VOLUMETRIC AND PHASE BEHAVIOR OF PROPENE-1-BUTENE SYSTEM

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ABSTRACT

The volumetric behavior of an 81.739 mole % 1-butene mixture of propene and 1-butene was investigated at seven temperatures from 40°F to 280°F over a pressure range from about 40 pounds per square inch absolute to 10,000 pounds per square inch absolute. Tabulations of single-phase and two-phase data interpolated to even values of pressure are presented.

Revised volumetric data for three mixtures of propene end 1-butene previously investigated by Farrington are presented in tabular form over similar ranges of temperature and pressure. Variations of actual volumetric behavior from ideal behavior are shown graphically for the system.

The compositions of bubble-point liquid and dew-point gas were established experimentally throughout the two-phase region for temperatures between 40° and 280°F. Values of specific volume and composition for coexisting liquid and gas phases are tabulated. Equilibrium constants are given for propene and 1-butene. Properties for the critical region are estimated.

TABLE OF CONTENTS

PART	TITLE												PAGE
I.	Introduction		٠	•	٠	ø	٠	٠	٠	ø	٠	۵	. 1
II.	Materials	٠	•	٠	۵	٠	٠	٠	٠	٠	٠	ø	. 3
III.	Experimental	Me	thod	an	d A	.ccu	rac	y o	f R	esu	lts	6	• 4
IV.	Experimental	Re	sult	S	٠	0	٠	٠	٠	٠	٠	ø	10
V.	Nomenclature		٠		٠	٠	٠	٠	٠	٠	٠	•	18
VI.	References		٠	٠	•	٠	•	٠	۰	٠	ø	•	19
VII.	Figures .		٠	•	٠	٠	0	٥	۵	٠	٠	۰	20
VIII.	Tables .	٩	٠	ø	٠	٠	٠	۲		۰	٠	0	28
IX.	Appendix .	۰	٠	٠	•	٠	•	0	٠	٠	٠	•	61

LIST OF FIGURES

		Page
l.	Schematic Diagram of Apparatus	. 20
2.	Compressibility Factor for the Propene-1-Butene	
	System at 280°F	. 21
3.	Pressure-Composition Diagram for Propene-1-Butene	
	System	. 22
4.	Temperature-Composition Diagram for Propene-1-Bu-	
	tene System	. 23
5.	Pressure-Temperature Diagram for Propene-1-Butene	
	System	. 24
6.	Equilibrium Constants for Propene and 1-Butene in	
	the Propene-1-Butene System	. 25
7.	Deviation of Bubble-Point Pressure from Raoult's	
	Law for Propene-1-Butene Mixtures at $160^{\circ}F$. 26
8.	Percentage Deviation of Actual Specific Volume	
	from Ideal Solution Value for Propene-1-Butene	
	Mixtures at 160°F	. 27

LIST OF TABLES

,

		Page
I.	Single-Phase Volumetric Behavior of Four	
	Experimental Mixtures of Propene and 1-Butene .	. 28
II.	Two-Phase Volumetric Data for a Mixture of	
	Propene and 1-Butene with 81.739 Mole % 1-	
	Butene	. 56
III.	Experimental Data for Coexisting Phases in	
	the Propene-1-Butene System	• 57
IV.	Properties of Coexisting Liquid and Gas	
	Phases in the Propene-1-Butene System	. 58
٧.	Properties of Propene-1-Butene System in	
	the Critical Region	. 60

I. INTRODUCTION

Olefins are becoming of increasing industrial importance as raw materials because of their susceptability to varied chemical reactions. A growing synthetic chemical industry makes use of olefins as a starting point in the production of a relatively large number of organic compounds. The petroleum industry is a source of vast quantities of unsaturated hydrocarbons which result from cracking operations. Natural gas can be converted in part to olefins by cracking or catalytic dehydrogenation.

Propene and 1-butene are two of the more common and important olefins. Together they enter into many polymerization reactions. Because propene and 1-butene are very similar in their physical and chemical properties, an accurate knowledge of the phase equilibrium for the system is needed for separation processes. Reliable volumetric and phase equilibrium data concerning 1-butene and propene may serve to illustrate the behavior of other closely related olefins.

Almost no experimental volumetric and phase equilibria data are to be found in the literature concerning combinations of unsaturated alighatic compounds. The behavior of mixtures of propene and 1-butene does not appear to have been investigated previously. However, the two individual components have been investigated in some detail. Olds, Sage, and Lacey (1), in this laboratory, have established the volumetric behavior of 1-butene at pressures up to 10,000 pounds per square inch and in the temperature interval between 100° and 340°F. The results of other investigations of 1-butene may be found in the literature (2)(3)(4)(5). The volumetric behavior of propene was studied recently in this laboratory by Farrington (5)(6), who used pressures up to 10,000 pounds per square inch throughout the temperature interval between 40° and 460° F. Other investigations of the volumetric behavior of propene are reported in the literature (8)(9)(10)(11).

