- I. KINETICS OF THE THERMAL DECOMPOSITION OF NITROGEN
  DIOXIDE BEHIND SHOCK WAVES
- II. KINETICS OF THE FERROUS ION-OXYGEN REACTION IN SULFURIC ACID SOLUTION

Thesis by

Robert Eugene Huffman

In Partial Fulfillment of the Requirements

For the Degree of

Doctor of Philosophy

California Institute of Technology

Pasadena, California

#### ACKNOWLEDGEMENTS

I would like to express my gratitude to Professor Norman Davidson, who has directed the research presented here. His guidance, enthusiasm, and patience have been greatly appreciated. Professor E. H. Swift has supervised my teaching experience, and his stimulating direction is acknowledged. I would especially like to thank all the people in Professor Davidson's group who preceded me on the shock tube project for the development of procedures and the construction of apparatus.

The Corning Glass Works Foundation and the General Education Board have each contributed fellowships, and their support is gratefully acknowledged. The shock wave research was financially supported by the Office of Naval Research, and the ferrous ion kinetics research was supported by the Atomic Energy Commission. These agencies have also contributed summer grants, and the Office of Naval Research has contributed a research assistantship. This support is appreciated.

I would like to thank my wife, Jackie, for her patience and understanding.

Shock waves into argon containing a small amount of NO have been used to study the kinetics of the thermal decomposition of nitrogen dioxide from 1100 to 2300°K. Mole fractions of NO<sub>2</sub> varied from  $2.8 \times 10^{-3}$  to  $1.5 \times 10^{-1}$ ; the ratio argon/NO2 varied from 5.6 to 360; the argon concentration varied by a factor of twenty; and the NO concentration varied by a factor of ten. Under these conditions, the results indicate that two separate reaction mechanisms are operative. One path has the rate law  $-d[NO_2]/dt = k_{11}[NO_2][A]$ with  $k_{ij} = 3 \times 10^{13} \exp[-65400/RT] \, \underline{M}^{-1} \, \text{sec}^{-1}$  and is apparently the unimolecular decomposition of NO2 at the second order limit. The other path has the rate law  $-d[NO_2]/dt = k_b[NO_2]^2$ with an activation energy of 22 + 6 kcal/mole. This path is believed to be the bimolecular decomposition of NO2 first observed by Bodenstein. However, extrapolation of this mechanism to the shock tube temperatures gives results about eight times too low. The reason for this discrepancy is not known. One interpretation is that there is another bimolecular reaction path for the decomposition of NO2. A good possibility for such a path is the bimolecular formation of NO2, recently postulated by Ashmore and Levitt, and its subsequent rapid decomposition, either by reaction with NO2 or by unimolecular dissociation into NO2and O. This discrepancy has also recently been observed by Steinburg and Lyon in a concurrent investigation. However, the mechanism and conclusions of that study are not supported by the present investigation.

Part II consists of a paper that has already been published on the kinetics of the ferrous ion-oxygen reaction in sulfuric acid solution.

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# I. KINETICS OF THE THERMAL DECOMPOSITION OF NITROGEN DIOXIDE BEHIND SHOCK WAVES

## A. Previous Investigations

At temperatures of around 800°K and above, nitrogen dioxide is unstable thermodynamically with respect to nitric oxide and oxygen.

$$NO_2 + NO_2 = NO + O_2 + NO$$
 (1)

The rates of both the forward and reverse of reaction 1 have been extensively studied. Bodenstein and Ramstetter (1) used a manometric technique and observed that, between 592 and 656°K, the rate of the forward reaction was proportional to the square of the NO<sub>2</sub> concentration and the activation energy was 26.6 kcal/mole. Thus for this case the above stochiometric equation is, in fact, the elementary reaction. kinetics of the reverse reaction were studied by Bodenstein and Lindner (2) from 470 to 662°K, and the reaction was found to be termolecular as written. From the known equilibrium constant, the bimolecular rate constants for the forward reaction were computed. The two sets of data form a single line on an Arrhenius plot of log rate constant versus reciprocal temperature (3). This is one of the classical demonstrations that the equilibrium constant of an elementary process is the ratio of the forward to the reverse rate constant. The combined data may be well represented by the rate expression (4):

$$k_h = 1.8 \times 10^9 \exp \left[-26600/RT\right] M^{-1} sec^{-1}$$

where  $k_{\rm b}$  is the rate constant for reaction 1 in the forward direction and M signifies units of moles per liter.

The kinetics of reaction 1 have recently been studied by a spectrophotometric method by Rosser and Wise (5) between 630 and  $1020^{\circ}$ K over  $NO_2$  concentrations of  $10^{-4}$  to  $10^{-5}$  M. They too report a bimolecular rate law. The combined data of all investigations fit a single straight line on an Arrhenius plot with an activation energy of 26.9 kcal/mole. Rosser and Wise found the reaction strictly homogeneous and unaffected by large pressures of the inert gases nitrogen, helium, and carbon dioxide. Their expression for the rate constant is  $k_b = 4.0 \times 10^9$  exp [-26900/RT] M<sup>-1</sup> sec<sup>-1</sup>.

Ashmore and Levitt (6) have reported that initial rates of nitrogen dioxide pyrolysis near 700°K are greater than the rates observed by Rosser and Wise at this temperature or the extrapolated rates of Bodenstein and Ramstetter. The reaction was followed by measuring the change in light absorption through a heated cylindrical cell with a logarithmic photometer and high speed recorder. In this way the concentration could be measured every five seconds. The initial rate was about twice as great as the rate expected from the earlier work, but the rate decreased to the expected value as the reaction proceeded. This increased initial rate was not observed when NO was present initially, so the conclusion

was drawn that the presence of NO, either added initially or due to reaction, inhibits the mechanism responsible for the increase in initial rate. Ashmore and Levitt have proposed the following mechanism involving NO<sub>3</sub>, the nitrate free radical.

$$NO_2 + NO_2 \xrightarrow{k_2} NO_3 + NO$$
 (2)

$$NO_3 + NO - \frac{k_3}{2} > NO_2 + NO_2$$
 (3)

$$NO_3 + NO_2 \xrightarrow{k_4} NO_2 + O_2 + NO$$
 (4)

Reactions 3 and 4 are well known in the thermal decomposition of  $N_2O_5$ , and a recent summary of estimates of their rate constants is available (7). By combining information obtained from the shock tube investigation of the  $N_2O_5$  decomposition by Schott and Davidson (7) and other studies, it is possible to arrive at independent values of  $k_2$ ,  $k_3/k_4$ , and  $k_3/k_4k_2$  (8) which agree fairly well with the values published by Ashmore and Levitt. These values will be considered further when attempts to extrapolate the Ashmore and Levitt mechanism to high temperatures are considered. It should be pointed out that the bimolecular path first observed by Bodenstein and Ramstetter is also occurring, and after inhibition of the Ashmore and Levitt mechanism by NO has become effective, the simple bimolecular path may be observed. Ashmore and Levitt

find the bimolecular rate constant  $k_b = 19.4 \ \underline{M}^{-1} \ \text{sec}^{-1}$ , which agrees very well with the value 20  $\underline{M}^{-1} \ \text{sec}^{-1}$  reported by Rosser and Wise at  $707^{\circ}$ K.

The kinetics of NO<sub>2</sub> decomposition at the high temperatures behind shock waves was investigated briefly in this laboratory by Dr. W. R. Gilkerson in 1954. The results of this unpublished investigation were that the process had an activation energy of about 25 kcal/mole and that the reaction was proportional to the square of the total gas concentration.

As the present investigation was being conducted, a concurrent investigation of NO2 decomposition behind shock waves was reported by Steinburg and Lyon (9). The reaction was studied in mixtures containing 1 to 3.22% NO, in argon over the temperature region 1400-2500°K in a three inch square shock tube. The reaction was followed by measuring the absorption of light of a small wavelength band near 436 mm, as in the present experiments. The decomposition rate was reported to be first order in both NO, and argon, resulting in the rate expression -d  $[NO_2]/dt = k_{SI}[NO_2][A]$ . The rate constant is  $k_{SL} = 3.82 \times 10^{11} \exp [-46100/RT] M^{-1} sec^{-1}$ . As will be discussed in more detail later, the two shock tube investigations give identical rates of decomposition under identical conditions. When NO2-argon mixtures are rapidly heated and compressed by a shock wave, light emission is observed which is yellow-orange in color. Steinburg and Lyon

found the intensity of this light to follow the  $NO_2$  concentration. This conclusion has been qualitatively verified in the present investigation.

The mechanism proposed by Steinburg and Lyon is given below.

$$NO_2 + A \xrightarrow{k_5} NO_2^* + A$$
 (5)

$$NO_2^* + A \xrightarrow{k_6} NO_2 + O + A$$
 (6)

$$NO_2^* + A \xrightarrow{k_7} NO_2 + A + hv \tag{7}$$

$$NO_2 + O \xrightarrow{k_8} NO + O_2$$
 (8)

From their empirical observation of a 46 kcal/mole activation energy they rule out the dissociation reaction 9 below, which has an activation energy of around 71 kcal/mole. However, the above mechanism is highly implausible, as will be discussed in detail later.

The present investigation, over wider concentration ranges, indicates that the decomposition proceeds partly via the Bodenstein mechanism and partly via the "quasiunimolecular" decomposition described by reactions 9 and 10.

$$NO_2 + A = NO + O + A$$
 (9)

$$NO_2 + O = NO + O_2 \tag{10}$$

Reaction 9 is rate determining since 10 is very fast. The apparent activation energy is therefore intermediate between 26.6 and 71 kcal/mole and is dependent on the experimental conditions. Under suitable conditions in the present work, an activation energy of 57 kcal/mole was observed in experiments designed to emphasize the contribution of reaction 9. Therefore, the present investigation does not support the mechanism or the conclusions of Steinburg and Lyon.

Other investigations of nitrogen oxide reactions by the shock tube method include the study of  $N_2O_5$  decomposition rates mentioned above (7), and the study of the room temperature decomposition of  $N_2O_4$  to  $NO_2$  by Carrington and Davidson (10). The fact that the latter reaction is quite rapid at room temperature means that it will have no influence upon the high temperature decomposition of  $NO_2$ .

# B. The Experimental Method

### 1. Introduction

The thermal decomposition rate of NO, has been observed over the temperature range 1100 to 2300°K in a gas mixture of argon containing a small amount of NO2. The high temperatures result from passage of a plane shock wave through the gas mixture contained in a shock tube. The NO2 mole fractions ranged from  $2.8 \times 10^{-3}$  to  $1.5 \times 10^{-1}$ , and initial pressures of NO2-argon mixture ranged from .01 to .1 atm. The pressure and density ratios across the shock depend on the shock speed and composition of gas. The NO2 concentration behind the shock wave varied from about 7.8 x  $10^{-5}$  to about 8.0 x  $10^{-4}$  M or a factor of ten. The argon concentration varied from  $1.5 \times 10^{-3}$  to  $3.0 \times 10^{-2}$  M or a factor of twenty. The ratio argon/NO2 varied from 5.6 to 360 or a factor of sixty-five. Final pressures behind the shock wave varied from .23 to 4.4 atm.

The general technique of studying fast reactions behind shock waves, as previously developed in this laboratory, has been used (11). The shock wave is generated in a shock tube--a long, cylindrical tube separated into two sections by a diaphragm of easily ruptured material. Gases such as helium and hydrogen are placed in one section at high pressure, and the gas under investigation is placed in the other section at a lower pressure. When the diaphragm is ruptured,

a shock wave is propagated into the gas under study, which imparts a large amount of enthalpy to an element of the gas in the time of a few collisions. If observations are made at a place sufficiently far removed from the diaphragm so that the wave has become stable, all the gas parameters immediately behind the wave are constant and may be calculated from the initial conditions and one property of the shock The property is usually the incident shock wave speed. The calculation assumes that equilibrium is established in the time of a few collisions, and for many gases this assumption is found to be true over a wide temperature range. processes such as chemical reaction, ionization, or vibrational relaxation may require a certain observable time to reach equilibrium, so it is in principle possible to study these events. Also, the temperature and density behind the shock wave change as these processes occur, since a change in enthalpy is involved. In the present case, the reaction is endothermic, and the temperature and density would change greatly behind the shock front if pure NO2 were placed in the tube. This would greatly complicate determination of the rate constant at a certain temperature, so a small amount of NO<sub>2</sub> and a large amount of argon is used instead. shock wave properties are largely determined by the argon, and this "heat buffer" greatly decreases the temperature and density changes behind the shock wave. In the current experiments, the change in light absorption by NO, due to chemical

reaction was observed with a photomultiplier-oscilloscope combination.

The reflected shock wave region has also been used in the present investigation in addition to the incident shock wave region discussed in the last paragraph. The reflected shock wave processes the hot compressed gas behind the incident shock wave, and therefore temperatures and pressures in this region are much larger than behind the incident shock wave. It is possible to adjust conditions so that no reaction occurs behind the incident shock but only behind the reflected shock. Therefore, much larger argon/NO<sub>2</sub> ratios and temperatures are possible with the same equipment. The calculation of gas parameters behind incident and reflected waves will be discussed in detail in a later section.

#### 2. Wave Motion in a Shock Tube

Shock wave methods offer a way of studying the rates of rapid gas phase reactions. The waves may be easily generated in a shock tube by allowing a high pressure gas originally in the driver section to push on the gas under investigation at a lower pressure in the shock wave section. Rupture of the diaphragm between these two sections causes a flow pattern which may be shown ideally on an x,t diagram (figure 1) of distance along the tube, x, plotted against t, the time after rupture of the diaphragm. The dimensions are those of the shock tube used in the present study, and the waves shown result from hydrogen at .57 atm in the driving section and argon at .04 atm in the shock wave section. This results in temperatures of 1341°K behind the incident shock and 2745°K behind the reflected shock if room temperature is 300°. The diagonal lines represent various disturbances moving through the gas; the reciprocal of the slope of the line gives its speed. Pressure profiles at various times are also shown.

When the diaphragm is removed, the high pressure gas pushes on the low pressure gas like a piston, causing a shock wave to move out into the gas. The shock wave compresses and imparts a large amount of enthalpy to an element of the gas. It moves into the gas under investigation with a speed, S, intermediate between the speed of sound in the cool, unshocked gas and the hot, shocked gas. Any compres-

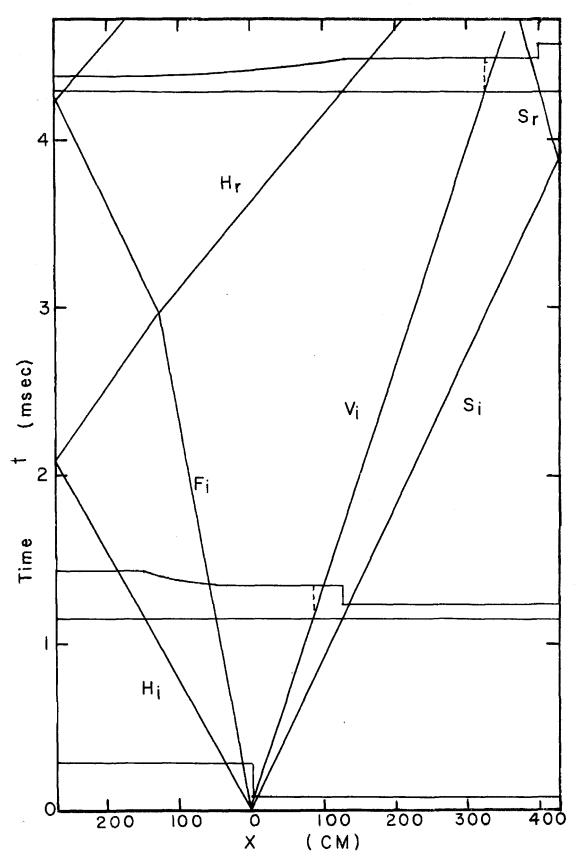


Figure 1. Shock Tube Flow Pattern

sion wave generated behind the shock wave will travel with the faster sonic speed in the hot gas and will overtake the shock front. Therefore, the shock front is self-sharpening, and even though the diaphragm does not shatter uniformly, a steady shock wave will result--empirically in a distance of ten or fifteen tube diameters. The temperature, density and pressure change as step functions across the shock front in a manner which may be calculated.

The gas behind the incident shock wave is set in motion with the speed v. Also, the original interface between the two gases moves into the shock wave section with the speed v of the gas flow behind the incident shock wave. In front of this interface is the hot, compressed gas under investigation; behind is the cool, expanded driving gas. The interface is not self-sharpening and spreads out by turbulent mixing of the two gases. Arrival of this "cold front" at an observation port therefore concludes an experiment; however, reflected shock waves may arrive first depending upon the geometry of the experiment.

The incident shock wave is reflected from the closed end of the tube as a second shock wave which travels through the once shocked gas, again sharply raising the temperature, density, and pressure. The gas behind the reflected shock, however, is at rest with respect to the shock tube. The gas parameters may be known in this region, and in this investigation both incident and reflected waves were used with the

same results under identical conditions.

An expansion wave travels into the high pressure gas in the driver section with the local sonic speed. This wave broadens with time, as the foot of the wave must travel with the lower sonic speed of the expanded, cool gas which is flowing toward the shock wave section. The head of the expansion fan is reflected from the end of the driver section as an expansion wave whose head moves into the shock wave section with a speed equal to the gas flow speed plus the local sound speed. This expansion wave could therefore overtake and dissipate the shock wave, so the driver section is made long enough to prevent interference from this wave. The relationships between these disturbances may be seen on the x, t diagram (figure 1). Methods of calculating the wave speeds and parameters of gases behind incident and reflected shock waves are described below.

The motion shown in the x, t diagram is for an ideal case in which the shock wave is set up instantly, and no energy is required to remove the diaphragm. In practice, the wave is usually somewhat weaker than predicted from the initial pressure ratio. The usual procedure is to work many tube diameters below the diaphragm and to base calculations on the measured speed of the shock front near the observation port. Experimental study of other dissipative effects in real gases has established that the simple equations neglecting

heat flow and viscosity are satisfactory. Many investigations have considered these problems; references 12, 13, and 14 are a few selected examples.

## 3. Observations of Rapid Events behind Shock Waves

The thermal decomposition rate of  $NO_2$  was measured by observing the change in light absorption through the  $NO_2$ -argon mixture in the shock tube with time. The sources of radiation were lines isolated from mercury arcs with interference filters. Nitrogen dioxide absorbs strongly from around 300 to 550 m $\mu$  (15), and mercury lines near 405, 436, and 546 m $\mu$  are satisfactory. A one mm wide sheet of this light passes through the shock tube and falls on the cathode of a photomultiplier.

The photocurrent is displayed as the vertical deflection of an oscilloscope trace. Photographs of a single oscilloscope sweep beginning just before the shock wave passes a given station therefore give a record of light intensity as a function of time.

Typical oscilloscope traces are shown in figure 2 for incident and reflected shock waves. As the shock wave passes before the observing station, the gas is compressed, and the signal is deflected upward, corresponding to smaller light transmission. As  ${\rm NO_2}$  disappears by reaction and forms the transparent products  ${\rm NO}$  and  ${\rm O_2}$ , the light transmission increases, and the trace moves lower. At sufficiently low temperatures, no reaction is observed (figure 2 (a) and (d)). The fact that this signal is constant proves that the conditions behind the shock wave are somewhat uniform. A slow and fast reaction behind incident shock waves (figure 2 (b) and (c)) illustrates typical experimental observations. The

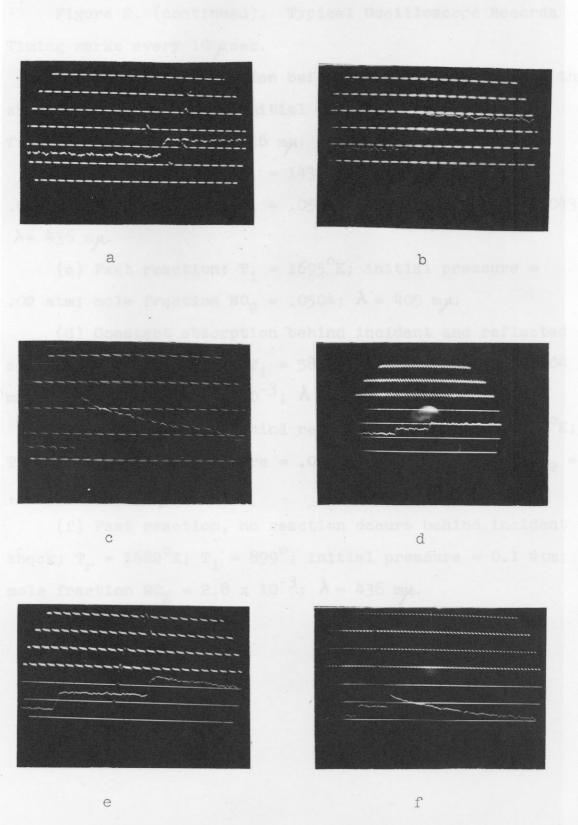


Figure 2. Typical Oscilloscope Records

- Figure 2. (continued). Typical Oscilloscope Records Timing marks every 10  $\mu$ sec.
- (a) Constant absorption before and after passage of the shock wave;  $T_i = 844^{\circ}K$ ; initial pressure = .04 atm; mole fraction NO<sub>2</sub> = .023;  $\lambda$  = 436 m $\mu$ .
- (b) Slow reaction;  $T_i = 1431^{\circ} K$ ; initial pressure = .02 atm; mole fraction NO<sub>2</sub> = .0500; mole fraction NO = .0430;  $\lambda = 436 \text{ m}\mu$ .
- (c) Fast reaction;  $T_i = 1695^{\circ} K$ ; initial pressure = .02 atm; mole fraction NO<sub>2</sub> = .0504;  $\lambda$  = 405 m $\mu$ .
- (d) Constant absorption behind incident and reflected shock waves;  $T_r = 932^{\circ} K$ ;  $T_i = 583^{\circ}$ ; initial pressure = .04 atm; mole fraction NO<sub>2</sub> = 7 x 10<sup>-3</sup>;  $\lambda$  = 436 m $\mu$ .
- (e) Slow reaction behind reflected shock;  $T_r = 1716^{\circ}K$ ;  $T_i = 952^{\circ}$ ; initial pressure = .019 atm; mole fraction  $NO_2 = .0234$ ;  $\lambda = 436$  m $\mu$ .
- (f) Fast reaction, no reaction occurs behind incident shock;  $T_r = 1682^{\circ} K$ ;  $T_1 = 899^{\circ}$ ; initial pressure = 0.1 atm; mole fraction  $NO_2 = 2.8 \times 10^{-3}$ ;  $\lambda = 436$  m $\mu$ .

remaining two photographs (figure 2 (e) and (f)) illustrate reactions behind reflected shock wave, and it may be seen that no reaction takes place behind the incident wave. Other sweeps are for calibration of the photocurrent, and the timing marks are ten  $\mu$  sec apart in all cases.

