5.3.2 Miyagi-oki — ruptures of 1936, 1978, and 2005

Umino et al. [2006] infer that three ruptures on this asperity that occurred in the mid 1930s — in 1933, 1936, and 1937 (with a combined moment release of \( 2.6 \times 10^{20} \text{ N.m} \), equivalent to \( M_w 7.5 \)) overlapped with the western, central and eastern portions of the \( M_w 7.5 \) 1978 rupture area, but with a moment of only a third of the latter event [Tanioka, 2003b]. The 2005 rupture also partially overlapped with the updip (southeastern) portion of the 1978 rupture area [Miura et al., 2006]. We assume the 1978 \( M_w 7.4-7.5 \) event as the characteristic earthquake for this region (\( M_0 = 1.7-3 \times 10^{20} \text{ N.m} \) estimated from tsunami data [Tanioka, 2003b], and long-period surface waves [Seno et al., 1980]). The stress drop, \( \Delta \sigma \), based on localized high-slip patches was estimated to be 10 - 15 MPa.

As before, assuming a characteristic elliptical asperity having a mean stress drop, \( \Delta \sigma_{mean} \sim 1 \text{ MPa} \), the semi-major asperity dimension is:
resulting in a recurrence interval for the characteristic earthquake
\[ \Delta T_R = \left( \frac{M_0}{\mu f (r_{maj})^2 v_p} \right) \approx 9 \text{ yrs (I)} \] (13)

Since the next major event after the 1933–37 sequence did not occur until the 1978 event, we estimate a semi-major asperity dimension, instead, assuming a rupture interval of ~40 years (the 2005 event may be consistent with the 1933–37 sequence in that it ruptured only one part of the characteristic asperity, and subsequent events may follow to rupture the rest of the characteristic asperity) to be
\[ r_{maj} = \Theta(1) \left( \frac{M_0}{\mu f (r_{maj})^2 v_p} \right)^{1/2} \approx 3.5 \times 10^4 m = 35 \text{ km} \] (14)
implying a mean stress drop
\[ \Delta \sigma = \Theta(1) \left( \frac{M_0}{f (r_{maj})^2 v_p} \right) \approx 9 \times 10^6 \text{ Pa} = 9 \text{ MPa} , \] (15)
which is, again, near the upper-bound of observed seismic stress-drops [Kanamori and Anderson, 1975]. Another way to estimate the characteristic asperity dimension in this case is by assuming that the mean stress-drops and asperity shapes in the 2005 and 1978 events are similar. In this case, an estimate can be made of the 1978 (characteristic) asperity size relative to the well-determined asperity size for the 2005 Mw7.2 event (\(M_0 = 1.7-7 \times 10^{19} \text{ N.m estimated from GPS and seismic data [Miura et al., 2006]}\)):
\[ \Delta \sigma_{1978} = \Delta \sigma_{2005} = \Theta(1) \left( \frac{M_0}{f (r_{maj,1978})^2 v_p} \right) = \Theta(1) \left( \frac{M_0}{f (r_{maj,2005})^2 v_p} \right) \]
\[ \Rightarrow r_{maj,1978} = r_{maj,2005} \left( \frac{M_0}{M_0} \right)^{1/2} \approx 35 \text{ km} \] (16)

which agrees almost exactly with that from the assumed recurrence interval.

5.3.3 **Sanriku-oki — ruptures of 1931, 1968, and 1994**

The 1994 Mw7.8 event off Sanriku (\(M_0 = 3-4 \times 10^{20} \text{ N.m}\)) [Nishimura et al., 1996; Tanioka et al., 1996; Nakayama and Takeo, 1997] coincided with the shallow portion of the 1968
5-10

$M_w 8.2$ event (based on source inversion for the former event using strong-motion
[Nakayama and Takeo, 1997], and broad-band [Nishimura et al., 1996] data; and for the
1968 event, using P-wave first motions as well as long-period surface waves [Kanamori,
1971]). We consider only the 1994 even rupture area as the characteristic asperity
because the deeper part of the 1968 event may not even be on the subduction megathrust
(based on focal mechanisms — Hiroo Kanamori, personal communication). Again, if we
assume a characteristic elliptical asperity having a mean stress drop, $\Delta \sigma_{mean} \sim 1$ MPa, the
maximum semi-major asperity dimension is

$$ r_{maj} = \Theta(1) \left( \frac{M_w}{\Delta \sigma} \right)^{1/2} = 8 \times 10^4 m = 80 \text{ km} $$

with an estimated recurrence interval for the characteristic earthquake as,

$$ \Delta T_R = \frac{M_w}{\mu \pi (r_{maj}) \sqrt{V_p}} \approx 12 \text{ yrs (!) } $$

Again, since the next “major” rupture after the 1968 one was not until 1994, we instead
estimate a semi-major asperity dimension assuming a rupture interval of $\sim 30$ years
(approximate mean value of rupture intervals between 1931, 1968, and 1994 events):

$$ r_{maj} = \left( \frac{M_w}{\mu \pi (r_{maj}) \sqrt{V_p}} \right)^{1/2} \approx 4.5 \times 10^4 m = 45 \text{ km} $$

implying a mean stress drop of

$$ \Delta \sigma = \Theta(1) \left( \frac{M_w}{\mu \pi (r_{maj}) \sqrt{V_p}} \right) \approx 5 \times 10^6 \text{ Pa} = 5 \text{ MPa} , $$

in the middle of the range of observed seismic stress-drops [Kanamori and Anderson,
1975].

5.3.4 Tokachi-oki — ruptures of 1952 and 2003

The 2003 rupture off Tokachi was determined to be either slightly smaller than the 1952
event ($M_w 8.0$, from tsunami waveform modeling [Satake et al., 2006], and re-estimation
of 1952 aftershock pattern [Hamada and Suzuki, 2004]), or roughly equal in size to
the 1952 rupture ($M_w 8.2$, from broad-band SH & long-period mantle phases [Robinson
and Cheung, 2003], as well as joint inversion using strong-motion and GPS [Koketsu et
With nearly coincident rupture areas, using the better constrained and more recent estimates, the characteristic moment release, $M_0$, for Tokachi-Oki is $\sim 2 \times 10^{21}$ N.m. Robinson and Cheung [2003] estimated stress drop, $\Delta \sigma$, between 10–25 MPa, using localized high-slip regions, but a mean stress-drop, $\Delta \sigma_{\text{mean}} \sim 0.5$ MPa. They also estimated the mean slip to be $\sim 2.2$ m. If we assume that the 1952 and 2003 events ruptured the same characteristic elliptical asperity having a mean stress drop, $\Delta \sigma_{\text{mean}} = 1$ MPa (10 bar), then the semi-major asperity dimension is

$$ r_{maj} = \Theta(1) \left( \frac{M_0}{\Delta \sigma} \right)^{\frac{1}{3}} \approx 1.4 \times 10^5 \text{ m} = 140 \text{ km} $$

resulting in a characteristic earthquake recurrence interval of

$$ \Delta T_R = \left( \frac{M_0}{\mu f(r_{maj})^2 V_P} \right) = \left( \frac{2 \times 10^{21}}{(3 \times 10^{10})(0.8)(8.3 \times 10^{-2})(50)} \right) \approx 17 \text{ yrs} $$

Therefore, we assume that the 2003 event is the characteristic repeat event of the 1952 event, for a rupture interval of $\sim 50$ years, implying a characteristic semi-major asperity dimension

$$ \frac{r_{maj}}{r_{maj,2003}} = \left( \frac{M_0}{\mu f(r_{maj,2003})^2 V_P} \right) \approx 8 \times 10^4 \text{ m} = 80 \text{ km} $$

resulting in a mean stress drop of

$$ \Delta \sigma = \Theta(1) \left( \frac{M_0}{\mu f(r_{maj})^2 V_P} \right) \approx 5 \times 10^6 \text{ Pa} = 5 \text{ MPa} $$

which is within the observed range of seismic stress-drops [Kanamori and Anderson, 1975]. Again, as with the Miyagi-oki asperity, if we assume that the mean stress-drops and asperity shapes in the 2003 and 1952 events are similar, then the last equation can be used to compute yet another estimate of the characteristic semi-major asperity dimension relative to the well determined coseismic asperity for the 2003 event:

$$ \Delta \sigma_{1952} = \Delta \sigma_{2003} = \Theta(1) \left( \frac{M_0}{\mu f(r_{maj,1952})^2 V_P} \right) = \Theta(1) \left( \frac{M_0}{\mu f(r_{maj,2003})^2 V_P} \right) $$

$$ \Rightarrow r_{maj,1952} = r_{maj,2003} \left( \frac{M_0}{M_0} \right)^{\frac{1}{3}} \approx 75 \text{ km} $$

which agrees well with that estimated from the assumed recurrence interval. The along-strike dimension of the asperity, $D (=2 \times r_{maj})$, of $\sim 150$ km, also agrees well with the width between two subduction zone geologic features that seem to bound this rupture
area: Kushiro canyon to the east, and the plate bend with deepening of continental shelf to the west [Hamada and Suzuki, 2004].

5.3.5 Nemuro-oki — rupture of 1973

Great earthquakes occurred off Nemuro in 1894 and 1973, but the latter event is estimated to have been much smaller than the 1894 event. It is conjectured that the 1894 event ruptured the source areas of both the 1973 Nemuro-oki and 1952 Tokachi-oki events [Tanioka, 2003a]. The 1973 event has been estimated to be between $M_w 7.8$ [Tanioka, 2003a] (from tsunami waveforms, with $M_o \sim 5 \times 10^{20}$ N.m), and $M_w 7.9$ [Shimazaki, 1974] ($M_o \sim 6.7 \times 10^{20}$ N.m). We adopt the more recent estimate from Tanioka [2003a], who estimated mean fault slip to be $\sim 2$ m. In contrast, Shimazaki [1974] estimated a slip of 1.6 m, and mean stress drop of 35 bars (3.5 MPa). As before, assuming a characteristic elliptical asperity having a mean stress drop, $\Delta \sigma_{mean} \sim 1$ MPa, the semi-major asperity dimension is

$$r_{maj} = \Theta(1) \left( \frac{M_o}{\mu \Delta \sigma} \right)^{1/2} \approx 8.5 \times 10^4 m = 85 \text{ km}$$

(26)

implying a recurrence interval for the characteristic earthquake of,

$$\Delta T_R = \frac{M_o}{\mu \Delta \sigma (r_{maj})^3 V_p} \approx 11 \text{ yrs (I)}$$

(27)