## 4. Instruments and Procedures

The experiments reported here were done in a 15 cm diameter shock tube of aluminum and pyrex glass pipe. The lengths of the driving section and the shock wave section were increased about 50 percent over the tube previously described (11). The driving section: was a 270 cm aluminum pipe, while the shock wave section consisted of a 140 cm aluminum pipe and two 150 cm pyrex glass pipes. Optical measurements were made directly through the pyrex glass pipe. The sections were sealed with "O" rings lubricated with silicone stopcock grease (Dow Corning Company) and held together with standard glass pipe flanges. For experiments behind incident shock waves, the ends of the driver and shock wave sections were closed with flat plates. For experiments with reflected shock waves, a special end plate was used which placed the reflecting surface about 12 centimeters in front of the end of the glass pipe. The clearance between the circumference of this plate and the inside glass wall was about one mm. A plunger arrangement allowed the portion of the shock tube behind the reflecting surface to be evacuated through a hole in the reflecting plate. This opening could then be closed immediately before the diaphragm was burst. The reflecting surface was about 3 cm from the station at which observations of the reflected shock were made.

The shock wave section of the tube could be pumped to below 0.1  $\mu$  mercury pressure, but usual practice was to

evacuate to 1 pressure before placing the NO2-argon mixture in the tube. The pumping time in this case was around eight hours, and this long time was the limiting factor in collecting data. A mercury diffusion pump, protected with liquid nitrogen at all times, was used to evacuate the shock wave section. A mechanical oil pump evacuated the driving section. The leak rate was measured at various times, and a value of 0.05 pm/min was typical. Apiezon N grease was used on the stopcocks. Cellulose acetate sheets were used for diaphragm material and were usually burst by touching with a needle. The pressure of NO2-argon mixture in the shock tube was measured with a butyl phthalate manometer, while the high pressures of the driving section were measured approximately with spring type dial gauges.

Two types of mercury arc lamps were used as sources for the photoelectric observation of NO<sub>2</sub> concentration. In practically every experiment, a Hanovia Type SH quartz lamp (No. 5352) was operated from a 120 volt battery bank at 150 watts. The 436 m µ line was isolated, and the light intensity was measured with an RCA 931-A photomultiplier. In several early experiments, an Osram HBO 200 high pressure d.c. mercury arc operated as described previously was used (16). The 405 m µ line was isolated, and an RCA 1P28 photomultiplier was used. The 1P28 tube is the 931-A with a quartz jacket to improve the ultraviolet sensitivity. This arc became unstable in operation, and the Hanovia arc was then used

exclusively. Experiments with higher concentrations of NO<sub>2</sub> used the 546 mm line isolated from the Hanovia lamp and collected on a 931-A photomultiplier.

Filter combinations found useful in this work are presented below.

Wave length (mu)	Interference filter	Corning cutoff filter	Half maximum width (m, m)
405	405 (B & L)	3060	11
436	436 (B & L)	3060	10
546	546 (Baird)	3486	15
	(monolayer	)	

The various light beams through the Pyrex shock tube passed three one mm slits before falling on the photomultiplier.

The optical instrumentation has been previously described and was used unchanged in the present experiments (17).

In experiments behind both incident and reflected shock waves, the speed of the incident shock wave front was measured to provide the extra condition needed to solve the shock wave equations. This speed was measured by an optical method-based on the schlieren effect-between two stations on the optical bench 30.00 cm apart. The rapid change in density as the shock wave passes an observation station will deflect a light ray several degrees toward the upstream side. Light beams are positioned on the three slit optical path so that they partly go through the last slit and partly fall on the upstream side of the slit. As the shock wave passes

before a timing station, the amount of light passing through the last slit and falling on the photomultiplier changes rapidly. This give a sharply rising signal which may be amplified and used to switch a timing circuit. The light sources are 500 watt tungsten filament projection lamps operated at 120 volts d.c.; the photomultipliers are 931-A The sharply rising signal from the photomultiplier triggers a pulse from a monostable multivibrator (univibrator) circuit. This "flip-flop" circuit effectively amplifies the pulse so that it may be used to switch a crystal controlled timing circuit (Potter Model 456 1.6 megacycle counter chronograph). Blue cobalt glass filters were used to make the intensity of the tungsten lamps comparable with the mercury arcs. The total change in intensity of the triggering light beam is enhanced by the light absorption of NO2 behind the shock wave.

In addition to switching the timer, the pulse from one timing station was used to trigger a single sweep on either one or both of two oscilloscopes available (Tektronix, model 512). This negative pulse is taken from the circuit at the plate of a thyratron (6D4) inserted after the stage from which the timer pulse is taken. The relatively slow recovery time of the thyratron insures that extraneous sweeps will not be triggered after the passage of the shock. Such triggering might occur from passage of reflected shock waves, various expansion waves, or bits of membranes in front

of the light beam. The oscilloscope sweep was triggered by the first timing station when the reaction was observed behind incident shock waves. The reaction was followed at one of the two stations between the timing stations. When the reaction was followed behind reflected shocks, the timing station which cut off the timer started the sweep. The reaction was followed at a station between the last timing station and the reflected shock end plate. This enables the reaction to be followed before boundary layers grow too large.

The photomultipliers were operated so that 100 microamperes of plate current were drawn through a plate resistor of 104 ohm, and therefore the deflection on the scope was about one volt. The plate of the photomultiplier was connected to the vertical amplifier input of the scope with about three feet of low capacitance coaxial cable (13 µ f/ft). The scope presents a capacitance of 45 مرم in the vertical amplifier circuit. Therefore, the rise time of the photomultiplier-scope combination should be about one microsecond. All electronic equipment was given time to become thoroughly stable in operation before an experiment was performed. change in current through the photomultiplier as the shock passes would tend to change the voltage across each dynode stage. This voltage controls the total amplification of the signal and is typically 60 volts per stage in these experiments. The effect is most serious in the last few

dynode stages, where the space current is an appreciable fraction of the total current through the tube. Therefore, the voltage is held fixed across the last three dynodes for a few milliseconds by suitable capacitors.

Photographs of the sweeps and calibration marks were made on the very fast Kodax Linagraph Pan 35 mm film. These photographs were accurately traced from enlarger projections. Light intensity values at various times were measured from the tracings.

The calibration procedure for interpreting vertical deflection measurements is described by G. Schott (16). The photomultiplier output enters the scope vertical amplifier circuit at one terminal of the difference amplifier, and a dry cell is connected to the other terminal. Immediately after completion of the experiment, the photomultiplier cable is replaced by a connection to ground, and sweeps at various accurately known fractions of the dry cell voltage are photographed. The voltage is measured with a Helipot precision potentiometer. The photocurrent values as a function of time can then be obtained. It is necessary that the scope does not change in sensitivity between the photomultiplier record and the calibration records. It will be noticed that no scope control must be used to carry out this procedure. An important precaution is that the grid of the side of the difference amplifier that is not used during the calibration must not be allowed to float, but must be

connected to ground. The scopes used in this investigation—when operated so that the input signal was d.c. coupled to the vertical amplifier—have the annoying feature that rapid changes in d.c. level are not measured accurately. The correct d.c. value is not reached for several seconds. The discrepancy was found to be typically 3%, and corrections for this "d.c. shift" were applied to all photomultiplier records. Timing marks were placed on the photomultiplier and calibration sweeps by applying pulses to the cathode of the cathode ray tube every ten microseconds from a crystal controlled 100 kilocycle circuit.

## 5. Reagents

Nitrogen dioxide (The Matheson Company) was purified using the method of reference (16). Oxygen (Linde) was passed through a dry ice trap filled with glass wool and then was bubbled through liquid NO2 in an ice-salt bath. The liquid was initially dark blue-black due to the presence of  $N_2O_3$ , but became light yellow in color, since the NO present had either been swept out or oxidized. At this stage, the oxygen stream saturated with NO2 vapor was diverted to a train consisting of  $P_2O_5$  coated glass beads and a storage trap on the vacuum line. After the NO2-02 stream had swept through the trap about five minutes, collection of the NO2 was begun. It was frozen out as a very pale yellow solid in the storage trap by a dry ice-trichloroethylene bath. About two-thirds of the liquid NO2 remaining in the ice-salt bath was distilled in the stream of 02 into the storage trap. The oxygen was then pumped off, and the NO2 was stored as a solid under dry ice.

Nitric oxide (The Matheson Company) was purified by distillation, and the main impurity was  $NO_2$ . Nitric oxide was condensed under liquid  $N_2$  in a trap on the vacuum line as a green, brown, blue, and white solid. The material was then distilled twice from the liquid at about  $-150^{\circ}$ C to a trap cooled with liquid  $N_2$  at  $-196^{\circ}$ C. The temperature of the  $NO-N_2O_3$  solution was not easy to control by lowering the liquid  $N_2$  level in a dewar flask. The resulting dangerously

large vapor pressure could blow out stopcocks. A methylpentane bath (Phillips Petroleum Company, Methylpentanes, commercial grade) which had been cooled with a liquid N<sub>2</sub> cold finger is usable to around -160°C and is very satisfactory for holding the liquid NO-N<sub>2</sub>O<sub>3</sub> at -160 to -150°C, where the vapor pressure of NO above the solution is in the one atmosphere range. After the second distillation the solid was a uniform very light gray which melted to give a light greenish-blue liquid.

Mixtures of NO, and argon were prepared as needed and stored in a 22 liter bulb covered with black cloth to prevent photodecomposition from the room fluorescent lamps. As many as twenty and as few as two shock tube fillings could be stored. The NO2 under dry ice in the storage trap was pumped on briefly with the mercury diffusion pump and then was allowed to melt. The manifold and storage bulb were conditioned by allowing about 30% of the final  ${\tt NO_2}$  pressure to stand in the system for about ten minutes and then pumping this gas out. Next, NO2 was allowed to flow into the bulb to the desired pressure, as determined by a butyl phthalate manometer. The storage bulb stopcock was closed, and the NO2 in the vacuum manifold was pumped out. Argon (Linde, 99.92% pure, principal impurity  $\rm N_2$ ) was used without further purification and was added to the manifold in such a way that a small positive pressure was always maintained in the argon line. About .8 atm argon, as measured with a

mercury manometer, was placed in the manifold, and then the storage bulb stopcock was opened slightly. Argon at the much higher pressure filled the bulb, and no NO<sub>2</sub> escaped. When the pressure reached one atm, the manifold was isolated from the argon supply. About 15 seconds were allowed for the NO<sub>2</sub> and argon pressure inside the bulb to slightly adjust to the argon pressure in the manifold, and then the storage bulb stopcock was closed. The manifold pressure was then the total pressure in the storage bulb.

It was necessary to correct for the  $N_2O_{\frac{1}{4}}$  present to determine the formal mole fraction of  $NO_2$ . Values of the equilibrium constant for the reaction

$$2NO_2 = N_2O_{\downarrow\downarrow}$$

were taken from Yost and Russell (18). By combining the results of several investigations, they recommend  $\Delta F_{298}^{0} =$  -1110 cal,  $\Delta H_{298}^{0} =$  -13693 cal, for the reaction as written above. The equilibrium constant is therefore  $K_{298} = P_{N_20_{||}}/P_{N0_2}^{2} = 6.51 \ \text{atm}^{-1}$ . This constant was corrected to the measured room temperature. The formal NO<sub>2</sub> mole fraction is then the NO<sub>2</sub> mole fraction plus twice the N<sub>2</sub>O<sub>||</sub> mole fraction.

The NO-NO<sub>2</sub>-argon mixture was prepared by flowing NO to the desired pressure into the storage bulb using the butyl phthalate manometer. Then an NO<sub>2</sub> pressure over twice as great was placed in the manifold, and the storage bulb

stopcock was slightly opened, allowing the NO<sub>2</sub> to flow into the storage bulb with a higher pressure in the manifold. The total pressure of NO<sub>2</sub> and NO was then measured by allowing the manifold and bulb pressures to equalize as explained above. Then argon was placed in the bulb as before. In all cases, the contents of the bulb were allowed over eighteen hours to mix before being used for an experiment.

6. Calculation of Gas Parameters behind Incident and Reflected Shock Waves

The gas parameters behind plane incident and reflected shock waves may be calculated from a knowledge of the initial temperature, initial pressure, initial composition and one property of the shock wave--almost invariably the incident shock speed. The equations of flow through a shock front -the Rankine-Hugoniot conditions -- state that mass, momentum and energy are conserved in the process. The equation of state of the material must also be known. Since one is mainly concerned with the properties of an inert gas at high temperatures and low pressures, the perfect gas law is used. The reflected shock parameters may be obtained from the additional condition that the gas behind the reflected shock front has no material velocity. Discussions of solution of the shock wave equations for the case of a reacting gas have been given previously (17), so the present discussion will refer almost exclusively to the system of this investigation.

The Rankine-Hugoniot conditions will be set up initially with respect to a stationary shock front--either incident or reflected. The velocities concerned are shown below both for shock stationary coordinates and for laboratory coordinates; the vertical lines denote the shock front.

The subscript 1 refers to gas through which the wave has not passed; subscript 2 refers to shocked gas. Subscript i refers to incident shocks, and subscript r refers to reflected shocks. The speeds u refer to material or gas flow speeds relative to the shock front. The speeds of the shock fronts are denoted by S, and v<sub>i</sub> refers to the material speed, all in the laboratory system. The gas is not flowing in the laboratory coordinates before the passage of the incident shock and behind the reflected shock. Therefore, the two sets of speeds are related by the expressions below.

$$S_{i} = u_{1}$$
  $S_{r} = u_{2r}$   $v_{i} = u_{1} - u_{2}$   $S_{r} + v_{i} = u_{1r}$ 

The magnitudes are correctly given by the equations presented; the directions of the motions are shown in the diagram above.

The Rankine-Hugonoit conditions in the shock stationary coordinates are:

$$\rho_1 u_1 = \rho_2 u_2 \qquad \text{mass} \tag{11}$$

$$P_1 u_1^2 + P_1 = P_2 u_2^2 + P_2$$
 momentum (12)

$$h_1 + \frac{1}{2}u_1^2 = h_2 + \frac{1}{2}u_2^2$$
 energy (13)

In these expressions,  $\rho$  is the gas density, P is the pressure, and h is the enthalpy per gram. The ideal gas equation

for one mole of gas of molecular weight W is:

$$\frac{P}{P} = \frac{RT}{W} \tag{14}$$

It is convenient to use the ratios given below.

$$\pi_{i} = \frac{P_{2}}{P_{1}} \qquad \pi_{r} = \frac{P_{r}}{P_{2}} \qquad \pi_{T} = \frac{P_{r}}{P_{1}}$$

$$\Delta_{i} = \frac{P_{2}}{P_{1}} \qquad \Delta_{r} = \frac{P_{r}}{P_{2}} \qquad \Delta_{T} = \frac{P_{r}}{P_{1}}$$

$$\Theta_{i} = \frac{T_{2}}{T_{1}} \qquad \Theta_{r} = \frac{T_{r}}{T_{2}} \qquad \Theta_{T} = \frac{T_{r}}{T_{1}}$$

The perfect gas equation for one mole then simplifies to:

$$\mathbf{\pi} = \Delta \Theta \tag{15}$$

From the Rankine-Hugoniot relations and the ideal gas expression, the incident shock speed,  $S_{i}$ , is found to be given by:

$$S_{i}^{2} = \frac{RT_{1}}{W} \frac{(\boldsymbol{\pi}_{i}-1) \boldsymbol{\Delta}_{i}}{(\boldsymbol{\Delta}_{i}-1)}$$
 (16)

The material speed behind the incident shock wave is:

$$v_i = S_i \left(1 - \frac{1}{\Delta_i}\right)$$
 (17)

The enthalpy change per gram across the shock front is:

$$h_2 - h_1 = \frac{1}{2} \frac{RT_1}{W} (T_1-1)(1+\frac{1}{\Delta_1})$$
 (18)

which may be rearranged with the aid of the perfect gas law to give:

$$\Pi_{i} = \frac{2W}{RT_{1}} (h_{2} - h_{1}) + 1 - \theta_{i} + \frac{1}{\Delta_{i}}$$
(19)

If the necessary enthalpies are known, 18 can be applied to shock waves in any gas. The reciprocal density ratio  $1/\Delta_i$  is very insensitive to changes in the temperature and is small, so 18 or 19 is usually solved for a given enthalpy and temperature ratio at an approximate  $1/\Delta_i$ . The correct  $1/\Delta_i$  is then found readily by iteration. One then has values of  $T_i$ ,  $\Delta_i$ , and  $\theta_i$  from which  $s_i$  and  $v_i$  may be calculated. For the inert gases, h = (5/2) (RT/W), and 19 becomes with this substitution:

$$TT_i = 4 (\Theta_i - 1) + 1/\Delta_i$$
 (20)

Extensive tables of incident shock wave parameters in dimensionless form for perfect monoatomic and diatomic gases exist (19).

The gas parameters behind reflected shocks may be obtained in simple closed form for the case in which the heat

capacity does not change with the temperature (13). In this case, the enthalpy is given by:

$$h = c \frac{P}{\rho} = \frac{\chi}{\chi - 1} \frac{P}{\rho} = \frac{\chi + 1}{2} \frac{P}{\rho}$$
 (21)

The various heat capacity expressions are:

The Rankine-Hugoniot relations then give the following expressions for any shock wave.

$$\Delta = \frac{\Pi \mu + 1}{\Pi + \mu} \tag{22}$$

$$\Theta = \frac{TI(T+\mu)}{T\mu + 1} \tag{23}$$

The incident shock imparts the material speed v<sub>i</sub> to the still gas, and the reflected shock reduces this speed back to zero again. The following expression is defined.

For incident and reflected shock waves, respectively:

$$\oint_{i} = \frac{v_{i}^{2}}{a_{1}^{2}} = \frac{(\pi_{i}^{-1})^{2}(\mu^{-1})^{2}}{(\pi_{i}\mu^{+1})(\mu^{+1})}$$
(24)

$$\oint_{r} = \frac{v_{i}^{2}}{a_{2}^{2}} = \frac{(\Pi_{r}^{-1})^{2}(\mu-1)^{2}}{(\Pi_{r}\mu+1)(\mu+1)}$$
(25)

The speed of sound, a, is  $(\chi_P/P)^{\frac{1}{2}}$ , and  $a_2^2/a_1^2$  is  $\theta_1$ . Combining 24 and 25 and substituting 23 gives a quadratic equation in  $\pi_p$ .

$$\frac{(\Pi_{i}^{-1})^{2}}{\Pi_{i}(\Pi_{i}^{+}\mu)} = \frac{(\Pi_{r}^{-1})^{2}}{(\Pi_{r}\mu+1)}$$
(26)

The roots of this equation are:

$$\Pi_{r} = \frac{\Pi_{i}(\mu+2)-1}{\Pi_{i} + \mu}$$
 (27)

$$T_{\rm r} = \frac{1}{T_{\rm i}}$$

The second solution is unacceptable physically.

From the first Rankine-Hugoniot condition applied to the reflected shock:

$$\Delta_{r} = \frac{u_{1r}}{u_{2r}} = \frac{S_{r} + v_{1}}{S_{r}} = \frac{\pi_{r} \mu^{+1}}{\pi_{r} + \mu}$$
 (28)

Substitution of  $v_i$  from 17 and  $\pi_r$  from 27 gives the reflected shock speed as a function of  $S_i$ ,  $\pi_i$  and  $\mu$ .

$$S_{r} = \frac{S_{i} (2\pi_{i} + \mu - 1)}{(\mu\pi_{i} + 1)}$$
 (29)

Substituting 27 in 22 gives:

$$\Delta_{r} = \frac{\pi_{1}(\mu + 1)}{2\pi_{1} + \mu - 1} \tag{30}$$

The perfect gas equation gives the final expression:

$$\Theta_{r} = \frac{\pi_{r}}{\Delta_{r}} \tag{31}$$

Therefore, if the parameters of the initial shock wave into the gas are known, the reflected parameters may be obtained. Values of the reflected shock wave parameters in argon over a reflected temperature range of 850-2750°K are given in Table 1. Since only small NO<sub>2</sub> concentrations were used in the reflected shocks, no calculation of reflected parameters with added NO<sub>2</sub> was made.