So, we instead assume a recurrence interval of $\sim 75$ yrs for a characteristic earthquake as in the Tokachi-Oki region [Yamanaka and Kikuchi, 2003] (which is not unreasonable, given that the 1894 event must have completely ruptured the 1973 asperity), obtaining a semi-major asperity dimension of

$$r_{maj} = \left( \frac{M_o}{\mu \Delta \sigma (r_{maj})} \right)^{1/2} \approx 3 \times 10^4 m = 30 \text{ km}$$

(28)

implying a mean stress drop of

$$\Delta \sigma = \Theta(1) \left( \frac{M_o}{\mu \Delta \sigma (r_{maj})} \right)^{1/2} \approx 2 \times 10^7 Pa \approx 20 \text{ MPa} ,$$

(29)

which is beyond the upper bound for the range of observed seismic stress-drops [Kanamori and Anderson, 1975]. However, given there hasn’t been a rupture off Nemuro
since 1973, if we assume a characteristic rupture interval of ~ 40 years (similar to the
Miyagi-oki region adjacent to the Fukushima asperity), we obtain a semi-major asperity
dimension of

\[
    r_{maj} = \left( \frac{M_o}{\mu f \Delta T_R} \right)^{\frac{1}{2}} = 4.5 \times 10^4 \text{ m} = 45 \text{ km}
\]

This latter estimate of \( r_{maj} \) implies a mean stress drop of:

\[
    \Delta \sigma = \Theta(1) \left( \frac{M_o}{f (r_{maj})} \right) \approx 7 \times 10^6 \text{ Pa} = 7 \text{ MPa},
\]

which is within the range of observed seismic stress-drops [Kanamori and Anderson,
1975].

5.3.6 Summary

A summary of the final asperity parameters chosen for the northern Japan megathrust is
presented in Table 5-1, and the resulting asperity configuration is illustrated in Figure
5-1.

Table 5-1. Summary of asperity parameters for Northern Japan. The last column represents the
time from the present (here, the year 2000, which marks the end of the time-period over which
the observed GPS velocities were computed in Hashimoto et al. [2009]) to the most recent
earthquake for each asperity.

<table>
<thead>
<tr>
<th>Region</th>
<th>( D ) (km)</th>
<th>( f = r_{min}/r_{max} ) (non-dim)</th>
<th>( s_0^* ) (m)</th>
<th>( \Delta T_R' ) (yr)</th>
<th>( \Delta \sigma_{\text{mean}}^{2,3} ) (MPa)</th>
<th>( T_R ) [yrs(date)]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fukushima-oki</td>
<td>120</td>
<td>0.8</td>
<td>6.4</td>
<td>75</td>
<td>10</td>
<td>62 (1938)</td>
</tr>
<tr>
<td>Miyagi-oki</td>
<td>70</td>
<td>0.8</td>
<td>3.3</td>
<td>40</td>
<td>9</td>
<td>22 (1978)</td>
</tr>
<tr>
<td>Sanriku-oki</td>
<td>90</td>
<td>0.8</td>
<td>2.5</td>
<td>30</td>
<td>5</td>
<td>6 (1994)</td>
</tr>
<tr>
<td>Tokachi-oki</td>
<td>160</td>
<td>0.8</td>
<td>4.2</td>
<td>50</td>
<td>5</td>
<td>48 (1952)</td>
</tr>
<tr>
<td>Nemuro-oki</td>
<td>90</td>
<td>0.8</td>
<td>3.3</td>
<td>40</td>
<td>7</td>
<td>27 (1973)</td>
</tr>
</tbody>
</table>

\( V_p = 8.3 \times 10^{-2} \text{ m/yr}; \)
\( \Delta T_R \propto (1/A) \approx (1/r^2) \)
\( \Delta \sigma \approx s_0 = V_p \times \Delta T_R \)
\( \Delta \sigma \approx (1/AD) \approx (1/r^3), \ and, \ \Delta \sigma \approx (\Delta T_R)^{1.5} \)
Figure 5-1. Asperity configuration chosen for the northern Japan megathrust interface, and the epicentral locations of the last earthquake(s) prior to the year 2000 (blue stars, multiple around an asperity start indicate two ruptures within the same year).

5.4 Simulating rupture-sequences for the northern Japan asperity configuration

In section 4.7, we briefly mentioned the hierarchy of basic, but general benchmark tests done to test the physicality of our simulations. Here, we discuss the issue of numerical convergence specifically for the Japanese megathrust problem, and then explore the analysis of model spin-up for the full five-asperity problem. The first tests with any model were carried out with a linear viscous fault rheology (even if it may not be a realistic rheology for modeling slip evolution on fault surfaces). Since the strain-rate and stress are linearly dependent, this rheology is more straightforward for testing model behavior (benchmarking, convergence, spin-up), and for developing some intuition about
the interaction between asperities and their relationship to the predicted surface velocity field.

5.4.1 Model Convergence for the Japan megathrust interface

An important issue for determining the accuracy of model predictions is whether the coseismic signal is accurately resolved by a given mesh resolution. From the meshing convention described in Chapter 4, a higher resolution mesh has essentially the same number of elements as the coarse mesh outside the asperity transition zone, but may have significantly more elements within this transition zone. The goal of such refinement was to better resolve the coseismic tractions that drive fault slip, which ultimately determines the predicted surface velocities. However, increasing the mesh resolution beyond a certain point does not significantly improve the spun-up fault tractions.