Solution of the shock wave equations for a reacting gas is more involved than the cases so far discussed where the enthalpy is directly proportional to the temperature. It is desired to find  $\pi_i$ ,  $\Delta_i$  and  $S_i$  for chosen  $\Theta_i$  for various initial compositions and amounts of reaction. The change in enthalpy across the shock front is a function of these variables. The initial temperature in all shock calculations was assumed to be  $300^{\circ}$ K, and the measured room temperature was

never far from this value. The derivation below refers to incident shocks only, and the subscripts i have been eliminated.

The molar enthalpy of mixtures of  $NO_2$  in argon at  $300^{\circ} K$  is:

$$H_{T_1} = \frac{(1-\phi) \mathcal{X}_A R T_i + \phi [(1-\alpha_i) \mathcal{X}_{NO_2} R T_i + (\alpha_i/2) \mathcal{X}_{N_2O_4} R T_i + \alpha U_a]}{1 - (\alpha_i/2) \phi}$$
(32)

The symbols are defined as follows:

 $H_{T_1}$  = molar enthalpy at temperature  $T_1$ 

 $\phi$  = formal mole fraction NO<sub>2</sub>

 $\alpha_1$  = degree of association of NO<sub>2</sub> to N<sub>2</sub>O<sub>4</sub> in the reaction NO<sub>2</sub> = 1/2 N<sub>2</sub>O<sub>4</sub>

 $U_{\alpha} = \Delta H_{o}^{\circ}$  of above reaction = -7300 calories

 $\mathcal{H} = (H_{T} - H_{o})/RT$ 

The denominator gives the number of moles present as a function of  $\alpha_1$  and  $\phi$  for an initial amount of one mole of NO<sub>2</sub>. The molecular weight of the gas mixture—the weight which contains Avagadro's number of molecules—is given by:

$$\overline{W}_{\alpha_{1}} = \frac{(1-\Phi)W_{A} + \Phi(1-\alpha_{1})W_{NO_{2}} + (\Phi/2)\alpha_{1}W_{N2O_{4}}}{1-(\alpha_{1}/2)\Phi}$$
(33)

$$= \frac{W_A + \phi(W_{NO_2} - W_A)}{1 - (\alpha_1/2)\phi} = \frac{\overline{W_1}}{1 - (\alpha_1/2)\phi}$$

Therefore,  $\overline{W}_{i}$  is the molecular weight for the case of no association to N<sub>2</sub>O<sub>4</sub>. The enthalpy per gram at 300°K is accordingly:

$$h_{T_1} = \frac{1}{\overline{W}_i} \left\{ (1 - \phi) \mathcal{X}_A R T_i + \phi \left[ \mathcal{X}_{NO_2 T_i} R T_i + \alpha_i U_a \right] \right\}$$
 (34)

The enthalpy  $\mathcal{H}_{N_2O_4}$  has been set equal to  $2\mathcal{H}_{NO_2}$  .

At the high temperatures of the gas behind the shock front,  $\mathrm{NO}_2$  is reacting to give NO and  $\mathrm{O}_2$ —the thermodynamically stable products. The small fraction of  $\mathrm{N}_2\mathrm{O}_4$  reacts very rapidly to give  $\mathrm{NO}_2$  and need not be considered. The process is represented stoichiometrically by:

$$NO_2 = NO + \frac{1}{2}O_2 \tag{35}$$

The standard enthalpy of this process at zero degrees is  $\Delta H_o^{\circ} = U_d = 12,795 \text{ cal/mole.}$  If the degree of reaction

in 35 is  $\alpha_2$ , the expressions analogous to 33 and 34 are:

$$h_{T_{2}} = \frac{1}{\overline{w}_{2}} \left\{ (1 - \Phi) \mathcal{H}_{R} R T_{2} + \Phi \left[ (1 - \alpha_{2}) \mathcal{H}_{NO_{2}T_{2}} R T_{2} + \alpha_{2} \mathcal{H}_{NO_{T_{2}}} R T_{2} + \alpha_{$$

$$\overline{W}_{2} = (1 - \Phi) W_{A} + \Phi \left[ (1 - \alpha_{2}) W_{NO_{2}} + \alpha_{2} W_{NO} + (d_{2}/2) W_{O_{2}} \right]$$
(37)

The perfect gas law for this situation is:

$$\pi = \left(1 + \frac{d_2 \Phi}{2}\right) \Delta \Theta \tag{38}$$

The enthalpy per gram at the two temperatures, 34 and 36, and the ideal gas law, 38, may be substituted into 18 and rearranged to give the final expression.

$$TT = -\left[1 + (\alpha_{2}/2) \Phi\right] \Theta + 1 + 1/\Delta + 5(1 - \Phi) \left[(\overline{w}_{1}/\overline{w}_{2})\Theta - 1\right] + 2\Phi(\overline{w}_{1}/\overline{w}_{2}) \left\{(1 - \alpha_{2}) \mathcal{H}_{NO_{2}T_{2}}\Theta + \alpha_{2} \mathcal{H}_{NO_{T_{2}}}\Theta + (\alpha_{2}/2) \mathcal{H}_{O_{2}T_{2}}\Theta + (\alpha_{2}/2) \mathcal{H}_{O_{2}T_{2}}\Theta + (\alpha_{2}/2) \mathcal{H}_{O_{2}T_{2}}\Theta + (\alpha_{2}/2) \mathcal{H}_{O_{2}T_{2}}\Theta\right] + (\alpha_{2}U_{2}/RT_{1}) - 2\Phi \left\{\mathcal{H}_{NO_{2}T_{1}} + (\alpha_{1}U_{2}/RT_{1})\right\}$$
(39)

When the degree of reaction  $\alpha_2$  is zero--immediately after passage of the shock front--the final expression is:

$$TT = 1 - \theta + 1/\Delta + 5(1 - \Phi)(\theta - 1)$$

$$+ 2 \Phi \left\{ \chi_{NO_{2}T_{2}} \theta - \chi_{NO_{2}T_{1}} - (\alpha_{1}U_{4}/RT_{1}) \right\}$$
(40)

The expressions 39 and 40 were solved for  $\pi$  and  $\Delta$ , by the iterative process previously described, for each mixture composition and initial pressure at zero and fifty percent reac-This calculation was generally done at the four temperatures 1000, 1500, 2000, and 2500 $^{\rm O}$ K. Values of S. could be calculated at these temperatures, and values of S, at intermediate temperatures could be found on plots of  $T_2$ against  $S_i^2$ , which are linear over this range. The values of  $T_2$  for each experiment were found from large graphs of  $T_2$ against S<sub>i</sub>. The value of  $\Delta$ , for  $\alpha$ , equal zero at various values of To was found to the accuracy required from smooth curves of  $\Delta_i$  for the NO<sub>2</sub>-argon mixtures minus  $\Delta_i$  for pure argon plotted against To. When NO is also present initially, its contribution to the enthalpy must be considered in a way which is analogous to the case with added NO<sub>2</sub> presented above. Values of gas parameters behind incident shock waves calculated for compositions used in this investigation are presented in Table 2.

Thermodynamic properties of NO and  ${\rm O_2}$  over a wide

temperature range have been obtained from NBS tables, Series III (20). The corresponding properties of NO $_2$  were taken from NBS-NACA tables (21). Values of  $\Delta$  H $_{_{0}}^{\bullet}$  were taken from Series I of the NBS tables (22).

The gas parameters behind the reflected shock wave are calculated from the measured incident shock wave speed. photoelectric records of intensity versus time for reflected shock wave experiments may be used to obtain an observed reflected shock speed. This speed may be compared with the reflected shock speed calculated from the observed incident shock speed. As shown in figure 2, the time between passage of the incident and reflected shock waves is the length of the "plateau" between the two upward deflections. With the distance between the observation slit and the reflecting surface and the observed incident shock speed known, the reflected shock speed may be easily calculated. Figure 3 represents  $S_r$ , the reflected shock speed, versus  $T_r/T_2 = \Theta_r$ , the temperature ratio between once and twice shocked gas. The curve refers to speeds calculated from the measured incident shock speed; the points refer to speeds measured from the photoelectric records. The approximate agreement between these quantities is comforting. The values shown in figure 3 are tabulated as table 3.

A further indication that viscosity and heat conduction effects do not invalidate experiments behind reflected shock waves is the observation that rate constants are the same to

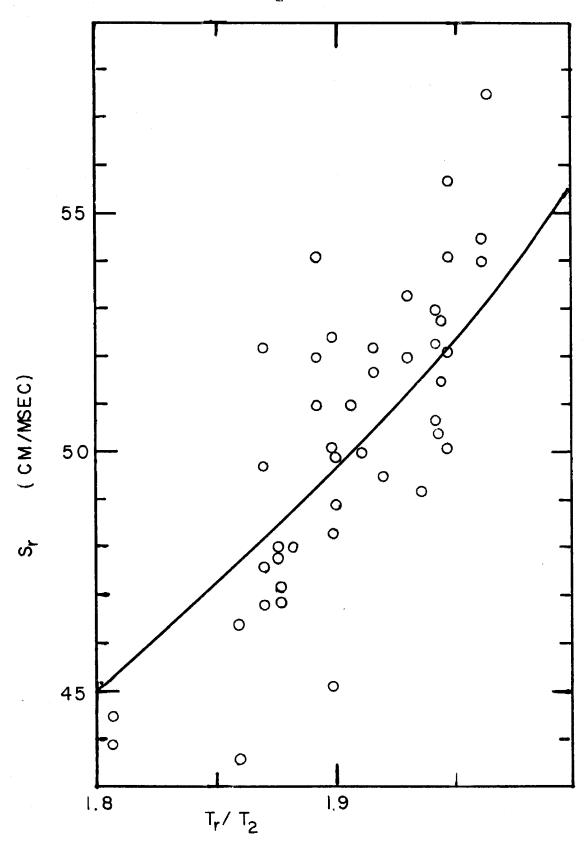


Figure 3. Measured and Calculated Reflected Shock Speeds
Line from incident shock; points from trace

within experimental error under the same conditions in reflected and incident shock waves. A series of experiments was done at an  $NO_2$  mole fraction of 2.3 x  $10^{-2}$  and an initial pressure of 0.04 atm behind incident shock waves. Another series at essentially the same mole fraction and an initial pressure of around 0.019 atm was done behind reflected shock waves. Since the ratio  $\Delta_r$  is around 2.1, the concentrations in the two regions were the same. Measured rate constants for these two types of experiment may be compared on an Arrhenius plot in figure 4 and seen to be equal within the experimental error.

7. Calculation of Rate Constants and Extinction Coefficients

Initial rate constants and extinction coefficients were calculated from the observed records of light intensity as a function of time. The ratio of incident intensity  $\mathbf{I}_0$  to transmitted intensity  $\mathbf{I}_1$  may be calculated for a given composition and pressure of gas by the following expression for the initial optical density  $\mathbf{D}_1$ .

$$\log_{10} \frac{I_0}{I_1} = \epsilon_1 [NO_2]_1 l = D_1$$
 (41)

The subscript 1 refers to properties of the unshocked gas;  ${\bf l}$  is the length of the light path. Measurement of  ${\bf e}_1$ , the room temperature extinction coefficient, is discussed later in this section. The intensity  ${\bf I}_1$  may be obtained from the photoelectric record before the gas is shocked, so the incident intensity  ${\bf I}_0$  is known also. Measured light intensity values at various times can then be converted into optical density values, which have the following simple relation to the degree of reaction  ${\bf e}$ .

$$D = \epsilon_2 \Delta [NO_2]_1 (1 - \alpha) \mathcal{L}$$
 (42)

The relation between the NO<sub>2</sub> concentration before and after passage of the shock is given by:

$$[NO_2] = [NO_2]_1 \Delta (1 - \alpha) \tag{43}$$

The symbol  $\boldsymbol{\prec}$  , the degree of reaction, is the same as  $\boldsymbol{\prec}_2$  of the last section. Differentiating 42 yields the expression:

$$\frac{d \ln D}{dt} = \frac{d \ln \epsilon}{dt} + \frac{d \ln \Delta}{dt} - \frac{1}{(1-\alpha)} \frac{d\alpha}{dt} \tag{44}$$

The last term of 44, the chemical reaction term, is much larger than the other two under the usual conditions of a large excess of buffer gas. The expression, 44, may be rearranged to give:

$$\frac{d \ln D}{dt} = \frac{d\alpha}{dt} \left[ \frac{d \ln \epsilon}{d\alpha} + \frac{d \ln \Delta}{d\alpha} - \frac{1}{1-\alpha} \right] \tag{45}$$

The particular expression used for  $\mathrm{d} \mathbf{A}/\mathrm{d} t$  depends on the assumed mechanism of  $\mathrm{NO}_2$  decomposition. The total decrease in  $\mathrm{NO}_2$  concentration with time,  $-\mathrm{d}[\mathrm{NO}_2]/\mathrm{d} t$ , is proportional to the sum of the change due to reaction, measured by  $\mathbf{A}$ , and the change due to density, measured by  $\mathbf{A}$ . For an assumed mechanism whose rate step is proportional to  $[\mathrm{NO}_2]$  and  $[\mathrm{M}]$ , the total gas concentration, this relation is:

$$\frac{d[NO_2]}{dt} = \frac{3[NO_2]}{3t} \Big|_{\Delta} + \frac{3[NO_2]}{3\Delta} \Big|_{\alpha} \frac{d\Delta}{dt}$$

$$= -k_1 \text{ obs } [NO_2][M] + \frac{3[NO_2]}{3\Delta} \Big|_{\alpha} \frac{d\Delta}{dt}$$
(46)

The first term on the right of 46 is the conventional isochoric reaction rate. Also,  $d[NO_2]/dt$  may be obtained from 43.

$$\frac{d[NO_2]}{dt} = -\Delta[NO_2]_1 \frac{d^{\alpha}}{dt} + [NO_2]_1 (1-\alpha) \frac{d^{\Delta}}{dt}$$
(47)

The second terms on the right of 46 and 47 are equal, so the first terms may be set equal and rearranged.

$$\frac{d d}{dt} = k_{1 \text{ obs}} \Delta[M]_{1} (1-\alpha)$$
 (48)

The time scale with which observations are made on reacting gases behind an incident shock wave is compressed since the reacting gas before the slit at any time has come from upstream. This means the gas has been heated for a time longer than the time since the shock wave has passed the observation station. The relation between the gas time  $\boldsymbol{T}$  and the laboratory time t is dt =  $\Delta$  d $\boldsymbol{T}$ , where  $\Delta$  is the compression ratio. In order to make the times in the expressions above correspond to times measured on the oscilloscope traces, the above relation is introduced. Behind reflected shocks the gas is at rest, and no such correction is needed. Therefore 48 becomes:

$$\frac{d \, \alpha}{d \, \tau} = k_{1 \text{ obs}} \, \Delta^{2}[M]_{1}(1-\alpha) \tag{49}$$

The final expression for  $k_{1 \text{ obs}}$  is obtained by combining 49 and 45 and letting  $\triangleleft$  approach zero for initial rate constants.

$$k_{1 \text{ obs}} = \frac{-\frac{d \ln D}{d \tau} \alpha = 0}{\Delta^{2} [M]_{1} \left[ 1 - \frac{d \ln \epsilon}{dT} \frac{dT}{d\alpha} - \frac{d \ln \Delta}{d\alpha} \right]}$$
(50)

For each experiment, values of  $\ln D$  were plotted against  $\pmb{\tau}$ , and the best initial slope obtained for use in the expression above. If one chooses to initiate the interpretation of the data by assuming that the reaction proceeds exclusively by the bimolecular path, the apparent second order constant,  $k_{2,obs}$ , can be calculated as:

$$k_{2 \text{ obs}} = k_{1 \text{ obs}} \frac{[M]_{1}}{[NO_{2}]_{1}}$$
 (51)

The term in brackets in 50 is a correction for change in  $\pmb{\epsilon}$  and  $\pmb{\Delta}$  with  $\pmb{\prec}$ . It is rarely less than .85 and is usually much closer to unity. To evaluate this term, it is necessary to know  $d\pmb{\epsilon}/dT$ ,  $dT/d\pmb{\prec}$ , and  $d\pmb{\Delta}/d\pmb{\prec}$  for each experiment. The factor  $d\pmb{\epsilon}/dT$  is obtained from graphs of  $\pmb{\epsilon}_2$  versus T. The change in temperature,  $dT/d\pmb{\prec}$ , is obtained from the expression:

$$\frac{\partial T}{\partial \alpha|_{S}} = -\frac{\partial S/\partial \alpha|_{T}}{\partial S/\partial T|_{\alpha}} \tag{52}$$

Shock calculations at  $\mathbf{A} = 0$  and  $\mathbf{A} = .5$  give two values of S at a given temperature, from which the numerator may be approximated. The denominator may be found from the empirical relation  $T_2 = AS^2 + B$ , which may be differentiated to give  $\mathbf{A} = \mathbf{A} = \mathbf$ 

By combining relations for the heat absorbed during the reaction with the hydrodynamic expressions, one can obtain explicit relations for L T/d a and d  $\Delta$ /d a. Values calculated from these relations agree well with the more approximate values described above for one mixture. Therefore, the approximate corrections are used throughout.

Room temperature extinction coefficients were measured for each filter combination with a photomultiplier and oscilloscope. Filter combinations described above were used. At 405 and 436 mm using the Osram and Hanovia arcs, respectively, the absorption of a known pressure of NO<sub>2</sub> was measured in a 10 cm cell with corex windows. At 546 mm with the Hanovia arc the absorption of a known pressure of NO<sub>2</sub>-argon mixture in the shock tube was measured. Decadic extintion coefficients at  $300^{\circ}$ K were 164, 144 and  $29 \ {\rm M}^{-1}$  cm<sup>-1</sup> at 405, 436, and 546 mm, respectively.

High temperature extinction coefficients were calculated from the room temperature value and the initial decrease in

light intensity. The ratio  $I_0/I_1$  is obtained from 41. The ratio  $I_1/I_2$  is obtained from the observed intensity,  $I_1$ , before the shock wave arrived at the station and the extrapolated value of the intensity after the gas had reached the high temperature but before any reaction had occurred. The coefficient  $\boldsymbol{\epsilon}_2$  at the high temperature is then given by the expression:

$$\epsilon_2 = \frac{\log_{10} (I_0/I_1)(I_1/I_2)}{[NO_2]_1 \Delta_i \ \text{(53)}}$$

In the experiments with reflected shocks,  $\epsilon_2$  and  $\epsilon_r$  behind the incident and reflected waves is obtained. The expression for  $\epsilon_r$  is identical with 53 with the substitution of  $\Delta_T$  for  $\Delta_1$  and  $I_r$  for  $I_2$ . The values observed are more reliable when little reaction occurs. For more rapid reactions, the extrapolation to  $\alpha = 0$  is long and uncertain.

The extinction coefficient of NO<sub>2</sub> has been measured over the temperature range of this investigation at nominal wave lengths of 405, 436, and 546 mm. These values are given in Table 4. As previously found (16), the extinction coefficients decrease with temperature at 405 and 436 mm, but increase at 546.