Exact convergence tests for the full five-asperity problem (JT5, of Section 4.7) will be carried out in the near future. Such tests are time-consuming, especially for the JT5 problem with frictional rheologies. During the hierarchical tests mentioned in Section 4.7, we found that even though frictional faults were spun-up in fewer rupture-cycles than linear viscous faults, each cycle had a lot more time-steps owing to the exponential dependence of strain-rates on imposed coseismic stresses. However, such tests are worth the “cost” because they allow us to test whether further mesh resolution improvement (which could be still more expensive computationally) is necessary.

Here, we present the results from such test for the two-asperity case (JT2, of Section 4.7, containing only the Miyagi & Sanriku asperities). Since the strategy used in both cases is identical, as long as the kernels are computed from nearly identical sources around two common asperities in both models (i.e., having roughly the same element size, or resolution, in the transition zone), it is reasonable to qualitatively extrapolate convergence of spun-up solutions for the JT2 mesh to the JT5 mesh. Such extrapolation through intuition can be helpful in figuring out whether the time spent generating the
mesh, computing kernels, and subsequent iterations for smoothing (discussed in Chapter 4) would be worth it.

Figure 5-2 shows the spun-up tractions for a benchmark linear-viscous run for three different transition zone mesh resolutions for JT2. The number of elements in the asperity transition zone increases threefold between “RES1” (blue) and “RES2” (red) runs, but the spun-up solution appears to have “converged”, because no significant improvement is seen for the added cost of a high-resolution mesh – especially late in each rupture cycle (i.e., just before each rupture). So, compared to the lowest resolution JT5 mesh, the next level (“RES1”, with nearly 6000 fault patches) can be expected to improve our solution, but the next higher resolution (“RES2”, with nearly 9700 fault patches) may not be worth its significantly larger computational time relative to the improvement in the solution. But it is perhaps good practice to compute the “RES2” solution for one case, and if significant improvement is not seen, then ignore this resolution for the rest of the suite of runs. Further, the surface displacement field is much smoother (i.e., of longer wavelength) than the stress-perturbation on the fault surface, and therefore affected much less by the small improvement in tractions from “RES1” to “RES2”.
5.4.2 Model spin-up using a synthetic rupture catalog

In order to simulate the multi-asperity problem, we need to start with a realistic catalog of ruptures for spin-up. To build the catalog, we first set the end-time for each asperity’s rupture sequence as the time of the most recent rupture on that asperity. We then compute a series of “past” ruptures for each asperity, going backward in time for a sufficiently large number of ruptures. We thus build a synthetic rupture “catalog” that includes all past rupture times for each asperity. We reset the simulation start time to the beginning of the oldest complete characteristic rupture sequence - a sequence consisting of ruptures on all five asperities, in the order of their most recent ruptures - in this catalog. Irrespective of the starting time-shifts, $T_R$ (Table 5-1), as long as the
characteristic rupture interval, $\Delta T_R$ for each asperity is fixed, the order of asperity ruptures will be identical after a time, $T_{CRS}$, arithmetically equal to the least common multiple of all asperity rupture intervals, $\Delta T_R$. For the rupture intervals estimated here (Table 5-1), $T_{CRS}$ is 600 years. If one of the rupture intervals were off by even one year, $T_{CRS}$ would be much longer. Here, to avoid unnecessarily extending simulation time, we rounded rupture intervals to the nearest 5 years. So, $T_{CRS}$ is very sensitive to the actual rupture intervals chosen, which depend not only on the exact asperity size, but also on the mesh resolution used. Therefore, $T_{CRS}$ does not have any physical meaning. But as shown below, it is a convenient measure for following the evolution of model tractions, once a set of rupture-intervals are chosen for a given asperity configuration, and mesh resolution.

We start each model with zero initial tractions. Although the existing Matlab forward model EvolveSlip, has the option to prescribe a pre-stress, for the initial runs at least, we do not specify a pre-stress. Tractions induced on the fault surface by repeated asperity ruptures as well as continuous far-field loading by the semi-infinite extensions of the fault (equivalent to backslip) eventually reach an equilibrium value determined by the fault rheology. The time taken to reach equilibrium depends on the dynamic “strength” of the fault, as discussed in Section 5.2. For a given rheology, this steady state traction is that which is required to maintain the relative motion between the hanging- and foot-walls at the loading rate, $V_0$. We call this evolution of fault tractions from their initial value to a final steady state, the “spin-up” of fault tractions. Once steady state is attained, the mean value of fault tractions as well as that of the surface displacement field do not change over a time scale equal to that for the characteristic rupture sequence, $T_{CRS}$.

Since $T_{CRS}$ does not have a physical basis and can be a very large number, a practical choice for the reference time-scale, $T_0$, over which to compute the evolution of mean tractions is the largest rupture interval of all asperities (75 years, here). Because of ongoing slip associated with ruptures, the mean tractions over the fault surface fluctuate significantly over a single cycle (Figure 5-3). So, we take moving averages of the mean traction vector over time-windows that are multiples of this reference time, $n.T_0$ (with $n$=
1, 2, …). As this averaging time-window gets larger, the moving average of mean tractions gets smoother, and it becomes easier to measure model spin-up. From Figure 5-3, the smallest window for which the spun-up tractions are stable corresponds to the $T_{CRS}$ (or, cycle = $T_{CRS} / T_0 = 600/75=8$). This is not a surprising result, since $T_{CRS}$ is an inherent numerical feature of the set of rupture intervals chosen for the simulation. So, in order to measure spin-up, a simulation must be run for the duration of at least $T_{CRS}$. The minimum spin-up time estimated for a low-resolution run can be used to significantly reduce computation time for higher resolution runs.