## C. Results and Conclusions

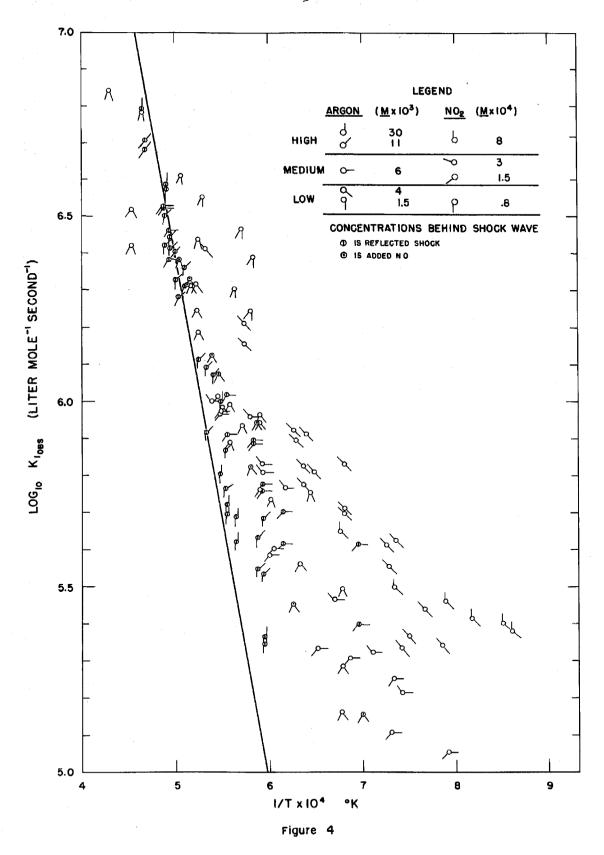
## 1. Observed Rate Constants

The principal experimental results are values of initial rate constants at various conditions. Ten groups of reactions were done in which the  $\mathrm{NO}_2$  concentration, the argon concentration, and the ratio  $[\mathrm{M}]/[\mathrm{NO}_2]$  were widely varied. The approximate conditions of each group of experiments are presented in Table 5. Since  $\Delta$  changes slowly with shock strength, the concentrations in the shocked gas vary slightly, and exact concentrations for each experiment are given in Table 6. Rate measurements of these reactions were calculated as discussed above in terms of the conventional rate constants defined below.

$$k_{1 \text{ obs}} = -\frac{1}{[NO_2][M]} \frac{d[NO_2]}{dt}$$
 (54)

$$k_2 \text{ obs} = -\frac{1}{[NO_2]^2} \frac{d[NO_2]}{dt}$$
 (55)

From Arrhenius plots of the data calculated in this way, several qualitative conclusions may be drawn. The data from experiments at the higher mole fractions of .05, .10 and .15 may be fitted to a straight line when  $k_{2~\rm obs}$  is plotted on an Arrhenius graph (figure 5). The activation energy is 23  $\pm$  4 kcal / mole, which is within the observed



OBSERVED BIMOLECULAR RATE CONSTANTS

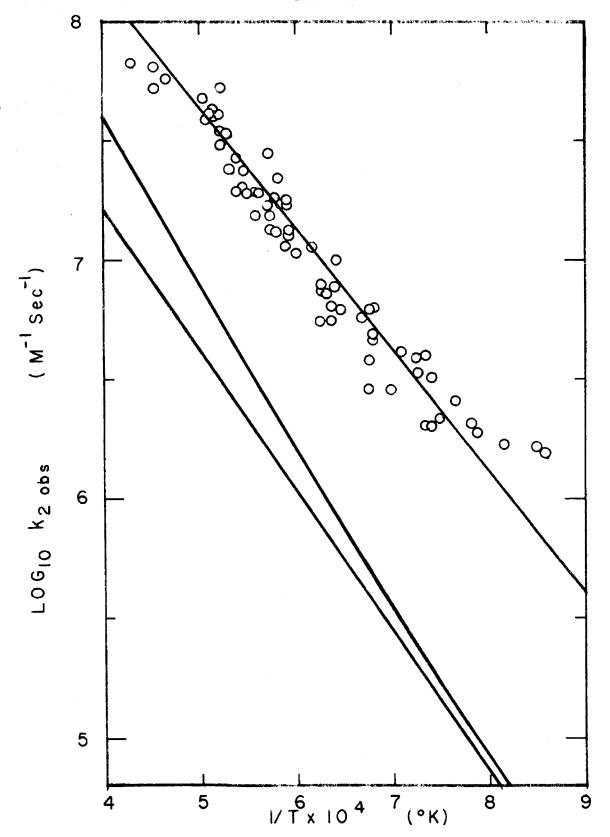


Figure 5. Observed Rate Constants for High NO<sub>2</sub> Concentrations Lower two lines are extrapolations of low temperature results

Bodenstein activation energy of 26.6 kcal / mole (1). However, the observed rate constants are about twelve times higher than the constants predicted from a straight line extrapolation of the Bodenstein and Ramstetter (1) and Rosser and Wise (5) results to temperatures of this investigation. For example, at  $1667^{\circ}$ K,  $\log_{10}$  k<sub>2 obs</sub> is 7.10, while the extrapolated value is 6.03, where the constants are in the units M-1 sec-1. If data from the four lowest NO2 mole fraction groups are calculated as k2 obs and plotted, the results do not fall on the straight line shown in figure 5, but are too high. At  $2000^{\circ}$ K, the  $k_{2 \text{ obs}}$  for the lowest  $N0_2$ concentrations are about 12 times higher than the average of the higher concentrations. It is particularly significant that the 2.8 x 10<sup>-3</sup> mole fraction mixture rate constants are higher than the  $7 \times 10^{-3}$  mixtures. The NO<sub>2</sub> concentration is the same in both cases, while the argon concentration is three times greater in the latter group. This result suggests a path dependent on the argon or total gas concentration.

The Arrhenius plot of  $\log k_{1 \text{ obs}}$  (figure 4) seems to apply to all the data much better. In particular, the points of lower  $NO_2$  concentrations near  $2000^{\circ}K$  seem well established. The highest activation energy observed was 57 kcal/mole for the 2.8 x  $10^{-3}$  mole fraction points. The points at lower  $[M]/[NO_2]$  ratios have lower activation energies, and many groups at higher  $[NO_2]$  clearly fall

above the best line through the lower [NO<sub>2</sub>] results. Qualitative observations of this sort indicate that more than one process is occurring under these conditions. It should also be pointed out that additions of .043 mole fraction NO to experiments containing .050 mole fraction NO<sub>2</sub> did not affect the rate, as shown in figure 4.

Values of  $k_{\rm l}$  obs as defined in 54 along with other experimental conditions for each of the ten groups of reactions are given in Table 6.

## 2. Extrapolation of Proposed Mechanisms

In this section, an attempt will be made to make the best possible extrapolation of reported rate expressions and mechanisms to the conditions of the present experiments.

The detailed extrapolation of the bimolecular NO<sub>2</sub> decomposition observed by Bodenstein and Ramstetter (1) and Rosser and Wise (5) may be carried out using the transition state theory in the manner of Herschbach, Johnston, Pitzer and Powell (4). The rate step for this process is reaction 1 previously given:

$$NO_2 + NO_2 \xrightarrow{k_b} NO + O_2 + NO$$
 (1)

The value of  $k_b$  over the total range (5) is:

$$k_b = -\frac{1}{[NO_2]^2} \frac{d[NO_2]}{dt} = 4.0 \times 10^9 \exp [-26900/RT] M^{-1} sec^{-1}$$
(56)

The extrapolation of these results to temperatures of around 2000°K of this investigation is not accurate unless the detailed temperature dependence of the pre-exponential factor in 56 is known.

Reference 4, hereafter called HJPP, calculates theoretical values of pre-exponential factors for a number of bimolecular gas phase reactions including 1. A detailed form of the

transition state theory is used, which requires all partitions functions of the reactants and the activated complex. Estimates must therefore be made of bond lengths, vibration frequencies, moments of inertia for total and internal rotation, symmetry numbers for the rotations, and ground state electronic degeneracies for the reactants and activated complex. Although in general the pre-exponential factor will vary with temperatures, it is very difficult to observe this variation in any given investigation. Accordingly, an observed pre-exponential factor A, not dependent on temperature has been obtained from the observed rate constant and experimental activation energy, E, at a given temperature from the expression below.

$$A = \frac{k}{\exp[-E/RT]}$$
 (57)

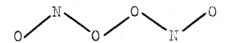
This observed pre-exponential factor may be calculated in terms of the theoretical expression:

$$k = B (T) \exp \left[-E_0/RT\right]$$
 (58)

where B is a function of temperature and  $E_0$  is not. The temperature dependent experimental activation energy E in 57 and  $E_0$  are related by the expression:

$$E_{o} = E - RT^{2} \frac{d \ln B}{dT}$$
 (59)

An important feature of the method is an approximate method of calculating moments of inertia for internal rotation. For reaction 1, HJPP have assumed a planar activated complex of the form:



The observed and calculated pre-exponential factors are  $1.8 \times 10^9$  and  $4.5 \times 10^9$   $\text{M}^{-1}$  sec<sup>-1</sup> at  $570^{\circ}$ K, using the data of Bodenstein and Ramstetter (1). The recent combined rate expression for the two investigations given by Rosser and Wise has a pre-exponential factor of  $4.0 \times 10^9$ . Either experimental value is in excellent agreement with the theoretical.

Although it would not be a good approximation to use the calculated pre-exponential value for extrapolations, it would be justifiable to use the ratio of the rate constant expression 58 at two temperatures, and the measured rate constant at one temperature, to calculate a rate constant at the upper temperature. This ratio is given by the expression:

$$\frac{k_{T_2}}{k_{T_1}} = \frac{B(T_2)}{B(T_1)} \exp\left[-\frac{E_0}{R}\left(\frac{1}{T_2} - \frac{1}{T_1}\right)\right]$$
(60)

For the transition state theory, B(T) is given by the expression:

$$B(T) = \frac{\mathbf{K} \, \mathbb{K}_{B} T}{h} \, \frac{\mathbf{Q}^{\ddagger}}{\mathbb{Q}_{A} \, \mathbb{Q}_{B}} \tag{61}$$

In this expression K is the transmission coefficient which will be assumed temperature independent,  $k_{\rm b}$  is Boltzmann's constant, h is Planck's constant, Q is the partition function for the activated complex with the degree of freedom corresponding to the reaction coordinate removed, and  $Q_{\mathbf{q}}Q_{\mathbf{p}}$ are the total partition functions for the reactants. partition functions are the product of partition functions for translational, electronic, total and internal rotational, and vibrational degrees of freedom. No upper electronic states contribute to the electronic partition function for NO2 and none are assumed for the complex, so this term in B(T) does not appear in 60. For all other motions except vibration, the high temperature expressions for the partition functions may be considered as a constant times the temperature raised to a certain power. The constants cancel from 60, and one obtains a  $T^{-1/2}$  from the temperature dependences. This exponent arises since translation contributes  $T^{-3/2}$ , total rotation contributes T-3/2, internal rotation contributes T3/2 and the frequency factor contributes T. Since not all vibrations are excited at all temperatures of this extrapolation, no simple expression holds, and the vibrational partition function  $Q_{\mathbf{w}}$  must be calculated at each  $T_2$ . With these substitutions, 60 becomes:

$$\frac{k_{T_2}}{k_{T_1}} = \left(\frac{T_1}{T_2}\right)^{1/2} \frac{Q_{v2}}{Q_{v1}} \exp\left[-\frac{E_0}{R}\left(\frac{1}{T_2} - \frac{1}{T_1}\right)\right]$$
(62)

To qualitatively understand the change of  $k_{T_2}$  with  $T_2$ , a fairly accurate approximation of 62 may be given. activated complex has been assumed planar, and all vibrations lie in the plane. The six out-of-plane motions include one translation, two total rotations, and three free internal rotations. There are twelve in-plane motions, including two translations, one total rotation, and one reaction coordinate. This leaves eight vibrational frequencies to be estimated. The estimates of six of these are obtained from comparison with the frequencies of NO2, which are included twice in the denominator of Q. The other two motions are low frequency rocking motions of large groups in the complex and give large contributions to the partition function. These estimated frequencies are 350 and 250 cm<sup>-1</sup>. If the six NO<sub>2</sub> frequencies are allowed to cancel the six largest complex frequencies and the fully excited approximation to the partition function  $k_h T/h \eta$  is substituted for the two low frequencies, the expression becomes:

$$\frac{k_{T_2}}{k_{T_1}} = \left(\frac{T_2}{T_1}\right)^{3/2} \exp\left[-\frac{E_0}{R}\left(\frac{1}{T_2} - \frac{1}{T_1}\right)\right] \tag{63}$$

The Arrhenius plot should therefore show an upward curvature as the temperature increases.

The extrapolation was made from the exact expression, 62, between 570°K, the temperature used by HJPF, and 2500°K using the combined rate constant given by 56. This extra-

polation is shown on figure 5. At 1667°K, E° is found by 59 to be 25.9 kcal/mole compared to 26.9 kcal/mole for E. Moreover, the curve is very sensitive to changes in E. The  $\mathbf{E}_{\mathbf{o}}$  necessary to connect the average shock tube results with 56 at 570°K is 29.3 kcal/mole. While the activation energy is usually not accurately known, this difference of 3.4 kilocalories between the observed value and the value necessary to fit the high temperatures results does seem well outside the experimental uncertainty in the present To obtain the same agreement between measured and calculated partition functions at 570°K, the factor B(T) associated with an  $E_0$  of 29.3 kilocalories would have to be twenty times greater than the B(T) previously calculated. This factor would seem also somewhat larger than could be obtained by refining the HJPP estimates of parameters. extrapolation is discussed further in the next section after an analysis of the experimental data obtained in the present work.

Another mechanism giving a rate expression with a quadratic dependence on the NO<sub>2</sub> concentration is the Ashmore and Levitt (6) mechanism shown below, which postulates NO<sub>3</sub> as an unstable intermediate.

$$NO_2 + NO_2 \xrightarrow{k_2} NO_3 + NO$$
 (2)

$$NO_3 + NO \xrightarrow{k_3} NO_2 + NO_2$$
 (3)

$$NO_3 + NO_2 \xrightarrow{k_{1}} NO_2 + O_2 + NO$$
 (4)

The rate expression for this mechanism is:

$$-\frac{1}{[NO_2]^2}\frac{d[NO_2]}{dt} = \frac{2 k_2}{1 + k_3 [NO]/k_4 [NO_2]}$$

This mechanism is inhibited by NO, either added initially or produced in the reaction, so that it only contributes to the rate during the early stages of the reaction even in pure  $NO_2$ . The bimolecular path of reaction 1 is, of course, continuing to occur. At  $707^{\circ}$ K, Ashmore and Levitt report  $k_b = 19.4$ ,  $k_2 = 26$  (both  $\underline{M}^{-1} \sec^{-1}$ ) and  $k_3/k_4 = 60$ . Davidson and Schott (8) give  $k_3/k_4 = 570$ . Therefore at  $707^{\circ}$ K, without NO present, initially each path contributes about the same. Both  $k_3$  and  $k_4$  are known from previous kinetics investigation on the nitrogen oxides (7). The values of the pre-exponential factors and the activation energies for  $k_3$  and  $k_4$  are reported as 6 x  $10^{10}$  and 1.5 x  $10^5$   $\underline{M}^{-1} \sec^{-1}$ , and  $1.4 \pm 2.5$  and  $3.8 \pm 1$  kcal/mole respectively.

It is difficult to predict whether a mechanism involving  ${\rm NO_3}$  is important at a temperature of  $1750^{\rm o}{\rm K}$ , an average for the present investigation. Ashmore and Levitt (8) have some evidence that the activation energy of 2 is 30 kcal/mole. The very small activation energy of 3 given by Schott and Davidson (7) suggests that the activation energy should be  $\Delta{\rm H_0}^{\rm o}$  for 2, or 23 kcal/mole. These estimates bracket the observed bimolecular activation energy, 26.9 kcal/mole, so it is possible that  ${\rm k_2}$  would be comparable with  ${\rm k_b}$  at  $1750^{\rm o}{\rm K}$ .

Using the activation energies of Schott and Davidson (7),  $k_3/k_4$  would become 20 (AL) or 190 (SD) at  $1750^{\circ} K$ . If  $k_3/k_4$  were very large, a very small amount of NC would completely inhibit the mechanism. If  $k_3/k_4$  were very small, it might prove impossible at certain temperatures to observe the inhibition in the shock tube even with all the argon replaced by NO. In figure 4 are presented values of  $k_2$  obs for gas mixtures containing .050 mole fraction NO<sub>2</sub> and .043 mole fraction NO in argon. Within the limited precision available, the same rate constants are obtained with and without added NO. Thus, the actual situation is still uncertain.

Another possibility is that a reaction faster than 4 destroys NO<sub>3</sub> at the high temperatures. The unimolecular decomposition of NO<sub>3</sub> at the low pressure limit may be represented by:

$$NO_3 + M \xrightarrow{k_d} NO_2 + O + M$$
 (64)

The total reaction would then involve 10, the rapid reaction of 0 and  $NO_2$ , as the final step. An estimate of  $k_d$  may be made from the known thermodynamic functions of  $NO_3$  (7) and the rate of the reverse reaction, which has recently been measured by Ford and Endow (23). At  $298^{\circ}$ K, the equilibrium constant for 64,  $K_c$ , is  $4.5 \times 10^{-31}$  M. This value may be extrapolated to high temperatures by using the expression

below for equilibrium constants in terms of partition functions, Q.

$$\frac{K_{c_2}}{K_{c_1}} = \left[ \left( \frac{Q_{NO_2}Q_0}{Q_{NO_3}} \right)_2 / \left( \frac{Q_{NO_2}Q_0}{Q_{NO_3}} \right)_1 \right] \exp \left[ -\frac{\Delta E_0}{R} \left( \frac{1}{T_2} - \frac{1}{T_1} \right) \right]$$
(65)

The rotational temperature dependence will cancel, since there are three rotational degrees of freedom in both NO<sub>3</sub> and NO<sub>2</sub>. The six vibrations of NO<sub>3</sub> may be classified as three stretches, two bends, and one out-of-plane vibration. The vibrations of NO<sub>2</sub> consist of two stretches and one bend. If it is assumed that the stretches make small contributions, that one bend may be cancelled in NO<sub>2</sub> and NO<sub>3</sub>, and that the other two vibrations of NO<sub>3</sub> are classical, the total contribution from vibrations is T<sup>-2</sup>. Therefore, 65 may be written:

$$\frac{K_{c_2}}{K_{c_1}} = \left(\frac{T_1}{T_2}\right)^{1/2} \exp\left[-\frac{\Delta E_0^{\circ}}{R}\left(\frac{1}{T_2} - \frac{1}{T_1}\right)\right] \tag{66}$$

If  $\Delta E^{\circ}_{298} = 49.6$  kcal/mole is used for  $\Delta E^{\circ}_{0}$ ,  $K_{c}$  at 1750°K is .29. Ford and Endow report  $k_{r} = 1.0 \times 10^{11}$  M<sup>-2</sup> sec<sup>-1</sup> at 298°K. Reactions of this type are expected to have a temperature dependence of approximately T<sup>-1</sup> to T<sup>-2</sup>, and in the present case T<sup>-3/2</sup> was used. Therefore,  $k_{r}$  at 1750°K is 7.0 x 10<sup>9</sup> M<sup>-2</sup>sec<sup>-1</sup>, and  $k_{d}$  is 2.0 x 10<sup>9</sup> M<sup>-1</sup> sec<sup>-1</sup>.

If 64 replaces 4 in the Ashmore and Levitt mechanism, the rate expression is:

$$-\frac{1}{[NO_2]^2} \frac{d[NO_2]}{dt} = \frac{2 k_2}{1 + k_3[NO]/k_d[M]}$$
(67)

From the expression given by Schott and Davidson (7),  $k_3 = l_1 \times 10^{10} \, \text{M}^{-1} \text{sec}^{-1}$  at  $1750^{\circ} \text{K}$ . Using the values of [NO] and [M] present in the inhibition experiments, one obtains  $k_3$  [NO] =  $l_1 \times 10^6 \, \text{sec}^{-1}$  and  $l_2 \times 10^6 \, \text{sec}^{-1}$  or  $l_3 \times 10^6 \, \text{kg}$  [NO]/ $l_3 \times 10^6 \, \text{may}$  indeed become important at high temperatures. The inhibition by NO would not be observed at temperatures higher than 1750, since  $l_3 \times 10^6 \, \text{kg}$  has about 50 kcal/mole activation energy, while  $l_3 \times 10^6 \, \text{kg}$  kcal/mole. The rate expression 67 would then become identical with the simple bimolecular process and demonstration of this path would be quite difficult in the absence of information from lower temperatures about  $l_2 \times 10^6 \, \text{kg}$ .

Yet another process which may cause the thermal decomposition of NO<sub>2</sub> at high temperature is the unimolecular decomposition, and the standard mechanism of this type is presented below.

$$NO_2 + M \xrightarrow{k_u} NC_2 + M$$
 (68)  
 $NO_2^* + M \xrightarrow{} NO_2 + M$  (69)  
 $NO_2^* \xrightarrow{} NO + O$  (70)  
 $O + NO_2 \xrightarrow{} O_2 + NO$  (71)

The first three reactions represent the unimolecular decomposition. The last reaction completes the process and

is not rate determining. For a simple triatomic molecule like NO2, theory and general experience predicts that the rate will depend on the total pressure. In other words, the overall decomposition rate will equal the rate of production of energized NO2, NO2\*. This is the same as the rate of 68, or k [NO2][M]. In these equations, M represents any gas molecule, and initially this could be either argon or NO2. The efficiencies of NO2 and argon in energizing NO2 are assumed to be equal. An energized NO2\* molecule contains enough energy to dissociate, but the energy is distributed among several degrees of freedom. When this energy by chance becomes localized in an N-O bond, the molecule breaks into NO and O as shown in 70. If the energized NO, \* experiences a successful collision with another molecule before this energy becomes localized, the excess energy is lost, and the molecule becomes NO2 as shown in 69. Since NO2 is such a simple molecule, the time before the NO2 \* will react is small, and 69 is not effective.