**Figure 5-3.** Spin-up of mean fault tractions, and their moving averages for a linear viscous fault rheology with $\alpha=0.1$. The gray curve represents the mean tractions at every time-step. The light blue curve at the bottom represents a single pick of the grey curve at the end of each cycle of duration equal to the reference time, $T_0$. The moving average window, $T_{mav}=8$ (dark blue) corresponds to $T_{CRS}$. See text for details.

Once the model is spun up, the cumulative slip on the fault surface over the duration of the reference cycle, $T_0$ (right panels of Figure 5-4), must look identical to the applied variable-rake backslip on the fault surface (Figure 4-6), except for the asperities
themselves, which are in different stages of their cycle. All asperities catch up with the rest of the fault only at the end of a $T_{CRS}$-cycle. At the end of a $T_{CRS}$-cycle, there should be no difference (except for a scaling factor equal to $T_{CRS}$) between cumulative slip and applied backslip. The use of VTK for visualization allows on the fly spin-up checks such as these to be performed routinely. The dip-slip (top row of Figure 5-4) and strike-slip (-slip (bottom row of Figure 5-4) components are visualized separately in order to make sure that any slip-partitioning is being correctly applied. In the left panels of Figure 5-4 displaying slip-rates, the regions of nearly zero-rates surrounding the asperities are the “stress-shadow” zones, which travel passively with the downgoing plate, but are no-longer stressed (until the subsequent rupture). The surface velocities on the other hand depend only on the amount of the fault surface that is (nearly) not slipping. Therefore, the larger these stress-shadow zones, the larger, the “apparent locked zone”, and larger the corresponding surface velocities. We would expect dynamically weak rheologies to be able to propagate slip farther over each cycle, thereby producing larger apparently “locked” zones, and thus, larger surface velocities late in the cycle.

Once a model is spun up, the reference cycle of duration $T_0$ immediately following the last complete $T_{CRS}$-cycle contains the “most recent” characteristic rupture sequence (here, the 75 years starting from the oldest rupture in the sequence: Fukushima in 1938). The surface displacement field is extracted over the duration of this most recent rupture sequence, and synthetic surface velocities are estimated over the same time-window as that for the observed GPS velocities.
Figure 5-4. Plot of slip-rate (left column) and cumulative fault slip (right-column) at the end of the first reference cycle ($T_0$), post model spin-up, for the linear viscous rheology used in Figure 5-3. Top rows show the strike-slip component, bottom rows show the dip-slip component. As expected, the right column looks nearly identical to the input backslip velocities (Figure 4-6), except for the asperities themselves, which will match the surrounding fault only at the end of the $T_{CRS}$-cycle. See text for details.

5.5 Station velocity predictions for northern Japan using a realistic fault rheology

In this section, we demonstrate the methodology discussed in the past couple of chapters by using it to predict synthetic station velocities using realistic rate strengthening frictional rheology parameters inferred for the northern Japan megathrust interface. Several recent studies inverted post-seismic surface displacements to infer rate-dependent
or rate-state friction parameters for faults in California and Japan [e.g., Johnson et al., 2005; Perfettini and Avouac, 2007; Fukuda et al., 2009]. These studies have inferred that faults seem to be dynamically weak (i.e., low values for the strength parameter, \( \alpha = (a-b)\sigma_0^* \), of 0.1 to 0.5 MPa). So, for our demonstration run, we pick \( \alpha \approx 0.1 \) MPa, and \( \rho \approx 10 \), which yields a dimensionless strength parameter, \( \alpha' \approx 1 \) (see section 5.2). Model tractions are mostly spun-up in just over three \( T_{CRS} \) cycles (or 25 reference cycles, Figure 5-5). Note that equilibrium dimensionless stress is ten times larger than for the linear-viscous benchmark presented above (Figure 5-3), while the stress pulses induced by ruptures remains the same as in that case. Therefore, it is hard to see the individual ruptures at the scale of the full convergence test. While the expected steady state tractions are 1.0, the model apparently spins up to a value about 20% higher, which implies that frictional stresses are larger than that expected for the imposed coseismic stresses. The reason for a higher value has to do with which asperity was chosen for the reference asperity dimension, \( D_0 \). This reference dimension not only controls the non-dimensionalization of the mesh (so, larger \( D_0 \) implies a smaller non-dimensional mesh domain), but also that of tractions (since \( \tau_0 = \mu S_0/D_0 \)). The dimensionless result presented in Section 5-2 assumes a single characteristic asperity dimension, whereas here we have multiple asperities having a range of sizes.