The overall process represented by 68, 69, and 70 may be expressed by 9:

$$NO_2 + M = NO + O + M$$
 (9)

The rate of 9 may be estimated from the recent measurements of the rate of the reverse reaction by Ford and Endow (23), an estimation of its temperature coefficient, and the

equilibrium constant of 9. The temperature coefficient of the reverse reaction may be estimated from the temperature dependence of the equilibrium constant and the rate of the forward reaction. The equilibrium constants at two temperatures are related by 65, if  $Q_{\rm NO}Q_0/Q_{\rm NO}_2$  is the partition function quotient. Translation contributes  $T^{3/2}$ , rotation contributes  $T^{-1/2}$ , and one bending vibration contributes  $T^{-1}$  to the temperature dependence. Therefore the quotient has no temperature dependence. The forward unimolecular rate constant may be approximated by:

$$k_{u} = \frac{Z}{(s-1)!} \begin{pmatrix} E_{o} \\ \overline{RT} \end{pmatrix} \quad \exp \left[ -\frac{E_{o}}{RT} \right]$$
 (72)

This expression is given by the classical Rice, Ramsperger, Kassel theory, where Z is the collision number and s is the number of effective oscillators—classically 3(number of atoms) minus 6. In the present case s is three and the pre-exponential factor in the above equation has a  $T^{-3/2}$  temperature dependence. It is known that the reverse of 9 has little activation energy, so  $E_{\rm o}$  in 72 and  $\Delta E_{\rm o}^{\rm o}$  in 65 must be approximately equal. Since the ratio of the forward to the reverse rate constant is the equilibrium constant, the reverse rate constant will have only a  $T^{-3/2}$  dependence on the temperature. Arguments of this type justify the temperature dependence assumed for the reverse of 64 above.

Ford and Endow give the rate constant for the reverse

of 9 as 1.8 x  $10^{10}$   $\text{M}^{-2}$ sec<sup>-1</sup> at  $300^{\circ}$ K with N<sub>2</sub> as the "third body" M. Assuming that argon is about one-half as effective as  $N_2$ , the constant becomes 1.0 x  $10^{10}$   $M^{-2}$  sec<sup>-1</sup>. Using the  $T^{-3/2}$  temperature dependence derived above, the rate constant is  $4.1 \times 10^8$  and  $5.8 \times 10^8 \text{ M}^{-2} \text{sec}^{-1}$  at 2500 and 2000°K, respectively. The equilibrium constant for 9, [NO][0]/[NO2], may be calculated from standard thermodynamic information (20), (21), (22). It is found to be 3.83 x  $10^{-2}$  M and 1.15 x  $10^{-3}$  M at 2500 and 2000 K, respectively. Therefore the rate constants  $k_1$  are 3.2 x 10<sup>7</sup> and 1.3 x 10<sup>6</sup>  $\underline{M}^{-1}$  sec<sup>-1</sup> at 2500 and 2000°K, where the values calculated as indicated above have been multiplied by two because k obs has been defined, 54, for the decomposition of two NO2 molecules per reaction. The values of  $k_{1 \text{ obs}}$  at 2500 and 2000 $^{\circ}$ K are  $4.4 \times 10^7$  and  $2.6 \times 10^6 \, \text{M}^{-1} \text{sec}^{-1}$  in good agreement with the extrapolation. Therefore, it is not unreasonable to assume that the rate constants measured at the higher temperatures of this investigation are due mainly to a unimolecular reaction.

The local activation energy of the unimolecular reaction 9 may be estimated from the  $T^{-3/2}$  temperature dependence of the pre-exponential factor. The energy  $E_0$  in 76 is taken as  $\Delta H_0^0$  of reaction 9 or 71.381 kcal/mole (22). The predicted local activation energy,  $E_0$ , is given by 59. In the present case 59 becomes  $E_0 = E_0 - (3/2)RT$ , and therefore around 2000°K,  $E_0$  is 65.4 kcal/mole. This estimate will be used in the analysis of the rate data to be presented in the next section.

## 3. Interpretations and Comparisons

This section will describe an analysis of the observed rate constants that indicates the Bodenstein bimolecular decomposition and a unimolecular process are both occurring. Also, the results of this investigation will be compared with the results of the Steinburg and Lyon (9) investigation.

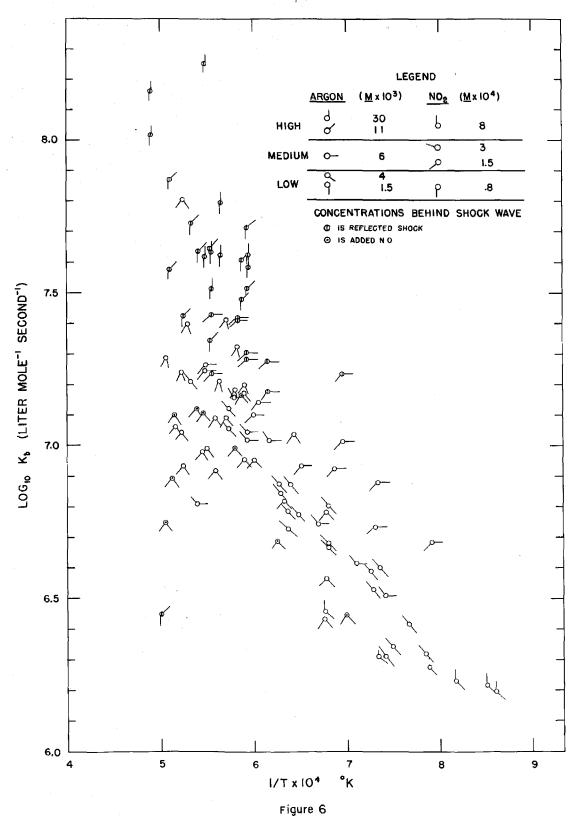
The analysis of observed rate constants into a bimolecular contribution  $\mathbf{k}_{\mathrm{b}}$  and a unimolecular contribution  $\mathbf{k}_{\mathrm{u}}$  was accomplished by subtracting an estimated value of  $\mathbf{k}_{\mathrm{u}}$  from the observed rate constant  $\mathbf{k}_{\mathrm{l}}$  obs (figure 4). The estimation of the local activation energy E to be 65.4 kcal/mole around 2000°K was discussed in the last section. Since one value of  $\mathbf{k}_{\mathrm{u}}$  must be known in addition to the local activation energy, it was judged most reasonable to draw several lines of 65.4 kcal/mole activation energy, and compare the  $\mathbf{k}_{\mathrm{b}}$  values obtained. These lines were drawn almost through the results for low NO2 concentrations at around 2000°K. The bimolecular rate constant was determined from the expression:

$$k_{b} = \frac{[M]_{1}}{[NO_{2}]_{1}} \left[ k_{1 \text{ obs}} - k_{u} \right]$$
 (73)

The best rate expression found was  $k_u = 3.06 \times 10^{13} \, \mathrm{exp}$  [ -65400/RT]  $\underline{\mathrm{M}}^{-1} \mathrm{sec}^{-1}$ , and it is shown in figure 4. The large slope of this line means that the rate constants are greatly affected at high temperatures and not changed at all at lower temperatures by this analysis. The Arrhenius plot

of log  $k_b$ , determined by 73, versus reciprocal temperature is shown in figure 6. As might be expected, the scatter at the higher temperatures is much greater than at the low temperatures. However, the significant point is that the groups with low  $NO_2$  mole fractions of 2.8 x  $10^{-3}$ , 7 x  $10^{-3}$  and 2.3 x  $10^{-2}$  are now much better represented on a single line. The experimental activation energy of figure 6 is  $22 \pm 6$  kcal/mole. Comparison of figure 5 and figure 6 show that the higher  $NO_2$  concentration results are not affected much. The extrapolation of the bimolecular path using experimentally determined quantities and the transition state theory is still almost eight times too low. Also, the extrapolated and observed values are in poor agreement at low temperatures.

The agreement between observed and extrapolated  $k_{\rm b}$  values might be improved if more information were available about the Ashmore and Levitt mechanism (6). At the present time, values have only been published for one temperature. The activation energy of 2 is needed, and measurements of the unimolecular decomposition of NO<sub>3</sub> might prove very significant. Because only one set of NO inhibition experiments were performed and because the extrapolation of  $k_3/k_4$  is quite uncertain, the inhibition experiments should not be interpreted as ruling out the Ashmore and Levitt mechanism. Experiments with a small amount of NO<sub>2</sub> in NO as the buffer gas between 1100 and 1500°K would give probably



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the greatest chance of observing inhibition by NO.

As previously noted, the results of Steinburg and Lyon (9) on the same system over the same temperature range are somewhat different. They find all their data may be accounted for by the rate expression:

$$k_{SL} = -\frac{1}{[NO_2][A]} \frac{d[NO_2]}{dt}$$

$$= 3.82 \times 10^{11} \exp [-\frac{1}{6}100/RT] \, \text{M}^{-1} \text{sec}^{-1}$$
(74)

Near  $2000^{\circ}$ K the results are in agreement. The expression above gives  $k_{\rm SL}=3.4\times10^6~{\rm M}^{-1}{\rm sec}^{-1}$ . At lower temperatures, the larger NO<sub>2</sub> concentration experiments definitely fall above the Steinburg and Lyon expression. Values of  $k_{\rm SL}$  were obtained from an integrated form of 74. In the present investigation it was felt that density and temperature changes, with the resultant changes in the rate constant and extinction coefficient, would make integrated expressions less certain than initial expressions. These objections are admittedly less important at low NO<sub>2</sub> mole fractions of .01 to .03 used by Steinburg and Lyon.

The following mechanism was proposed by Steinburg and Lyon.

$$NO_2 + A \xrightarrow{k_5} NO_2^* + A \tag{5}$$

$$NO_2 + A \xrightarrow{k_6} NO + C + A$$
 (6)

$$NO_2^* + A \xrightarrow{k_7} NO_2 + A + hv$$
 (7)

$$NO_2 + O \xrightarrow{k_8} NO + O_2 \tag{8}$$

If  $\mathrm{NO_2}^*$  and 0 are present in steady state concentrations and  $\mathrm{k_6}$   $\mathrm{k_7}$ , the mechanism above gives the concentration dependence of 74. The experimental justification for 7 is stated to be the fact that the light intensity is proportional to the product  $[\mathrm{NO_2}][\mathrm{A}]$ . Since an activation energy of 46 kcal/mole is observed, it is believed that 9--which requires about 71 kcal/mole--is not occurring.

The Steinburg and Lyon mechanism is difficult to justify physically. Since about 71 kcal/mole must be involved in going from the reactants of 5 to the products of 6, reaction 6 must have an activation energy of at least 25 kcal/mole if 5 has a 46 kcal/mole activation energy. This additional energy comes from another collision with argon, as shown in reaction 6. It must be postulated that the collision is much more likely to give 25 kcal/mole more energy to the NO<sub>2</sub>\* than it is to remove the excess 46 kcal/mole present in the molecule, i.e. to reverse 5. This possibility seems unlikely from previous experience.

The observation of a single activation energy equal to 46 kcal/mole is not supported by the present experiments. Steinburg and Lyon investigated the reaction over an  $[argon]/[NO_2]$  ratio of three and an argon pressure ratio of

two. The present study included their conditions but with ranges of sixty-five and twenty for the above quantities. It is clear that the observed activation energy changes with conditions, and in experiments designed to favor the unimolecular process, a measured activation energy of 57 kcal/mole was observed in this study. The results presented here would indicate that both the bimolecular and unimolecular processes were occurring in the Steinburg and Lyon experiments, and therefore an activation energy intermediate between 25.9 and 71 kcal/mole would be observed.

In summary, then, it is believed that the most reasonable interpretation of the shock tube experiments, taking into account the experimental data, extrapolation of other results, and general theoretical considerations, is that NO<sub>2</sub> is decomposing by two paths. One is the unimolecular decomposition of NO<sub>2</sub> into NO and O with a rate law - d[NO<sub>2</sub>]/dt =  $k_u$ [NO<sub>2</sub>][M], and an activation energy of about 65 kcal/mole. The second is a bimolecular decomposition, - d[NO<sub>2</sub>]/dt = k[NO<sub>2</sub>]<sup>2</sup>, with an activation energy of 22  $\pm$  6 kcal/mole. However, the limited precision of the shock tube work makes it impossible to definitely prove that the above interpretations are correct.

The observed bimolecular rate constants are greater by a factor of eight than extrapolated values for the bimolecular Bodenstein mechanism. It seems unlikely, but not entirely excluded, that this is due to an error in the extrapolation. Possibly the Ashmore and Levitt mechanism, or a simple extension thereof (including reaction 64), can account for the additional reaction path. Possibly there is some other as yet unrecognized reaction path. Possibly the discrepancy is in the present work. This question requires further work, but the present investigation has fairly definitely established the occurrence of both unimolecular and bimolecular reaction paths.

## D. Tables

Table 1. <u>Gas Parameters for Argon behind Reflected Shock</u>
Waves

 $T_1 = 300.00^{\circ}K$ ; Data for incident shocks taken from reference (19)

$\frac{s_{i}}{a_{i}}$		<u> </u>	Si (cm/msec)	T <sub>2</sub> (°K)
1.80 2.00 2.20 2.40 2.60 2.80 3.00 3.20 3.40	3.80000 4.75000 5.80000 6.95000 8.20000 9.55000 11.00000 12.55000	2.07692 2.28571 2.46939 2.63014 2.77049 2.89299 3.00000 3.09366 3.17582	58.059 64.510 70.961 77.412 83.863 90.314 96.765 103.216	548.9 623.4 704.6 792.7 887.9 990.3 1100.0 1217.0

S <sub>r</sub> (cm/msec)	$\Delta_r$	$\Theta_{r}$	$\Delta_{ m t}$	Tr (°K)
37.989 40.319 42.811 45.426 48.134 50.917 53.758 56.648 59.577	1.79245 1.90000 1.98630 2.05621 2.11340 2.16063 2.20000 2.23310 2.26115	1.55925 1.65414 1.73638 1.80764 1.86941 1.92304 1.96970 2.01040 2.04603	3.72278 4.34285 4.90495 5.40812 5.85515 6.25068 6.60000 6.90845 7.18101	855.9 1031.3 1223.5 1433.0 1659.9 1904.4 2146.7 2446.7

Table 2. Gas Parameters behind Incident Shocks for
Mixtures of Mitrogen Oxides and Argon

 $T_1 = 300.00^{\circ}$ K; Calculations made for first sample of a given composition; Other samples within 1%

Mole Fraction NO<sub>2</sub> =  $5.03 \times 10^{-2}$ ; Initial pressure = 0.02 atm

T <sub>2</sub> (°K)	Πi	<u> </u>	i (cm/msec)
	<b>d</b> <sub>2</sub> = 0		
1000 1500 2000 2500	10.395 17.705 25.082 32.482	3.1185 3.5410 3.7623 3.8979	92.55 120.1 142.6 162.0
	<b>x</b> <sub>2</sub> = 0	.50	
1000 1500 2000 2500	11.4977 18.7861 26.1487 33.4989	3.14063 3.7106 3.8699 3.9700	95.96 122.8 145.0 164.1

Mole Fraction  $NO_2 = 5.03 \times 10^{-2}$ ; Initial pressure = 0.04 atm

T <sub>2</sub> (°K)	<u> Ti</u>		S <sub>i</sub> (cm/msec)
Baseline Control of Co	<b>d</b> <sub>2</sub>	= 0	
1000 1500 2000 2500	10.412 17.721 25.095 32.497	3·1240 3·5436 3·7636 3·8997	92.62 120.2 142.6 162.0
	<b>∝</b> <sub>2</sub>	= .50	
1000 1500 2000 2500	11.5137 18.8023 26.1647 33.5151	3.4111 3.7136 3.8758 3.9717	96.01 122.9 145.0 164.1

Table 2. (continued)

Mole Fraction  $NO_2 = 1.068 \times 10^{-1}$ ; Initial pressure = 0.02 atm

T <sub>2</sub> (°K)	πί	$\Delta_{i}$	S <sub>i</sub> (cm/msec)
	<b>d</b> <sub>2</sub> = 0		
1000 1500 2000 2500	11.2453 19.3202 27.5077 35.7466	3·3738 3·8640 4·1254 4·2900	94.60 123.2 146.6 166.9
	<b>d</b> <sub>2</sub> = 0	•50	
1000 1500 2000 2500	13.5908 21.6126 29.7281 37.8961	3.9709 4.2101 4.3432 4.4290	101.7 128.9 151.4 171.1

Mole Fraction  $NO_2 = 1.068 \times 10^{-1}$ ; Initial pressure = .010 atm

T <sub>2</sub> (°K)	Πi	$\Delta_{i}$	$S_{i}$ (cm/msec)
	<b>d</b> <sub>2</sub> = 0	·	
1000 1500 2000 2500	11.2098 19.2843 27.4716 35.7105	3.3630 3.8569 4.1208 4.2854	94.49 123.15 146.6 166.8
	<b>∠</b> <sub>2</sub> = 0	•50	
1000 1500 2000 2500	13.5551 21.5766 29.6920 37.8599	3.9608 4.2032 4.3380 4.4251	101.6 128.8 151.4 171.0

Table 2. (continued)

Mole Fraction  $NO_2 = 2.35 \times 10^{-2}$ ; Initial pressure = 0.04 atm

T <sub>2</sub> (°K)	πi	i	S <sub>i</sub> (cm/msec)		
	<b>«</b> 2 = 0	)			
600 1000 1500 2000 2500	4.5639 10.0117 16.9586 23.9972 30.9524	2.2821 3.0035 3.3917 3.5920 3.7145	62.83 91.69 118.7 140.7 159.7		
<b>≈</b> <sub>2</sub> = 0.50					
600 1000 1500 2000 2500	5.0579 10.5222 17.4593 24.4324 31.4218	2.5141 3.1382 3.4714 3.6433 3.7485	64.75 93.26 119.9 141.8 160.7		

Mole Fraction  $NO_2 = 1.527 \times 10^{-1}$ ; Initial pressure = 0.03 atm

T (OK)	Πi	i	S <sub>i</sub> (cm/msec)
	<b>«</b> 2	= 0	
900 1200 1500	10.2992 15.4555 20.7015	3 • l4331 3 • 8639 14 • 114014	89.53 109.10 125.9
	<b>«</b> 2	= 0.50	
900 1200 1500	13 • 73 56 18 • 8744 24 • 0852	4.4101 4.5450 4.6399	100.26 118.26 134.02

Table 2. (continued)

Mole Fraction NO =  $4.30 \times 10^{-2}$ ; Initial pressure = 0.020 atm Mole Fraction NO<sub>2</sub> =  $5.00 \times 10^{-2}$ 

T <sub>2</sub> (°K)	$\pi_{i}$		S <sub>i</sub> (cm/msec)
Sandy and the sa	<b>A</b> <sub>2</sub> = 0		appelled and the second of the latter control of the second of the secon
1000 1500 2000 2500	10.650 18.207 25.850 33.529	3 · 1950 3 · 6413 3 · 8774 4 · 0234	93.30 121.2 144.1 163.8
	<b>~</b> <sub>2</sub> = 0	•50	
1000 1500 2000 2500	11.7448 19.2739 26.8983 34.5232	3.4800 3.8072 3.9849 4.0917	96.66 123.9 146.4 165.8

Table 3. Measured and Calculated Reflected Shock Speeds

Mole Fraction  $NO_2 = 2.38 \times 10^{-2}$ ; Initial pressure = .04 atm

Reflected Wave Speed Sr

Experiment and Scope	From S <sub>i</sub>	From trace n/msec)	
129-1	49.7	48.9	1.900
129-2	11	49.9	11
130-1	48.4	48.0	1.872
130-2	- 11	48.8	11
131-1	48.8	46.9	1.877
131-2	11	47.2	17
132-1	52.3	50.5	1.943
132-2	τŧ	50.4	11
133-1	45.5	43.9	1.807
133-2	n	44.5	11
134-1	47.7	43.6	1.860
134-2	11	46.4	11
135-1	52.4	52.1	1.947
135-2	10	50.1	17

Table 3. (continued)

Mole Fraction  $NO_2 = 7.12 \times 10^{-3}$ ; Initial pressure = .04 atm

	Reflected	Wave Speed Sr	
Experiment and	From S <sub>i</sub>	From trace	•
Scope	(cn	n/msec)	$\underline{\theta_{ m r}}$
115-1	48.4	46.8	1.870
115-2	11	47.6	11
108-1	48.6	48.0	1.876
108-2	11	47.8	11
113-1	49.8	45.1	1.899
113-2	11	48.3	11
97-1	50.3	50.0	1.911
114-1	50.6	52.2	1.916
114-2	11	51.7	tt
98 <b>-</b> 2	51.0	49.5	1.920
105-1	51.5	52.0	1.930
105-2	11	53 • 3	ŧŧ
104-1	51.8	49.2	1.936
109-1	52.2	53.0	1.94.2
109-2	11	50.7	n
112-1	52.2	52.3	1.942
112-2	ΙŤ	51.9	11
107-1	52.4	51.5	1.944
107-2	11	52.8	n
110-1	53 • 4	54.0	1.961
110-2	11	54.5	11
100-2	55•9	54.7	2.003

Table 3. (continued)

Mole Fraction  $NO_2 = 2.8 \times 10^{-3}$ ; Initial pressure = 0.1 atm

	Wave Speed S <sub>r</sub>		
Experiment and Scope	From S <sub>i</sub>	From trace	Θr
127-1 127 <b>-</b> 2	50.1	54.2 51.0	1.907
128-1 136-1 136-2	53 • 5 49 • 5	57•5 51•0 52•0	1.963 1.892
137 <b>-</b> 1 137 <b>-</b> 2	48.3	49.7 52.2	1.870
138-1 138-2	52.3 "	55.7 54.1	1.947
139 <b>-</b> 1 139 <b>-</b> 2	49.8	50.1 52.4	1.898 "

Table 4. High Temperature Extinction Coefficients of NO2

# $\lambda = 436 \text{ mu}$ ; $\epsilon = 144 \text{ M}^{-1} \text{ cm}^{-1} \text{ at } 300^{\circ} \text{ K}$

-	$\Lambda = 430 \text{ mu}$ ;	E = 144 M	cm = at 300 K	
Experiment and Scope	. Tr	€ r ( <u>M</u> -l <sub>cm</sub> -l)	<sup>T</sup> 2 (°K)	€ <sub>2</sub> (M <sup>-1</sup> cm <sup>-1</sup> )
Mole Fract:	$ion NO_2 = 2.8$	$\times 10^{-3};$	Initial pressure	= 0.10 atm
127-1 127-2 128-1 136-1 136-2 137-1 137-2 138-1 138-2 139-1	1829 2150 1775 1682 2040 1800	89 108 113 94 108 98 100 145 141 112	959 1095 938 899 1048 948	109 109 113 107 107 114 115 112 110 112
Mole Fract	ion $NO_2 = 7.1$	2 x 10 <sup>-3</sup> ;	Initial pressure	e = 0.04 atm
106-2 106-1 115-1 115-2 108-1 108-2 113-1 113-2 97-1 114-2 114-1 98-2 105-2 104-1 109-2	1300 1687 1703 1808 1848 1878 1907 1961 1988 2018	110 118 904 904 908 908 908 708 77 75	737 902 907 952 967 980 993 1016 1027	119 118 117 118 113 117 110 116 106 114 111 110 105 102 103 110 107

Table 4. (continued)

Experiment and Scope	T <sub>r</sub>	€ r 1-1cm-1)		T <sub>2</sub> (°K)	€ 2 (M <sup>-1</sup> cm <sup>-1</sup> )
112-1 112-2 107-2 107-1 110-2 110-1 100-2	2025 2047 1138 2388	89 102 97 81 81 70 134		1043 1053 1090 1192	110 113 113 110 112 110 81
Mole Fraction N	0 <sub>2</sub> = 2.38 2	10 <sup>-2</sup> ; In	nitial	pressure	0.019 atm
129-2 129-1 130-2 130-1 131-2 131-1 132-2 133-1 133-1 134-1 135-1	1809 1689 1716 2030 1439 1630 2048	104 97 102 104 106 104 86 113 107 104 94		952 902 913 1045 796 876 1052	120 115 121 120 123 119 110 113 125 120 124 118 115

Table 4. (continued)

Experiment and Scope	<sup>T</sup> 2 <u>(°K)</u>	€ <sub>2</sub> ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )	E: <u>a:</u>	xperiment nd Scope	T <sub>2</sub>	€ <sub>2</sub> ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )
Mole Fracti	on NO <sub>2</sub>	$= 2.34 \times 10$	<b>-</b> 2;	Initial	pressure	= 0.04 atm
68-2 70-2 71-2 72-2 92-2	1262 1828 1667 1370 1535	105 80 87 102 98		93-2 94-2 95-2 96-2	1366 1652 1827 1459	109 96 85 103
Mole Fracti	on NO <sub>2</sub>	= 5.04 x 10	<b>-</b> 2;	Initial	pressure	= 0.02 atm
2-1 3-1 6-1 10-1 11-1	1520 1580 1910 1477 1694	99 102 79 100 94		13-1 14-1 17-1 21-1	1916 1750 2209 1790	84 90 87 93
Mole Fracti	on NO <sub>2</sub>	= 5.00 x 10 = 4.30 x 10	-2; -2;	Initial	pressure	= 0.02 atm
117-2 118-2 119-2 121-2 122-2	1726 1830 1985 1598 1431	95 87 74 101 104		123-2 124-2 125-2 126-2	1707 1858 1952 1942	95 88 73 77
Mole Fracti	on NO2	= 5.09 x 10	-2;	Initial	pressure	= 0.04 atm
34-1 35-1 36-1	1727 1621 1689	91 96 91		37 <b>-</b> 1 38-1	1497 1858	61 85
Mole Fracti	on NO <sub>2</sub>	= 1.05 x 10	-1;	Initial	pressure	= 0.01 atm
76-2 77-2 79-2 81-2	2324 2150 1726 1750	51 74 89 93		82-2 84-2 90-2 91-2	1719 1777 1890 1976	91 91 83 86

Table 4. (continued)

Experiment and Scope		(M Cm )	Experiment and Scope		€ <sub>2</sub> (M <sup>-1</sup> cm <sup>-1</sup> )
Mole Fracti		= 1.06 x 10			e = 0.02 atm
43-1 44-1 45-1 46-1 47-2 49-2 50-2 51-2	1471 1570 1143 1335 1471 1598 1277 1591 1360	99 96 108 103 100 95 107 96	52-2 53-2 554-2 557-2 558-2 569-2 89-2	1564 1748 1748 1544 1303 1349 1375 1380	102 91 94 102 102 104 103 106 79
	<b>\( \)</b> = 40	5 mµ;	164 <u>M</u> -1cm-1 ε	it 300°	K
Experiment and Scope	T <sub>2</sub>	€ 2 ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )	Experiment and Scope	T <sub>2</sub>	€ 2 ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )
			and beope	( <u>w</u> )	
Mole Fract		= 5.04 x 10	_		e = 0.02 atm

Table 4. (continued)

Experiment and Scope	<sup>T</sup> 2 ( <sup>o</sup> K)	<b>€</b> 2 ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup>	<u>l</u> )	Experimenand Scope	t <sup>T</sup> 2	€ 2 ( <u>M</u> -1 <sub>cm</sub> -1	)
Mole Fract	ion NO2	= 5.09 2	x 10 <sup>-2</sup> ;	; Initial	pressure	= 0.04	a tm
31-2 32-2 36-2	1349 1408 1689	123 125 106		39-2 40-2	123 <i>l</i> 4 123 <i>l</i> 4	123 183	
Mole Fract	ion NO <sub>2</sub>	= 1.06 :	x 10 <sup>-2</sup> ;	: Initial	pressure	= 0,02	atm
41-2 43-2	1172 1471	125 111		44-2 45-2	1570 1143	106 126	
	<b>\( =</b> 546	т <b>и</b> ;	<b>E</b> = 29	<u>M</u> -1 <sub>cm</sub> -1 a	t 300 <sup>0</sup> K		
•	ſП	€ 2			m	<b>6</b> 2	

Experiment and Scope	T <sub>2</sub>	€ 2 ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )	Experiment and Scope	T <sub>2</sub>	<b>€</b> 2 ( <u>M</u> <sup>-1</sup> cm <sup>-1</sup> )
146-2 147-2 148-2 149-2	1053 1224 1364 1478	56 63 60 60	150-2 151-2 152-2	1269 1162 1176	62 55 57

Table 5. Range of Experimental Conditions

[M] [NO <sub>2</sub> ]	Unshocked gas	Shocked	<u>Wave</u> region		
	Mole Fraction NO <sub>2</sub>	Pressure (atm)	$\frac{(\overline{M} \times 10^{j+})}{[NO^{5}]}$	[A] ( <u>M</u> x 10 <sup>3</sup> )	)
357	0.28	0.1	.8	30	reflected
14.3	0.7	0.04	.8	1,1	tŧ
44	2.3	0.019	1.5	6	τţ
44	2.3	0.024	1.5	6	incident
20	5.0	0.02	1.5	3	15
20	5.0	0.02	1.5	3	" (NO)
20	5.0	0.04	3	6	11
10	10	0.01	1.5	1.5	† ŧ
10	10	0.02	3	3	н
6.7	15	0.03	8	1+	1\$

Table 6. Observed Initial Rate Constants

Experiment and Scope		$[NO_2]_1 \triangle$ $(M \times 10^5)$	log k <sub>l</sub> obs (M <sup>-1</sup> sec <sup>-1</sup> )
Reflected shocks Mole fraction NO <sub>2</sub>	$= 2.66 \times 10^{-3};$	Initial	pressure = 0.10 atm
127-2 127-1 128-1	1829 2150	6.80 7.19	6.000 5.803 6.791
Reflected shocks Mole fraction NO <sub>2</sub>	$= 2.98 \times 10^{-3};$	Initial	pressure = 0.10 atm
136-2 136-1 137-2 137-1 138-2 138-1 139-2	1775 1682 2040 "1800	7:46 7:23 7:80 7:58	5.622 5.690 5.348 5.368 6.576 5.722 5.696
Reflected shocks Mole fraction NO <sub>2</sub>	$= 7.12 \times 10^{-3};$	Initial	pressure = 0.04 atm
115-2 115-1 108-2 108-1 113-2 113-1 97-1 114-1 114-2 98-2 105-1 105-2 104-1 109-2 112-2 112-2 112-1 107-2 110-1 110-2 100-2	1687 1703 1808 1848 1878 1907 1961 1988 2018 2025 2047 2138 " 2388	7:07 7:04 7:12 7:24 7:23 7:44 7:62 7:94 7:73 7:67 7:98 7:67 7:76	5.682 5.634 5.5634 5.7659 5.7659 5.9934 6.111 6.3362 6.3329 6.442 6.466.66 6.709 7.470

Table 6. (continued)

Experiment and Scope	. <del></del>	$(\underline{M} \times 10^4)$	log k <sub>l obs</sub>
Reflected shocks Mole fraction NO <sub>2</sub>	$= 2.38 \times 10^{-2};$	Initial pr	ressure = 0.019 atm
129-2 129-1 130-2 130-1 131-2 131-1 132-2 132-1 133-2 133-1 134-2 134-1 135-2	1809 1689 1716 2030 1439 1630 2048	1.17 1.07 1.15 1.16 1.00 1.11	6.019 5.911 5.759 5.777 5.887 5.893 6.381 5.615 5.701 5.618 6.526
Mole fraction $NO_2$	$= 2.34 \times 10^{-2};$	Initial pr	ressure = 0.040 atm
68-2 92-2 71-2 72-2 70-2 93-2 94-2 95-2	1262 1535 1667 1370 1828 1366 1652 1827 1459	1.25 1.32 1.33 1.28 1.38 1.38 1.35 1.32	5.051 5.337 5.587 5.107 5.969 5.251 5.601 5.971 5.307
Mole fraction NO <sub>2</sub>	$= 5.04 \times 10^{-2};$	Initial pr	ressure = 0.02 atm
3-2 4-2 6-2 6-1 10-2 10-1 11-2 11-1 13-2 13-1	1580 1660 1910 1477 1694 1916	1.47 3.51 1.65 1.55 1.46	5.562 5.732 6.436 6.190 5.494 5.284 5.762 6.246

Table 6. (continued)

Experiment and Scope	(°K)	$\frac{(\underline{M} \times 10^{4})}{}$	$\frac{\log k_{1 \text{ obs}}}{(\underline{M}^{-1} \text{ sec}^{-1})}$
14-1 17-2 17-1 21-1 21-2 24-2 25-2 26-2 27-2 28-2 29-2	1750 2209 1790 1478 1936 1558 1695 1832 1818	1.49 1.63 "1.71 1.50 1.65 1.49 1.53 1.54 1.67	5.935 6.420 6.518 5.990 5.162 6.313 5.755 6.016 5.984
Mole fraction NO	$_2 = 5.09 \times 10^{-2};$	Initial pres	sure = 0.04 atm
31-2 32-2 34-1 35-1 36-2 36-1 37-1 38-1	1349 1408 1727 1621 1689 " 1497 1858	3.66 3.17 3.01 3.02 2.96 2.94 3.12	5.215 5.323 5.959 5.767 5.831 5.807 5.469 6.001
Mole fraction NO.	$2 = 5.00 \times 10^{-2}$ = 4.30 x 10 <sup>-2</sup> ;	Initial pre	ssure = 0.02 atm
117-2 118-2 119-2 121-2 122-2 123-2 124-2 125-2 126-2	1726 1830 1985 1598 1431 1707 1858 1952	1.56 1.62 1.57 1.55 1.64 1.62 1.61 1.65 1.64	5.823 6.074 6.383 5.453 5.157 5.942 6.127 6.316 6.331
Mole fraction NO	$_2 = 1.046 \times 10^{-1}$	; Initial pro	essure = 0.01 atm
76-2 77-2 79-2 81-2 82-2	2324 2150 1726 1750 1719	1.77 1.81 1.70 1.62 1.80	6.843 6.781 6.246 6.468 6.372

Table 6. (continued)

Experiment and Scope	<sup>Т</sup> 2 <u>(°к)</u>	$[NO_2]_1 \triangle$ $(\underline{M} \times 10^4)$	$\frac{\log k}{(\underline{M}^{-1} \sec^{-1})}$
84-2 90-2 91-2	1777 1890 1976	1.76 1.64 1.79	6.302 6.552 6.611
Mole fraction N	$10_2 = 1.060 \times 1$	.0 <sup>-1</sup> ; Initial pr	ressure = 0.02 atm
43-2 43-1 44-1 44-1 46-1 47-2 49-2 51-2 553-2 557-2 557-2 557-2 557-2 557-2 557-2 557-2 557-2	1471 1570 1335 1471 1598 1277 1591 1360 1564 1748 1748 1748 1748 1379 1379 1379	3	5.698 5.698 5.767 5.889 5.938 5.938 5.938 5.939
Mole fraction N	$10_2 = 1.527 \times 1$		ressure = 0.03 atm
152-2 151-2 150-2 149-2 148-2 147-2 146-2	1176 1162 1269 1478 1364 1224 1053	7.56 x 10 7.46 x 10 7.46 x 10 7.72 x 10 7.56 x 10 7.89 x 10 7.36 x 10 6.96 x 10	5.402 5.382 5.462

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II. KINETICS OF THE FERROUS ION-OXYGEN REACTION IN SULFURIC ACID SOLUTION

This section consists of a paper published with

Professor Norman Davidson

in the Journal of the American Chemical Society
during 1956

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## Kinetics of the Ferrous Iron-Oxygen Reaction in Sulfuric Acid Solution

By Robert E. Huffman and Norman Davidson<sup>1</sup> Received May 7, 1956

The reaction  $4\text{Fe}^{\text{II}} + O_2 \rightarrow 4\text{Fe}^{\text{III}} + 2\text{H}_2\text{O}$ , at  $140\text{-}180^\circ$  in 1~F H<sub>2</sub>SO<sub>4</sub>, proceeds by simultaneous bimolecular and termolecular reaction paths:  $-\text{d}(\text{Fe}^{\text{II}})/\text{d}t = k_{\text{b}}(\text{Fe}^{\text{II}})P_{\text{O}_2} + k_{\text{t}}(\text{Fe}^{\text{II}})^2P_{\text{O}_2}$ . At  $159^\circ$ ,  $k_{\text{b}} = 1.93 \times 10^{-5}$  atm. <sup>-1</sup> sec. <sup>-1</sup>,  $k_{\text{t}} = 1.60 \times 10^{-3}~M^{-1}$  atm. <sup>-1</sup> sec. <sup>-1</sup>; the respective activation energies were measured as  $13.4~(\pm 2)$  and  $16.3~(\pm 2)$  kcal. At  $30.5^\circ$ , only the termolecular path is observed (contrary to the predictions of the high temperature activation energies);  $k_{\text{t}} = 2.78 \times 10^{-6}~M^{-1}$  atm. <sup>-1</sup> sec. <sup>-1</sup> (1~F H<sub>2</sub>SO<sub>4</sub>). The variation of rate with SO<sub>4</sub> – ( $\mu \sim 1$ , NaClO<sub>4</sub>) indicates independent  $\frac{11}{4}$ 

reactions,  $2\text{Fe}^{++} + O_2 \xrightarrow{(1/2)k_u} 2\text{Fe}^{\text{III}} + \text{H}_2\text{O}_2$ , and  $\text{FeSO}_4 + \text{Fe}^{++} + O_2 \xrightarrow{(1/2)k_s} 2\text{Fe}^{\text{III}} + \text{H}_2\text{O}_2$ , where  $k_u = 1.4 \times 10^{-6}$   $k_s = 3.1 \times 10^{-5}$   $M^{-1}$  atm.  $^{-1}$  sec.  $^{-1}$ , and  $K_{\text{FeSO}_4} = 1.1$   $M^{-1}$ . The reaction rate increases a small amount with increasing

pH. Catalysis by Cu<sup>++</sup> follows the rate law  $-d(Fe^{++})/dt = 4k_9(Fe^{II})(Cu^{++})$  and is probably initiated by  $Fe^{II} + Cu^{++} \rightarrow Fe^{III} + Cu^{I}$ . In 0.23  $FH_2SO_4$ , 0.35  $FNa_2SO_4$ ,  $k_9 = 1.9 \times 10^{-3} M^{-1} sec.^{-1}$ . The rate-determining step for the bimolecular path is presumably either: (1a)  $Fe^{II} + O_2 \rightarrow Fe^{III} + HO_2$ , or (1b)  $Fe^{II} + O_2 \rightarrow Fe^{IV} + H_2O_2$ ; for the termolecular path it is  $2Fe^{II} + O_2 \rightarrow 2Fe^{III} + H_2O_2$ . Possible detailed mechanisms are discussed. There is evidence that the bimolecular path, the termolecular path and the Cu<sup>++</sup> catalyzed path are all accelerated by complexing anions, X, and to an extent depending on the affinity of X for  $Fe^{+++}$ . Furthermore, strong complexers favor the occurrence of the bimolecular path.

The rate of oxidation of ferrous ion by molecular oxygen in acid solution is very dependent upon the nature of the anions present. The rate increases as the complexing affinity of the anion for ferric ion increases. (It is to be expected that the complexing affinity for ferrous ion would be in the same order.) Thus, at a given pH, the rate is found to decrease in the series pyrophosphate,<sup>2</sup> phosphate,<sup>3</sup>

chloride,  $^{4,5}$  sulfate and perchlorate. The rate law is  $-d(Fe^{II})/dt = 4k(Fe^{II})P_{O_2}$  for the first three media listed above and  $-d(Fe^{II})/dt = 4k(Fe^{II})^2$ .  $P_{O_2}$  for the last two. The rate-determining steps are believed to be either (1a) or (1b) for the former case, and (2) for the latter.

$$Fe^{II} + O_2 \longrightarrow Fe^{III} + HO_2$$
 (1a)

$$Fe^{II} + O_2 \longrightarrow Fe^{IV} + H_2O_2$$
 (1b)

$$Fe^{II} + O_2 + Fe^{II} \longrightarrow 2Fe^{III} + H_2O_2$$
 (2)

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Reaction (1a) is the first step in the Weiss oneelectron oxidation mechanism.<sup>8,9</sup> The reactions as written are not balanced with respect to hydrogen ion; they are intended to indicate the oxidation changes involved but not to specify the dependence of rate upon acidity. The symbol (Fe<sup>II</sup>) is defined as the formal concentration of ferrous iron; (Fe<sup>++</sup>) means the concentration of the uncomplexed ion. A similar convention is used for other atomic species.

It was thought that the bimolecular reaction (1a or 1b), which involves one of the unstable intermediates, HO<sub>2</sub> or Fe<sup>IV</sup>, would have a higher activation energy than the termolecular path (2) and would be more important at high temperatures. We have accordingly studied the ferrous iron, oxygen reaction at 140–180° in sulfuric acid. These results prompted a further investigation of the reaction in various solutions of sulfuric acid and sodium sulfate at room temperature and at ferrous iron concentrations considerably lower than those used by previous investigators. Some information on the cupric ion catalyzed reaction was also obtained.

#### Experimental

The experimental techniques for the high and low temperature reactions were different and will be described separately. The amount of ferric ion produced at given times was determined in both cases by measuring the ultraviolet absorption of the ferric sulfate complex ion<sup>10</sup> with a Beckman DU spectrophotometer.

Reagent grade ferrous ammonium sulfate, ferric ammonium sulfate, cupric sulfate and sodium sulfate were used. Sulfuric and perchloric acid solutions were prepared from concentrated reagent grade acids. Sodium perchlorate was prepared by neutralizing sodium hydroxide solutions with perchloric acid. The water used for high temperature reactions was prepared by redistilling tap distilled water from alkaline permanganate solution in a Pyrex, electrically heated still. The commercial redistilled water used in the first low temperature studies was found to contain trace amounts of copper. The water used in all results reported here at room temperature was prepared by redistilling the commercial distilled water in a Pyrex, electrically heated still to remove these traces of copper. In all cases, precautions were taken to exclude dust and to rinse vessels with the pure distilled water before preparing solutions. Tank oxygen was bubbled through water and filtered through glass wool before use.

A high temperature reaction cell consisted of an 8 cm. length of 15 mm. Pyrex tubing and, as a neck, an 11 cm. length of 5 mm. tubing. About 5 ml. of reaction solution was added, and air was displaced by a stream of  $O_2$  gas introduced through a narrow capillary. The neck was then quickly sealed off in the middle while a stream of  $O_2$  was still passing through the top of the neck.