For the simulation shown below, we picked a single asperity (Fukushima, which is also the second biggest; Figure 5-1) to be the reference for both rupture interval as well as asperity dimension, to be consistent. However, had we chosen the mean asperity size, then \( \tau_0 \) would be larger (that is, larger non-dimensional induced stress field), and hence, smaller value of the mean steady state tractions, \( \tau_{\text{mean}} \). In fact a taking the ratio of these two sizes (\( R_{\text{Fukushima}}/R_{\text{mean}} \approx 1.2 \)), is roughly equal to the observed discrepancy. The resulting stress pulses (Figure 5-6), would be steeper, and hence decay slightly faster, resulting in slightly smaller surface velocity predictions late in the cycle. So, when multiple asperities are present, choosing a single characteristic asperity may be a challenge, especially when the largest asperity may not necessarily rupture with the largest rupture interval, as is the case here.
Figure 5-5. Spin-up tractions for northern Japan megathrust, for a rate-strengthening frictional rheology, with $\rho \approx 10$, and $\alpha \approx 10^5$ Pa ($\alpha' \approx 1$)

The stress change over the 75-year reference cycle right after the third $T_{CRS}$ cycle — simulating the past 75 years of asperity ruptures — shows the rapid evolution of stress early in the cycle, that is characteristic of frictional rheologies (Figure 5-6). Only the most recent events that occurred prior to the observed GPS velocity estimation window (1996–2000) are labeled for each asperity. The unlabeled stress spike in the middle of that figure is equivalent to the shallow portion of the 1968 Sanriku-oki event, while the last stress spike is equivalent to the 2003 Tokachi-oki event. It is worth noting that the modeled Sanriku-oki event is roughly four years early, because of our assumption regarding the mean rupture interval time. However, our simulations indicate that the 1968 Sanriku-oki event is far enough removed from the GPS velocity window that this slight rupture time-shift may not have a significant impact on velocity predictions, given the same asperity experienced the most recent of these large earthquakes.
Figure 5-6. Evolution of tractions over the “present” reference cycle of 75 yrs. Only the most recent events prior to the end-date of GPS velocity measurements (2000) are identified for each asperity. The two unlabeled events correspond to the 1968 “Tokachi-Oki” event off the Sanriku coast (but occurring in 1964 due to the approximate rupture interval chosen in Section 5.3), and the 2003 M8.2 Tokachi-oki 2003 event (here, occurring in 2002).

In order to check how realistic our input coseismic ruptures are, we compare the synthetic coseismic surface displacements due to characteristic slip on the modeled Tokachi-oki asperity to some recent joint geodetic/seismic inversions of the 2003 Tokachi-oki earthquake [Koketsu et al., 2004]. The overall pattern of surface displacements along southeastern Hokkaido seems to agree well with the observed coseismic surface displacement field (Figure 5-7). The synthetic displacements are scaled relative to the coseismic slip imposed (~6.4 m, see Table 5-1). The maximum scaled synthetic displacements are of the order of 0.07, or 45 cm. In comparison, the peak observed coseismic displacements were roughly 70–80 cm. It is possible that by spreading slip over the entire asperity, we are not able to produce the locally high slip regions (upto 8
m), that were inferred. However, because we impose a characteristic rupture for Tohoku having a significant strike-slip component, our model predicts excessive strike-slip surface coseismic displacements northeast of the Tohoku asperity. This is not seen in Figure 5-7(b), because the 2003 Tokachi-oki rupture was inferred to be predominantly in the dip-slip direction. This discrepancy highlights a limitation of our approach: in reality, the character of coseismic slip changes from rupture to rupture, and is not identical from rupture to rupture. The significant strike-slip partitioning due to the bend in the trench profile between the Sanriku and Tokachi asperities has to be absorbed some other way over the geologic time-scale. One way would be to periodically introduce a purely strike-slip rupture on the Tokachi asperity. However, a more plausible explanation might be that a significant portion of this strike-slip motion is absorbed by the strike-slip fault forming the western boundary of the Kurile sliver plate, which extends almost half way down the eastern Hokkaido coast [e.g., Figure 6 of DeMets, 1992].

Figure 5-7. (a) Synthetic Tokachi-oki coseismic displacements and (b) actual coseismic displacements from 2003 $M_w$ 8.2 Tokachi-oki earthquake [Koketsu et al., 2004]. The synthetic displacements are scaled relative to the imposed mean coseismic slip of 6.4 m (Table 5-1).

Sample surface displacements over the last reference cycle also show a rapid post-seismic response for the rheological parameters chosen here (Figure 5-8). It is interesting to note
that both stations displayed here (located along the Sanriku coast) show a different sense of offset in their north (y) component (middle panels of Figure 5-8) for the 1952 Tokachi-oki event and the subsequent 1968 Sanriku-oki event. In our synthetic predictions, this is due to the fact that the applied variable-rake backslip is partitioned into a small northward component (as opposed to being southward over the rest of the fault surface), over a small region around the Sanriku asperity (Figure 4-6), because of the change in orientation of the trench profile relative to the mean plate convergence direction. Such a reversal is also seen between the 1994 Sanriku-oki and 2003 Tokachi-oki events for this station. It will be interesting to check whether this latter reversal is indeed observed in the time-series for this station. A dynamically weaker frictional rheology (smaller $\alpha'$) could result in a more pronounced post-seismic response than that displayed in Figure 5-8.