The sealed reaction tubes were wrapped in glass wool and placed in short sections of iron pipe closed with pipe caps. The high temperatures were provided by a silicone oil-bath, and temperature control was by means of a mercury thermoregulator. The iron pipes containing the reaction cells were attached to a chain and sprocket wheel arrangement which rotated the iron pipes end over end in the bath, thus stirring the reaction tubes and the bath. The bath was allowed to heat up about 15° above the controlled temperature just before placing the stirrer and iron pipes therein. This reduced the time necessary to bring the reaction cells up to the high temperature. At the end of a reaction period, usually two hours, the reaction was quenched by cooling the pipes rapidly in cold water. The reaction tubes were placed in a one cm. Beckman cell holder drilled out to

hold the cylindrical tubes. The absorption spectrum of the iron (III)—sulfate system is dependent upon temperature. Optical density measurements between 340 and 410 m $\mu$  were made using a cell compartment thermostated at 33°. As compared to flat faced cells, the blank optical densities of the tubular reaction cells containing either 1 F sulfuric acid or water were about 0.180 to 0.080, depending on the wave length. Rough values for the effective extinction coefficient,  $\epsilon l$  in the expression  $D=\epsilon d$  are 1300, 200 and 36 at wave lengths of 340, 375 and 400 m $\mu$ , respectively. The reaction cells were calibrated after each reaction by measuring the absorption spectra of ferric ammonium sulfate solutions in the same sulfuric acid medium. We are indebted to Mr. John Andelin who constructed the high temperature bath and made a few preliminary runs.

The room temperature reactions, which were very slow, were carried out in Pyrex absorption cells, 5 cm. in diameter by 10 cm. long, with Corex windows. It was possible to make measurements at 310 m $\mu$ , where the complex has its maximum absorption. The cells had a total volume of 150–175 ml., and about 100 ml. of solution was used. Oxygen was added and the cells sealed as described above. The absorption cells were rotated slowly in a water-bath at 30.5°. At intervals of several hours, they were removed for optical density measurements and then replaced in the bath.

In both temperature ranges, the pressure or partial pressure of oxygen was essentially constant because there was a sufficiently large gas space above the solution.

Special care was taken to remove dust particles and traces of iron salts from the reaction vessels. The inside of the vessel was washed with hot aqua regia or nitric acid, thoroughly rinsed with distilled water, dried in an oven, and then protected from dust until the reaction solution was placed in it.

#### Results

Effects of Fe<sup>II</sup> and Fe<sup>III</sup> Concentrations. (a) High Temperatures.—In the range 140–180°, at ferrous ion formal concentrations between 0.00100 and 0.0250 F, the oxygenation was found to proceed by two independent reaction paths—one first order in ferrous ion and in oxygen, and one second order in ferrous ion and first order in oxygen—that is, according to the rate law

$$-\frac{\mathrm{d} \ln (\mathrm{Fe^{II}})}{\mathrm{d}t} = k_b P_{O_2} + k_t (\mathrm{Fe^{II}}) P_{O_2}$$
 (3)

where  $k_b$  and  $k_t$  may be functions of the sulfate and hydrogen ion concentrations as well. This rate law accounts for the change in rate during the course of a reaction and for the variation of initial rate with initial concentration. Added Fe<sup>III</sup> does not affect the rate.

Since the oxygen pressure remains constant during a reaction, it would be expected that plots of  $\log (Fe^{II})_i/(Fe^{II})_t$  vs. t would be linear for a first-order dependence on ferrous ion.  $(Fe^{II})_i$  and  $(Fe^{II})_t$  are the ferrous ion concentrations initially and at time t. Figure 1 shows that these plots are concave downward. However, plots of  $1/(Fe^{II})$  vs. t are concave upward.

The constants  $k_b$  and  $k_t$  were evaluated as follows. An apparent first-order rate constant, k', is defined by

$$k' = \frac{-\ln(\text{Fe}^{\text{II}})_{t_2}/(\text{Fe}^{\text{II}})_{t_1}}{t_2 - t_1}$$

for various times of reaction, where the interval between  $t_2$  and  $t_1$  is 1 hr. According to (3)

$$k' = k_b P_{O_2} + k_t (Fe^{II}) P_{O_2}$$

The quantity k' is taken to apply to the average of  $(Fe^{II})_{t_2}$  and  $(Fe^{II})_{t_1}$ ; plots of k' vs.  $(Fe^{II})$  were linear, as expected from (3), and were extrapolated to the initial ferrous ion concentration to give  $k'_1$ ,

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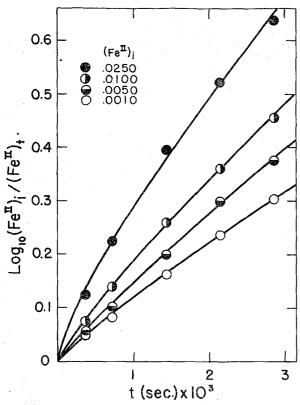


Fig. 1.—First-order plots for typical high temperature reactions (159°, 1.00 F H<sub>2</sub>SO<sub>4</sub>, in oxygen).

the initial apparent first-order constant. Values of  $k'_i$  at the same initial ferrous ion concentrations and temperatures were averaged and the averages plotted against the initial ferrous ion concentration. The straight lines obtained confirm equation 3 and are exhibited in Fig. 2. The resulting values of  $k_b$  and  $k_t$  are given in Table I. Activation energies of 13.4 ( $\pm$  2) and 16.3 ( $\pm$  2) kcal. were obtained for the second-order and third-order paths, respectively, from plots of log k vs. 1/T. The points fit on the appropriate straight lines to  $\pm 15\%$  giving rise to the indicated uncertainties.

TABLE I
HIGH TEMPERATURE RATE AND CONSTANTS

Initial FeII (mole l1) T, °C.	0.00100	0.00200	$0.00500$ $k_{i}'$ $(\sec c.^{-1})$ $\times 10^{5}$	0.0100	0.0250	$^{kb^a}_{(\mathrm{sec.}^{-1}$ $^{\mathrm{atm.}^{-1}})$ $\times 10^5$		
138 159 161	1.38 3.11 3.02	3.16	1.65 $3.88$ $3.52$	1.86 5.00 4.72	3.14 8.50	0.89 1.93 1.90	0.55 $1.60$ $1.33$	
180	6.65		8.44	10.6	19.0	3.84	3.40	

 $^aP_{02}$  calculated from initial pressure of one atmosphere at room temperature assuming perfect gas law.

Inhibition of the reaction by ferric ion was not found. At  $160^{\circ}$  in  $1.00 F H_2SO_4$  with an oxygen atmosphere, the reaction in solutions initially 0.00500 F in ferrous ion and 0.00100, 0.00500, 0.0100 and 0.0200 F in ferric ion were unaffected by the added ferric ion within the experimental error of 5%. Solutions initially 0.00100 and 0.00-

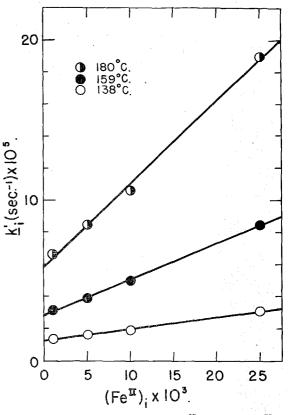


Fig. 2.—Variation of initial d ln (Fe<sup>II</sup>)/dt with (Fe<sup>II</sup>)<sub>i</sub>.

 $200 \, F$  in ferrous ion containing  $0.0100 \, F$  ferric ion initially gave no indication of ferric ion inhibition.

(b) Room Temperature.—The values for  $k_b$  and  $k_{\rm t}$  at 30° predicted by extrapolation of the high temperature measurements are  $2.5 \times 10^{-8} \text{ sec.}^{-1}$ atm.  $^{-1}$  and 3.5  $\times$  10 $^{-7}$  sec.  $^{-1}$   $M^{-1}$  atm.  $^{-1}$  (M = mole liter $^{-1}$ ). This suggested that the secondorder path would make a contribution to the rate equal to that of the third-order path for (Fe<sup>II</sup>) = 0.07 M. Previous investigators have worked at concentrations of 0.15-0.20 M,  $^{6} 0.02-0.46 M$ , and 0.01-0.3  $M.^7$  For the present investigations, measurements were obtained for only a few per cent. reaction, and the initial rate was determined from a plot of  $(Fe^{III})$  vs. t. The initial rates were plotted as  $-d \ln(Fe^{II})/dt$  vs.  $(Fe^{II})_i$ ; the intercepts, which should have been  $k_b P_{O_2}$ , were smaller than the experimental error and oxygen independent. In 1.00 F H<sub>2</sub>SO<sub>4</sub>,  $k_{\rm t} = 2.78 \times 10^{-6} \, {\rm sec.}^{-1} \, M^{-1} \, {\rm atm.}^{-1}$  and  $k_{\rm b} = 3 \times 10^{-10} \, {\rm sec.}^{-1} \, {\rm atm.}^{-1}$  from rates obtained at four ferrous ion concentrations. The small contribution from the path first order in ferrous ion could be due partially to the first-order ferrous path found at high temperatures. The erratic behavior, however, indicates that this contribution is a combination of experimental error and small amounts of impurities. Values of  $k_t$  at 30.5° in two sulfuric acid-sodium sulfate solutions in air and oxygen are given in Table II.

Effect of Glass Surface.—Studies with added Pyrex glass wool showed that catalysis by the walls of the reaction cells was probably not important. The first experiments at 140–180° gave erratic results, with some reactions proceeding very

Table II

Rate Data at 30.5°

			Ratio
			rates
(Fe <sup>II</sup> )i,	$-d(Fe^{II})/dt$	(M sec1)	(oxy- gen/ air)
	$\overset{ ext{air}}{( imes 10^{12})}$	oxygen (× 10 <sup>12</sup> )	
0.00100	6.62	6.55	
.00500	17.8	66.1	
.0100	55.0	284	
.0200	224	1130	
a			
$l_{\rm t}~({ m sec.}^{-1}~M^{-1})$	$5.47 \times 10^{-7}$	$2.78 \times 10^{-6}$	5.1
$l_{\rm b}  ({\rm sec.}^{-1})$	$3.9 \times 10^{-10}$	~0	0
0.22	6 F H <sub>2</sub> SO <sub>4</sub> and 0.	354 F Na <sub>2</sub> SO <sub>4</sub>	
(Fe <sup>II</sup> )i,	$(\times^{\mathrm{air}}_{10^{12}})$	oxygen (× 10 <sup>12</sup> )	
0.00100	4.86	8.68	
.00500	44.5	143	
.0100	139	540	
.0200	545	2320 .	
$l_t \text{ (sec.}^{-1} M^{-1})$	$1.18 \times 10^{-6}$	$5.65 \times 10^{-6}$	4.8
$l_{\rm b}$ (sec. $^{-1}$ )	$3.1 \times 10^{-9}$	$1.7 \times 10^{-9}$	0.5
a -d(Fe++)/c	$dt = l_b(Fe^{II}) + l_t$	(Fe <sup>II</sup> ) <sup>2</sup> .	

rapidly. Fairly reproducible results were obtained when the glass wool was heated to 500° in an oven for one-half hour, washed in hot aqua regia, rinsed, dried and transferred to the reaction cell with a glass rod. The glass wool could be centrifuged to the bottom of the cell for optical measurements.

The surface area<sup>3</sup> of the glass wool is estimated as  $2300 \text{ cm.}^2 \text{ g.}^{-1}$ . The additional surface area due to the glass wool was around three times the total inside wall area of a reaction cell. With  $(\text{Fe}^{\text{II}})_i = 0.001 \text{ to } 0.005 M$ , in oxygen, the ratio of reaction rates in the presence and absence of glass wool varied in an erratic fashion between 1.3 and 1. Thus it appears that the wall reaction was probably never more than 10% of the homogeneous reaction in the unpacked cells. Reaction rates in unpacked cells were more reproducible than in packed cells, suggesting that the cleaning procedure was effective and reproducible for the glass walls of the cells.

Experiments at  $30.5^{\circ}$  with added glass wool were carried out in glass stoppered bottles and the solutions siphoned back and forth between optical cells with an all-glass siphon system. With (Fe<sup>II</sup>), between 0.001 and 0.02 M, there was less than 1% effect that could be attributed to the walls of the optical cells.

Effect of Oxygen Pressure.—The first results obtained at 30.5° for the ratio of reaction rates in oxygen and in air at 1 atm. pressure were not the expected 4.76:1. A long and tedious set of measurements indicated that there was a reaction path that was first order in ferrous ion and zero order in oxygen and a reaction path that was second order in ferrous ion and first order in oxygen. A great deal of time was wasted before it was discovered that the commercial distilled water being used contained traces of cupric ion, which was responsible for the oxygen independent path.

At a fixed oxygen partial pressure, we may define apparent first- and second-order rate constants, referring to the dependence of rate on  $(Fe^{II})$ ;  $-d(Fe^{II})/dt = l_b(Fe^{II}) + l_t(Fe^{II})^2$ . In redistilled water, containing no significant  $Cu^{II}$ , the ratio of  $l_t$  in oxygen and air was evaluated as 5.1 in 1.00 F  $H_2SO_4$  and 4.8 in a solution 0.226 F in  $H_2SO_4$  and 0.354 F in  $Na_2SO_4$ , whereas the quantity  $l_b$  was very small and evidently inversely dependent on oxygen pressure (Table II). It seems probable that the apparent first-order path is a residual effect due to impurities and experimental error; the main part of the reaction proceeds by the rate law,  $-d(Fe^{II})/dt = l_t(Fe^{II})^2 = k_t(Fe^{II})^2 P_{O_t}$ .

The oxygen dependence was investigated at 160° in 1.00 F H<sub>2</sub>SO<sub>4</sub>, where reaction paths first and second order in ferrous ion had been found to occur. One run at each of two initial ferrous ion concentrations in air and oxygen was made. The ratio of the  $l_t$  values for the path second order in ferrous ion was 5.4 and the ratio of the  $l_b$  values for the path first order in ferrous ion was 3.5. The value of 3.5 is not entirely satisfactory. These reactions at high temperatures were carried out using the same 1.00 F H<sub>2</sub>SO<sub>4</sub> that was used at low temperatures, and it is known definitely that cupric ion is in very low concentration ( $\sim 1 \times 10^{-7} F$ ). The reaction between cupric ion and ferrous ion, which is a reasonable first step for cupric ion catalysis, would probably not be favored by an increase in temperature. The fact that the ratio of rate in oxygen to rate in air is not erratic and is 3.5 indicates that some of the path first order in ferrous ion must be oxygen dependent. We believe that the data indicate that the main part of the term in the rate law that is first order in (Fe<sup>II</sup>) is also first order in oxygen. The discrepancy between 3.5 and the expected 4.8 may be partially due to impurities. It may also be partially due to errors in determining both  $l_b$  and  $l_t$  from the data on change in initial rate with (FeII)i at any one oxygen pressure. The fact that the ratio, 5.4, of  $l_t$  in oxygen and air is higher than expected is consistent with this possibility.

Effect of Sulfate and Hydrogen Ion.—The effects of varying the sulfate ion at approximately constant hydrogen ion concentration and varying the hydrogen ion at relatively constant sulfate ion concentrations have been studied at 30.5° in one atmosphere of oxygen in solutions 0.0200 and 0.0400 F in ferrous ion. Stock solutions were prepared by dissolving various amounts of sodium sulfate and sulfuric acid in water that had been redistilled to remove traces of cupric ion. solutions were kept at an ionic strength of 1.0-1.3 with sodium perchlorate. These results are uncertain in that a value for the second ionization constant for sulfuric acid must be chosen. We have taken this value to be 0.075 at an ionic strength of 1.0 (sodium perchlorate). The dependence of the third-order rate constant  $k_t$  on sulfate ion is seen in Fig. 3. The hydrogen ion was varied from 0.066 to 0.099 M in this series but, as will be seen later, this will have little effect. The rate constant increases at a decreasing rate as the sulfate ion concentration is increased. The increase in the sulfate ion concentration and the slight increase in optical density of the reaction solution due to the large

amounts of ferrous ammonium sulfate added have been taken into account.

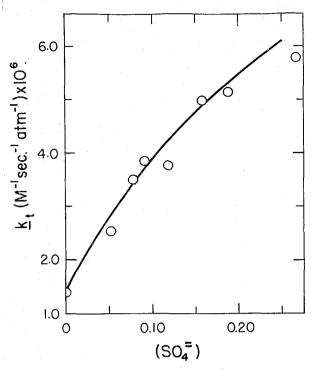


Fig. 3.—Dependence of termolecular rate constant at  $30.5^{\circ}$  on sulfate ion concentration. Reactions in oxygen at one atmosphere pressure. The formal concentrations of the various added chemicals, and the calculated concentrations of some of the ions (assuming  $K_{\rm HSO_4}$  = 0.075) are displayed below.  $\mu = 1.0$ –1.3 (sodium perchlorate).

		-	-	-	-
(H <sub>2</sub> SO <sub>4</sub> ), <i>F</i>	(Na <sub>2</sub> SO <sub>4</sub> ), F	$(Fe^{II}),$ $F$	(SO <sub>4</sub> ), M	(H +), M	(HSO4 <sup>-</sup> ), <i>M</i>
0.068	0	0.020	0.052	0.080	0.056
		.040	.078	.066	.070
.094	.061	.020	.091	.084	.104
		.040	.118	.071	.117
.135	.166	.020	.158	.087	.183
		.040	.118	.077	.193
.226	.354	.020	.267	.099	.353

The increase in the rate constant can be explained by the following argument. At zero sulfate ion concentration, the path second order in ferrous ion should be the same as the path in perchloric acid, where little complexing is to be expected. From data of George, the constant for this reaction is found to be  $1.4 \times 10^{-6} \, M^{-1} \, \mathrm{atm.^{-1}}$  sec.  $^{-1}$  in  $0.083 \, F \, \mathrm{HClO_4} \, \mathrm{at} \, 30^{\circ}$  and an ionic strength of 1.0. When this value is placed on Fig. 3, it is possible to draw a smooth curve through the points. A reasonable mechanism for sulfate ion catalysis would seem to be

$$2Fe^{++} + O_2 \xrightarrow{k_u} 2Fe^{III} + H_2O_2$$
 (4)

as an uncatalyzed rate step, and

$$Fe^{++} + SO_4^{-} \xrightarrow{K} Fe^{++}SO_4^{-}$$
 (5)

$$Fe^{++}SO_4^- + Fe^{++} + O_2 \xrightarrow{k_8} 2Fe^{III} + H_2O_2 + SO_4^-$$
(6

for the sulfate-catalyzed rate step. This mechanism would lead to the rate expression

$$\frac{-\mathrm{d}(\mathrm{Fe^{II}})}{\mathrm{d}t} = k_{\mathrm{u}}(\mathrm{Fe^{++}})^{2}P_{\mathrm{O}_{2}} + k_{\mathrm{s}}(\mathrm{FeSO}_{4})(\mathrm{Fe^{++}})P_{\mathrm{O}_{2}} = k_{\mathrm{s}}(\mathrm{Fe^{II}})^{2}P_{\mathrm{O}_{3}}$$
(7)

If all ferrous ion is either uncomplexed or as the ferrous-sulfate complex, the following expressions may be obtained, where (Fe<sup>II</sup>) is the formal ferrous ion concentration.

$$\frac{(\text{FeSO}_4)}{(\text{Fe}^{\text{II}})} = \frac{K(\text{SO}_4^-)}{1 + K(\text{SO}_4^-)} \qquad \frac{(\text{Fe}^{++})}{(\text{Fe}^{\text{II}})} = \frac{1}{1 + K(\text{SO}_4^-)}$$

Substituting these expressions into (7), one obtains

$$k_{\rm t} = \frac{k_{\rm u} + k_{\rm s} K({\rm SO_4}^{-})}{1 + K({\rm SO_4}^{-})^2}$$
 (8)

By setting  $k_{\rm u}=1.4\times 10^{-6}~M^{-1}~{\rm atm.^{-1}~sec.^{-1}}$  as found by George, and assuming the sulfate ion concentration is not appreciably affected by the ferrous sulfate complex, expression (8) may be solved numerically for  $k_{\rm s}$  and K by using values of  $k_{\rm t}$  and (SO<sub>4</sub>=) from Fig. 3. Values obtained were  $K=1.1\pm 0.2~M^{-1}$  and  $k_{\rm s}=3.1\pm 0.5\times 10^{-6}~M^{-1}$  atm.  $k_{\rm s}=1.1\pm 0.2~M^{-1}$  atm.  $k_{\rm s}=1.1\pm 0.5$  is the theoretical curve drawn from (8) with these values.

The results obtained by varying the hydrogen ion concentration are shown in Table III. The hydrogen ion dependence of the reaction is uncertain from these experiments in that the sulfate ion concentration has not been controlled as well as de-This makes detailed kinetic interpretation difficult. However, as the hydrogen ion concentration is decreased by a factor of 75 from 1.032 to 0.014, the rate constant at most doubles. Also, the rate constant does not change drastically over the hydrogen ion concentrations which were obtained in the sulfate dependence experiments. We have no satisfactory explanation for the observed small dependence upon hydrogen ion concentration. A generally similar dependence of the termolecular rate constant on H+ is observed in perchlorate media.7

TABLE III
HYDROGEN ION DEPENDENCE

H <sub>2</sub> SO <sub>4</sub> ,	Na <sub>2</sub> SO <sub>4</sub> ,	Fe(II),	(SO <sub>4</sub> =),	(H <sup>+</sup> ),	(HSO <sub>4</sub> -),	$(M^{-1} \text{ sec.}^{-1} \text{ atm.}^{-}) \times 10^{6}$
1.00	0.0	0.0200	0.072	1.032	0.968	2.78
0.466	.040	. 0200	.075	0.461	.471	3.17
		.0400	.086	.432	. 500	3.00
.094	.061	.0200	.091	.084	. 104	3.86
		.0400	.118	.071	.117	3.78
.0203	.0664	.0200	.104	. 017	.023	5.28
		.0400	. 141	.014	. 026	5.05

All rate determinations in this investigation were made on solutions of ferrous ammonium sulfate. By adding an equal concentration of ammonium sulfate to a typical high temperature reaction in 1.00 F H<sub>2</sub>SO<sub>4</sub> under oxygen, the ammonium ion was shown to be without effect on the reaction rate.

Possible Effects of Organic Impurities.—In the high temperature range, it was thought that residual organic dust impurities might participate in induced reactions, or otherwise enter into the

reaction and be destroyed in the process. To check on this possibility, solutions with  $(Fe^{II})_i = 0.001$  to 0.005 F in 1.00 F sulfuric acid were heated at  $160^{\circ}$  in oxygen to about 60% reaction. The tubes were then carefully opened, and a small, known volume of a concentrated ferrous ion solution was added. The tubes were then resealed in oxygen and reheated. The observed rate constants were the same before and after addition of the concentrated ferrous ion solution. Since there was no decrease in rate constant after addition of the concentrated ferrous ion solution, either reaction with organic dust impurities is not occurring, or the concentration of these impurities is too large to be appreciably reduced by the reaction.

Effect of Cu(II).—As described previously, the anomalous results first obtained at 30.5° led us to suspect  $Cu^{II}$  as an impurity. Trace analyses for  $Cu^{II}$  were therefore made using a spectrophotometric method based on the dithizone–cupric ion complex.<sup>11</sup> Sulfuric acid, sodium sulfate, ferrous ammonium sulfate and sodium perchlorate solutions were found not to contain significant concentrations of cupric ion. However, commercial distilled water contained concentrations of ca. 2  $\times$  10<sup>-6</sup> F  $Cu^{II}$ . In redistilled water, the cupric ion concentration was reduced at least twenty times to a value which would not significantly affect the rate.

At  $30.5^{\circ}$  in sulfuric acid—sodium sulfate solutions, cupric ion catalyzes the ferrous ion—oxygen reaction by a reaction path first order in ferrous ion, first order in cupric ion and zero order in oxygen pressure. These results have been obtained in a stock solution 0.226~F in  $H_2SO_4$  and 0.354~F in  $Na_2SO_4$ , which has  $(H^+) = 0.11~M$ ,  $(HSO_4^-) = 0.34$  and  $(SO_4^-) = 0.24$ .

In these solutions, increasing the cupric ion concentration increases the rate of the reaction path first order in ferrous ion. It was found that the measured rate is a linear function of the total cupric ion concentration for reactions with  $(Fe^{II})_i = 0.00100 \ F$  in air at one atmosphere. In reactions containing the relatively high total cupric ion concentration of  $1.1 \times 10^{-5} \ F$ , the rate is the same in air and oxygen. The rate law for this situation at given sulfate and hydrogen ion concentrations is

$$-d(Fe^{II})/dt = k_t(Fe^{II})^2 P_{O_2} + 4k_9(Fe^{II})(Cu^{II})$$

The above equation with  $k_9 = 1.9 \times 10^{-3} \ M^{-1}$  sec.<sup>-1</sup> and  $k_4 = 1.5 \times 10^{-5} \ M^{-1}$  atm.<sup>-1</sup> sec.<sup>-1</sup> fits the data to  $\pm 5\%$ .

Since the concentrations of cupric and ferric ions are relatively low, the catalysis may be explained by the following reactions postulated by Cher and Davidson<sup>3</sup> and many previous workers.

$$Cu^{II} + Fe^{II} \xrightarrow{k_9} Cu^{I} + Fe^{III}$$
 (9)

$$Cu^{I} + O_2 \longrightarrow Cu^{II} + HO_2$$
 (10)

It is assumed that the first reaction is the rate step and the second reaction is very rapid. The HO<sub>2</sub> reacts further with Fe<sup>II</sup> as in the Weiss mechanism.<sup>8</sup>

#### Discussion

The activation energy for the bimolecular reaction measured between 140 and 180° is 13.4 ( $\pm$  2) kcal. However, the upper limit for  $k_b$  at  $30.5^{\circ}$  combined with the average value,  $k_b = 1.9 \times 10^{-5}$  sec.  $^{-1}$  atm.  $^{-1}$  at  $160^{\circ}$ , implies that  $E_a > 22$  kcal. The activation energy for the termolecular reaction observed at high temperatures is  $16.3 (\pm 2)$  kcal. The values at 160 and 30° imply  $E_a = 12.6$  kcal. George<sup>7</sup> reports  $E_A = 17.4$  kcal, for the termolecular path between 20 and 40° in 0.50 F HClO<sub>4</sub>. The possibility of unknown experimental errors cannot, of course, be excluded. However, it would not be surprising if the activation energy for either reaction path were dependent on temperature. This is especially likely because there is probably a very marked change in the concentrations and activity coefficients of the ionic species present in 1F H<sub>2</sub>SO<sub>4</sub> between 30° and the range 140-180°.

The experimental results do not, of course, distinguish between the alternative intermediate HO<sub>2</sub> and Fe<sup>IV</sup> (reactions 1a and b) for the bimolecular reaction path. The Weiss mechanism<sup>8</sup> involves the former intermediate. In this case, the complete reaction path is

$$Fe^{II} + O_2 \longrightarrow Fe^{III} + HO_2$$
 (1a)

$$Fe^{II} + HO_2 \longrightarrow Fe^{III} + H_2O_2$$
 (11)

$$Fe^{II} + H_2O_2 \longrightarrow Fe^{III} + OH + OH^-$$
 (12)

$$Fe^{II} + OH \longrightarrow Fe^{III} + H_2O$$
 (13)

The observed values of  $k_b$  are four times the rate constant for reaction (1a) for this mechanism.

Experiments in this Laboratory have shown that in a pyrophosphate medium, the rate of oxygenation is first order in  $Fe^{II}$  and first order in oxygen, and faster than the corresponding reaction rate in a phosphate medium. Weiss<sup>9</sup> has reported that the reaction is bimolecular with respect to  $Fe^{II}$  and  $O_2$  in the presence of fluoride. Posner<sup>5</sup> reports a bimolecular reaction in 5–8 F HCl at room temperature, and the reaction rate decreased markedly with acidity. As discussed below, the data of McBain<sup>4</sup> indicate that the reaction is principally termolecular in 1 F HCl. In a perchlorate medium, the reaction path at room temperature is exclusively termolecular, and no investigations have been made at high temperature.

Weiss<sup>9</sup> has proposed essentially the following as a model of the transition state

$$[X-Fe^{II}-O_2] \leftrightarrow [X-Fe^{III}-O_2]$$

The transition state is stabilized by groups, X, which form complexes with tripositive iron. The equilibrium constants for the reaction

$$Fe^{+++} + X^{-n} \xrightarrow{\cdot} FeX^{3-n}$$

for  $\rm H_2P_2O_7^{=,12}$  F<sup>-,13</sup>  $\rm H_2PO_4^{-,14}$  SO<sub>4</sub><sup>=,10</sup> Cl<sup>-,15</sup> ClO<sub>4</sub><sup>-,16</sup> in the neighborhood of 25° are: 10<sup>5</sup>, 5  $\times$  10<sup>5</sup>, 1.4  $\times$  10<sup>3</sup>, 100, 4.1, 1–3 mole<sup>-1</sup> liter, respec-

- (12) Preliminary estimate based on work in this Laboratory.
- (13) H. W. Dodgen and G. K. Rollefson, This Journal, 71, 2600 (1949).
  - (14) T. Yamane and N. Davidson, to be published.
- (15) M. W. Lister and D. E. Rivington, Can. J. Chem., 38, 1603
- (16) K. W. Sykes, Chem. Soc. Special Pub. No. 1, 64 (1954).

<sup>(11)</sup> E. B. Sandell, "Colorimetric Determination of Traces of Metals," 2nd Ed., Interscience Publishers, Inc., New York, N. Y., 1950, p. 295.

tively. Thus, in the presence of the strong complexes, the oxygenation is bimolecular at room temperature. For the complexing agents of moderate strength, SO<sub>4</sub> and Cl-, the reaction is termolecular at room temperature and moderate (< 1 F) concentration of the complexing anions. A bimolecular reaction occurs in more extreme conditions at high temperatures in 1 F H<sub>2</sub>SO<sub>4</sub> or in 5 F HCl at room temperature. At room temperature in perchlorate media, the oxygenation is termolecular; it is not known whether a bimolecular reaction will occur for more extreme conditions. Suitable data for a quantitative comparison are not available, but the relative reaction rates for the bimolecular path generally parallel the complexing constants quoted above.

The rate-determining step for the termolecular path is probably

$$2Fe^{II} + O_2 \longrightarrow 2Fe^{III} + H_2O_2$$
 (2)

followed by reactions (7) and (8). The observed values of  $k_t$  are therefore twice the rate constant of the above reaction. Two possible detailed models for reaction (2) are

$$(H_2O_2)_5Fe^{II}OH_2^{++} + O = O + H_2OFe^{II}(OH_2)_5^{++} \longrightarrow (H_2O_2)_5Fe^{III}OH^{++} + H_2O_2 + HOFe^{III}(OH_2)_5^{++}$$
 (2')

Mechanism (2') involves a hydrogen atom transfer from the water molecules of the coördination sphere of Fe++. In mechanism (2"), an O2 molecule is directly coordinated to two Fe++ ions, and a peroxide bridge between two Fe+++ ions is formed. It may be recalled that a peroxy complex of Fe<sup>III</sup>, Fe( $O_2H$ )<sup>++</sup>, is known.<sup>I7,18</sup> If (2') were correct, there should be a marked hydrogen isotope effect and a significant decrease in reaction rate in  $D_2O$ , whereas this should not be the case for (2''). Evidence of this nature in favor of a hydrogen atom transfer mechanism for the Fe++, Fe+++ electron exchange has recently been reported. 19 Evidence that there is no significant hydrogen isotope effect in the similiar Pu<sup>III</sup>\_Pu<sup>IV</sup> oxygenation has been found recently. <sup>18</sup> In either case, it is plausible that sulfate ion would accelerate the rate because of complex ion formation in the transition state. for case (2''), the transition state would be

$$(H_2O)_4(SO_4)Fe-O-O-Fe(H_2O)_5^{+4}$$

No independent evidence is available to compare with the deduction from the kinetic data that the complex constant of Fe<sup>++</sup> with SO<sub>4</sub><sup>-</sup> is 1.1 mole<sup>-1</sup> liter. The value is about as expected for these ions for an ionic strength of 1.0, however.

The termolecular rate constant  $k_t$  at 30.5° in 1 F H<sub>2</sub>SO<sub>4</sub> found in this study, 2.78  $\times$  10<sup>-6</sup>  $M^{-1}$  atm.<sup>-1</sup> sec.<sup>-1</sup>, agrees well with values reported by

other investigators. Lamb and Elder<sup>6</sup> found 4.0  $\times$  10<sup>-6</sup> and McBain<sup>4</sup> reported 1.1  $\times$  10<sup>-6</sup>, in both cases at 30° in 1 F H<sub>2</sub>SO<sub>4</sub>. (The corresponding comparison made by George<sup>7</sup> between rates in HClO<sub>4</sub> and in H<sub>2</sub>SO<sub>4</sub> is slightly erroneous in that Lamb and Elder's results were not corrected from 1 atm. air to 1 atm. O<sub>2</sub>.) We find that the data of McBain in 1 F HCl fit a termolecular rate law much better than a bimolecular rate law; the rate constant (apparently at 30°) is  $6.5 \times 10^{-6} \ M^{-1}$  atm.  $^{-1}$  sec.  $^{-1}$ .

The rate constant for the first step in the cupric ion catalyzed reaction is  $1.9 \times 10^{-3} M^{-1}$  sec.<sup>-1</sup>

$$Fe^{II} + Cu^{II} \longrightarrow Fe^{III} + Cu^{I}$$
 (9)

in  $0.226~F~H_2SO_4$ ,  $0.354~F~Na_2SO_4$ . The corresponding value in  $0.434~F~H_3PO_4$ ,  $0.302~F~H_2PO_4^-$  is  $2.8~\times~10^{-1}$ . This shows that phosphate ion complexes the iron in the transition state for reaction (9). Since sulfate is a moderately strong complexing anion for Fe<sup>+++</sup>, it may be assumed that  $SO_4^-$  can also participate in the transition state for reaction (9). Unfortunately, no data to test this prediction were obtained.

George<sup>7</sup> reports that the Fe<sup>II</sup>, O<sub>2</sub> reaction in perchloric acid is only slightly catalyzed by Cu<sup>II</sup>, and that the catalyzed reaction is second order in Fe<sup>II</sup>. The smallness of the catalytic effect may in part be due to the slowness of reaction (9) in HClO<sub>4</sub>. There is however an additional consideration. Cher and Davidson<sup>3</sup> observed that at high Cu<sup>II</sup> concentrations, the mechanism of the Fe<sup>II</sup>, O<sub>2</sub> reaction was

$$Fe^{II} + Cu^{II} \xrightarrow{K_{9}} Fe^{III} + Cu^{I}$$
 (9)

$$Cu^{I} + O_{2} \xrightarrow{K_{10}} Cu^{II} + HO_{2}$$
 (10)

$$Fe^{II} + HO_2 \xrightarrow{k_{11}} Fe^{III} + H_2O_2$$
 (11)

The corresponding rate expression is  $-d(Fe^{II})/dt = 4 k_{11}K_9K_{10} (Fe^{II})^2P_{O_2}/(Fe^{III})$ , and the rate is independent of Cu<sup>II</sup> concentration.  $K_9K_{10}$  is actually the equilibrium constant for the reaction

$$Fe^{II} + O_2 \Longrightarrow Fe^{III} + HO_2$$
 (12)

The value of this equilibrium quotient in 1 F HClO<sub>4</sub> may be estimated as  $3 \times 10^{-4}$  of its value in  $0.43~F~H_3PO_4$ ,  $0.30~F~H_2PO_4^-$  from the formation constants of Fe(H<sub>2</sub>PO<sub>4</sub>)<sup>++</sup> and Fe(H<sub>2</sub>PO<sub>4</sub>)<sub>2</sub><sup>+</sup> (1.4  $\times$  10<sup>3</sup> mole<sup>-1</sup> liter and  $3.4 \times 10^4$  mole<sup>-2</sup> liter<sup>2</sup>). A Reaction (10) is a fast, exothermic reaction and possibly not greatly affected by complexing anions. On this basis, we estimate from the results of Cher and Davidson<sup>3</sup> that the rate law for the copper catalyzed reaction in 1 F HClO<sub>4</sub> is  $-d(Fe^{II})dt = 8 \times 10^{-7}~(Fe^{II})^2P_{O_2}/(Fe^{III})$ ; the rate law for the uncatalyzed reaction is  $2 \times 10^{-6}(Fe^{II})^2P_{O_2}$ . It is not expected that the above calculation is very reliable, but it does suggest that after the accumulation of some Fe<sup>III</sup> in the system, the copper catalyzed reaction might indeed be rather insignificant in comparison to the uncatalyzed termolecular reaction.

PASADENA, CALIFORNIA

<sup>(17)</sup> M. G. Evans, D. George and N. Uri, *Trans. Faraday Soc.*, **45**, 230 (1949).

<sup>(18)</sup> We are indebted to Dr. T. W. Newton for some interesting corespondence regarding the possibility of (2'').

<sup>(19)</sup> J. Hudis and R. W. Dodson, THIS JOURNAL, 78, 911 (1956).

### III. PROPOSITIONS

- 1. Study of the high temperature decomposition of NO to  $N_2$  and  $O_2$  between 2000 and  $3000^{\circ} K$  has indicated a mechanism involving O and N atoms, as proposed by Zeldovitch from experiments on explosions in air (1). The data of Glick, Klein, and Squire (2), who studied air reactions with a single pulse shock tube technique, support the mechanism. However, Fenimore and Jones (3), who studied NO decomposition in a flame, did not observe the predicted inhibition term  $k_3[NO]/k_2[O]$  even though [NO]/[O] was varied from .5 to 2000. There are several indications that  $k_3$  and  $k_4$  are comparable. It is proposed to study the decomposition of NO with the single pulse shock tube technique to resolve this question.
  - (1) J. Zeldovitch, Acta Physico. URSS 21, 577 (1946).
  - (2) H. S. Glick, J. J. Klein, and W. Squire, <u>J. Chem.</u>

    Phys. 27 850 (1957).
  - (3) C. P. Fenimore and G. W. Jones, <u>J. Phys. Chem.</u> 61, 654 (1957).
- 2. The reaction between ferric ion and iodide ion has been assumed to involve a ferric ion-iodide ion complex as the initial reaction step (3). A spectrophotometric method involving a fast mixing apparatus is proposed to detect and study this complex.
  - (3) A. J. Fudge and K. W. Sykes, J. Chem. Soc. 1952 119.

- 3. It has been postulated that in the urea-formaldehyde reactions leading to polymer formation urea acts as an
  amino acid amide (4). Results of more recent analyses and
  kinetics studies do not support such an interpretation (5).
  It is proposed that several of the arguments supporting the
  amino acid amide theory are unconvincing, and other experiments are proposed to test the theory. Two such experiments
  are the reaction of ethylene diamine and oxamide with
  formaldehyde.
  - (4) C. S. Marvel, J. R Elliot, F. E. Boettner, and H. Yuska, J. Am. Chem. Soc. 68, 1681 (1946).
  - (5) J. I. de Jong and J. de Jonge, <u>Rec. trav. Chim.</u>72, 139, 207, 213, 1027 (1953).
  - 4. It is proposed that the equilibrium

$$H_2O_2 = 2 OH$$

and the subsequent decomposition of OH radicals (6) be studied in the shock tube. The OH concentration may be determined spectrophotometrically using the electrodeless discharge through water vapor developed recently at the National Bureau of Standards (7). It might prove possible to use  $H_2O_2$  as a source of OH radicals for other reactions.

(6) C. N. Satterfield and T. W. Stein, J. Phys. Chem. 61, 537 (1957).

- (7) H. J. Kostkowski and H. P. Broida, <u>J. Opt. Soc.</u>

  <u>Am</u>. 46, 246 (1956).
- 5. Reditzki and Nowinski (8) have found that the catalysis of yeast alcohol dehydrogenase reactions by o-phenanthroline (9) is not effective when the reactants are purified. They interpret this to mean that the original catalysis was due to chelating of traces of heavy metals in the solutions. In view of the large effect involved, it is proposed that before this explanation is accepted some reactions be done in which traces of metal ions are known to be present. Besides more definitely establishing the cause, these experiments would provide data for extrapolation the effect to zero metal concentration.
  - (8) H. E. Redetzki and W. W Nowinski, <u>Nature</u> 179, 1018 (1957).
  - (9) B. L. Vallee and F. L. Hoch, <u>Pro. Nat. Acad. Sci.</u>
    41, 327 (1955).
- 6. It is proposed that a spectrophotometric study be made of the colored complexes formed between NO and ferrous ion in acid solution (10). Although known for many years as the basis of the "brown-ring" test for nitrates and nitrites, only one brief examination of the spectra (11)--with no equilibrium data--has been published.

- (10) T. Moeller, J. Chem. Ed. 23, 542 (1946).
- (11) H. I. Schlesinger and A. Salathe, <u>J. Am. Chem.</u>
  <u>Soc. 45</u>, 1863 (1923).
- 7. Preliminary evidence from the coulometric titration of bromate with cuprous copper (12) indicates that the rate of oxidation of cuprous ion by bromine in solution is dependent on the cupric ion concentration. It is proposed that a kinetic study of this effect be made. It may be possible to demonstrate that the catalytic effect of cupric ion is due to the formation of interaction complexes of the type previously found in chloride solutions (13).
  - (12) G. M. Arcand and E. H. Swift, unpublished experiments.
  - (13) H. McConnell and N. Davidson, J. Am. Chem. Soc. 72, 3168 (1950).
- 8. The unstable nitrogen oxide  $N_2O_2$  is described as a chain structure (14) and as a square (15) in the literature. A double labelled isotope exchange reaction between  $N^{14}-O^{16}$  and  $N^{15}-O^{18}$  is proposed to better determine the structure.
  - (14) A. L. Smith, W. E. Keller, and H. L. Johnston, <u>J. Chem. Phys.</u> 19, 189 (1951).
  - (15) W. J. Dulmage, E. A. Meyers, and W. N. Lipscomb,
     J. Chem. Phys. 19, 1432 (1951).

- 9. The autooxidation-reduction reaction of ferric thioglycolate in alkaline solution has been assumed to involve a hydroxyl bridged dimer (16). It is proposed that a sulfur bridged dimer is more likely from the final products obtained.
  - (16) D. L. Leussing and L. Newman, <u>J. Am. Chem. Soc.</u> 78, 552 (1956).
- 10. It is proposed that another copy of the Journal of Chemical Physics, Volume 19 (1951) be obtained, as the other copy has been missing from the library for several months.