**Figure 5-8.** Sample synthetic surface displacement time-series over the last 75 yr reference cycle for two stations (left: 960533; right: 950156; both located along the Sanriku coast). Blue dashed lines indicate the observed and synthetic GPS velocity estimation window, and the slopes used to infer the velocities are indicated as grey lines within this window.
Finally, we present comparisons between the GPS velocities estimated for the period 1996–2000 [Hashimoto et al., 2009], and the synthetic velocities assuming both a frictionless fault, as well as the rate strengthening rheology discussed above. The observed velocities are relative to the station Adogawa (Geonet #950320), located along the Japan Sea coast, just off the lower left corners of Figure 5-9 and Figure 5-10. In contrast, our model predictions are relative to the far-field of the overriding plate (i.e., Eurasia). Also, we do not model the incipient subduction thought to be occurring along the Japan Sea coast. Therefore, our “raw” model predictions near the Japan Sea coastline are opposite to the above relative velocities. Given that the above reference station is outside the area we can model with motion purely along the Japan Trench megathrust, we pick as the reference station, Geonet #950241, which is northeast of Adogawa along the Japan Sea coast. We confirmed that the observed GPS velocities at this station were negligible. All synthetic velocities presented below are relative to this station. All velocities are scaled relative to the plate velocity of 8.3 cm/yr for the Pacific Plate off Tohoku.

We first compare the predicted horizontal velocity field computed assuming that only the asperities are locked late in the cycle, and the surrounding fault slips aseismically, at the long-term slip-rate equal to the plate velocity (Figure 5-9). This scenario is equivalent to applying backslip over all of the asperities to estimate interseismic velocities. Clearly, this model explains only a small fraction of the observed horizontal field. From a purely backslip perspective, areas between the asperities are also required to be “locked”, or “coupled”, to explain the observed GPS velocities. Alternatively, significant post-seismic slip in the region between the three southernmost asperities, as well as between the two northernmost ones, could also explain the misfit.

We now compare the predicted velocity fields for the frictional rheology assumed above (Figure 5-10). The most interesting observation is that much of the horizontal velocity field in the vicinity of the two largest asperities (Fukushima in the south, and Tokachi in the north) is explained by the extensive post-seismic slip (Figure 5-11) around them after their most recent ruptures. In fact, by including variable-rake backslip, we fit the
Figure 5-9. Observed (left), synthetic-backslip (middle), and residual (right) horizontal GPS velocity fields (relative to a fixed Okhotsk plate) for the period 1996-2000. Synthetics were computed assuming that the fault is locked only at the asperities late in the cycle, and the rest of the fault surface is frictionless. Asperities are shaded in light gray and off-shore of the northern Japan coastline. Thick black arrows indicate the plate convergence direction. Velocities are scaled relative to the plate velocity of 8.3 cm/yr for the Pacific Plate off Tohoku. The color intensity has the same scale in each plot.

Figure 5-10. Observed (left), synthetic-frictional (middle), and residual (right) horizontal GPS velocity fields (relative to a fixed Okhotsk plate) for the period 1996-2000. Synthetics were computed assuming that slip on the fault surface is governed by rate strengthening friction with $\alpha' \approx 1$. Asperities are shaded in light gray and off-shore of the northern Japan coastline. Thick black arrows indicate the plate convergence direction. Velocities are scaled relative to the plate velocity of 8.3 cm/yr for the Pacific Plate off Tohoku. The color intensity has the same scale in each plot.
Figure 5-11. Slip-rates at the end of the cycle, for a fault surface governed by rate strengthening friction with $\alpha' \approx 1$. Notice the much larger areas of near-zero slip-rates compared to the upper-left panel of Figure 5-4.

Horizontals much better in southern Hokkaido, compared to recently published horizontal velocity predictions based on a sophisticated inversion scheme that probably did not include this effect [e.g., Supplementary Figure 1, Hashimoto et al., 2009]. However, around both these asperities, a dynamically weaker fault (smaller $\alpha'$) would lead to higher velocities, and perhaps a lower misfit (similar to our conclusion from surface displacement plots above).

However, there are several regions of significant misfits: (a) northeastern Hokkaido, along the Nemuro coastline, (b) along the Japan sea coast of southern Hokkaido, (c) along the eastern coastline of central Tohoku between the Miyagi and Sanriku asperities, and (d) along the Kanto-southern-Tohoku region in central Japan. We now examine each of these regions more closely.

(a) The biggest residuals are in northeastern Hokkaido, along the Nemuro coastline. There are a couple of plausible explanations for this discrepancy. The first has to do with the fact that we have ignored the large 1994 M8.1 Shikotan island earthquake, and perhaps this asperity needs to be included in our simulation to account for the discrepancy. The second has to do with the fact that the original slab geometry created in Gocad has a long-wavelength concave dip starting just downdip of Nemuro asperity. As
a result, there is considerably less downdip component in the variable rake backslip field we impose (blue area in the right column of Figure 4-6). This was confirmed by noting that in the synthetic surface displacement field just prior to the 1973 Nemuro-oki event, there is a significant trench-parallel, but almost no downdip, component (as would be expected late in the cycle, landward of a locked patch). So, correcting this long-wavelength feature (which was missed by the kernel residual checks discussed in Chapter 4) might also help better model the horizontals in this region.

(b) The misfit in southwestern Hokkaido could most likely be from ongoing post-seismic deformation after the 1993 Mw 7.8 Hokkaido-Nansei-oki earthquake in Japan Sea [Ueda et al., 2003]. The maximum residuals we obtain for this region are of the order of 0.2 of the plate velocity, or ~ 1.7 cm/yr. In comparison, the best-fit post-seismic relaxation models of Ueda et al. [2003] yield horizontal surface velocities of 1.5 and 2 cm/yr. While there is good agreement between our residuals and their predicted horizontals, we observe a significant counter-clockwise rotation due to the excess strike-slip component in the characteristic rupture imposed on the Tokachi asperity as well as the anomalous strike-slip contribution to the Nemuro asperity (above).

(c) The main characteristic of the misfits in central Tohoku are their trench-perpendicular orientations. This indicates either (i) that a yet to be detected asperity exists between the Miyagi and Sanriku asperities [e.g., Slip deficit region in Fig 6 of Miura et al., 2006], or (ii) this region may be susceptible to episodic aseismic afterslip [Igarashi et al., 2003; Uchida et al., 2004], or (iii) a region that could become “locked” owing to coseismic Coulomb stress changes as observed by Miura et al. [2006]. Although many cases of small but repeating earthquake clusters have also been documented in this region [Igarashi et al., 2003; Uchida et al., 2004], the frequent release of any accumulated strain would not result in an apparent slip-deficit along the megathrust interface here, ruling out the first possibility. Yet another possibility is that the location of the Miyagi asperity centroid may be too deep. The Japanese coastline in this region is located right above a steep change in slab dip, and locating the asperity even a little too landward would also make it deeper, reducing its contribution to the horizontal velocity field.
(d) Recently, Townsend and Zoback [2006] argued for additional permanent horizontal deformation in central Japan — beyond that inferred from deformation due to cyclic subduction zone megathrust ruptures - related to the horizontal motion of the Amurian plate with respect to northeastern Honshu. Their work was based on Henry et al. [2001], who estimated net deformation from GPS measurements to be directed west-northwest, ahead of the Izu-Bonin arc collision. Their inferred direction of additional deformation and magnitude of approximately 1.5-2 cm/yr agrees reasonably with the misfit in southern Tohoku.

In spite of the above discrepancies - some of which are due to phenomena we do not model here – to first order, ruptures on existing asperities do seem to explain a significant portion of the horizontal velocities in northeastern Japan. Once the Nemuro asperity is corrected, and the Shikotan rupture is included, we expect the agreement between the observed and predicted horizontal velocity field to be much better even in northeastern Hokkaido.

![Figure 5-12](image)

**Figure 5-12.** Observed (left), synthetic-frictional (middle), and residual (right) vertical GPS velocity fields (relative to a fixed Eurasian plate) for the period 1996-2000, for the same frictional rheology as in Figure 5-10.

The observed and predicted vertical velocities as well as their residuals are presented in Figure 5-12. Deep afterslip seems to explain part of the subsidence along the Sanriku, and southeastern Hokkaido coasts. However, most of the vertical signal remains
unexplained. The residuals along the west coast could be due to the fact that we do not model the incipient subduction in Japan Sea. It has long been known that much of the eastern Tohoku coastline has been experiencing persistent subsidence relative to the Eurasian plate. It has been argued that this subsidence is perhaps related to ongoing subduction erosion [Aoki and Scholz, 2003; Heki, 2004; Hashimoto et al., 2008]. We do not consider off-fault processes here, and therefore cannot correctly model the observed vertical geodetic data – even in eastern Tohoku.

5.6 Conclusions and future work

The results presented above demonstrate that the procedure developed here provides us with a unique way to probe deformation during the late post-seismic to interseismic time-periods. In a manner similar to the locking of large regions of the megathrust required by interseismic geodetic data inversions [e.g., Suwa et al., 2006], we too require large areas of afterslip (especially downdip) of the inferred asperities to explain current horizontal geodetic velocities. Such large afterslip areas create regions around the asperity having negligible slip-rates late in the seismic cycle, thus mimicking the effects of large slip-deficits required by interseismic geodetic data. Explaining the verticals is a more challenging problem that our single-fault model may not be able to constrain. However, our hypothesis that mechanical coupling on inferred asperities alone is sufficient to explain available geodetic observations along the Japan megathrust seems to be reasonable. More detailed exploration of the frictional rheology parameter space are required to solidify this assertion. Based on the systematic under-prediction by our model, we postulate that perhaps a dynamically weaker rheology might be needed to explain the larger observed late-cycle velocities.

There are some issues related to our model that still need to resolved. Chief among them is to correct for the slab interface downdip on Nemuro-oki, and add the 1994 $M_w$ 8 Shikotan asperity northeast of the Nemuro asperity. Another issue is the exact plate convergence velocity used. The values used in literature range from 9.5 cm/yr [e.g.,
Heki, 2004; Suwa et al., 2006], to 8.3 cm/yr, depending on whether the Eurasian or Okhotsk plates are used as the reference frame. A 10% larger plate velocity will result in synthetic velocities being that much larger, and therefore reduce the misfits further in Fukushima and southeastern Hokkaido. Also, in order to avoid reference frame issues, it may be more appropriate to compare strain rates instead of velocities. Using depth dependent rheological parameters may result in slip being constrained to the shallower portions of the megathrust, leading to stronger horizontal signal from both the shallower dip (on average) as well as by creating a larger zone of apparent locking.

Looking farther into the future, the procedure introduced here can be extended to model the full post-seismic to inter-seismic response of the megathrust to specified ruptures. Including ruptures on other major faults in the region (e.g., those related to incipient subduction in Japan Sea, or the Kurile sliver) can help us understand the current surface deformation field even better. This method can also be applied to other subduction zones where high density geodetic data may become available in the near future (e.g., Sunda Trench off Sumatra, or the Peru-Chile subduction zone). The ability to probe the synthetic velocity field in 3D, and being able to follow the evolution of surface displacements at hundreds of stations simultaneously has potential to provide valuable insights into the behavior of the subduction zones over the seismic cycle.
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