Farrington began the study of the propene-1-butene system and reported his results in a thesis(6). He investigated the volumetric properties of 17.050, 33.153, and 69.050 mole % 1-butene mixtures. The initial smoothing of his primary data was accomplished by Farrington. The final smoothing of Farrington's results against composition of the system was carried out by the author. The data are included in the present thesis.

The inconsistencies of data found by different investigators are expected to be more in the case of olefins than with paraffins, due to greater instability and difficulty of preparation. The present work was restricted to a maximum temperature of 280°F as a result of a previous investigation of 1-butene which reported a marked deterioration above 300°F. No appreciable decomposition, polymerization, or isomerization were detected during the investigation.

II. MATERIALS

The propene employed in this investigation was obtained from the Phillips Petroleum Company with an analyzed purity of greater than 0.995 mole fraction propene. Further purification of the propene was carried out by a fractionation at atmospheric pressure in a column packed with small glass helices. A reflux ratio of approximately 40 to 1 was used, and the first tenth and the last fifth of the material were discarded in the course of the fractionation. The purity of the propene was checked in the volumetric apparatus by means of an isothermal vaporization from bubble point to dew point at 100°F. Several batch lots of purified propene were prepared during the course of the investigation, and the maximum change of vapor pressure found in going isothermally at 100°F from bubble point to dew point was 0.8 pound per square inch.

The 1-butene was prepared by dehydration of n-butanol with activated alumina as a catalyst. A description of apparatus, preparation procedure, and method of purification used may be found in the literature (1). A modification of the apparatus was made in that the 4-8 mesh catalyst as described in the literature had been replaced with 8-14 mesh granular alumina. As a result the optimum flow rate of liquid n-butanol was increased from 35 to about 60 drops per minute. The maximum change in vapor pressure in going isothermally at 130°F from bubble point to dew point for any of the batches of 1-butene was 0.7 pound per square inch. Quantities of 1-butene were prepared as above shortly before use in the volumetric apparatus. The time of storage of the 1butene was held to a minimum to reduce the possibility of an isomerization to 2-butene.

III. EXPERIMENTAL METHOD AND ACCURACY OF RESULTS

The pressure-volume-temperature apparatus employed in the volumetric studies has been described in detail in the literature (12). However, it is felt that a brief description of the equipment is warranted here. In principle the apparatus (Figure 1) consists of a stainless steel chamber within which a sample of known weight and composition is introduced by a weighing bomb technique which has been described (12). The weight of sample is known within 0.1% and the composition to within 0.001 mole fraction. The sample is confined within the chamber, and simultaneous measurements of pressure, temperature, and volume of the sample are made after equilibrium has been attained. The equilibrium condition of the contents of the chamber is provided by mechanical agitation using a cylindrical cage of inclined paddles attached to vertical rods, activated by means of an electromagnet rotating about the outside of the chamber. The equilibrium chamber is submerged in an agitated oil bath whose temperature is controlled to within 0.03°F of the desired value. The temperature is measured with a strain-free platinum resistance thermometer in connection with a Mueller bridge. A cooling unit which draws kerosene from the oil bath, passes it over freon-cooled coils, and returns the kerosene to the oil bath is used at temperatures below 100°F. The volume of the sample in the chamber is varied by introduction or withdrawal of mercury. The quantity of mercury added to the equilibrium chamber is established from the change in elevation of a mercury-air interface within an interconnected air chamber as measured by an electric probe. The measurement of volume is possible with less accuracy than either the measurement of pressure

or of temperature, and the volumes are estimated to be known within 0.2-0.3%. The pressure is measured by a balance of the piston-cylinder type (12) which is calibrated against the vapor pressure of carbon dioxide at the ice point (13). The equilibrium pressure may be measured within 0.1 pound per square inch or 0.05%, whichever is larger in magnitude.

The method used in obtaining volumetric data may be summarized as follows:

1) After the sample has been introduced into the chamber, the pressure is raised to the greatest desired value by injecting mercury into the chamber.

2) The oil bath is maintained at a predetermined temperature and frequent readings are taken to see that no deviations occur from the desired temperature.

3) A sufficient period of time before taking measurements is allowed for equilibrium to be attained as shown by constancy of pressure and temperature with time.

4) Measurements of volume and pressure are made.

5) The pressure is decreased, equilibrium is re-established, and the process of making measurements of pressure and volume is repeated until that time at which the maximum working volume of the chamber is reached.

6) The temperature of the oil bath is changed to another desired value, and the entire process of measurements is repeated at the new temperature.

7) After completion of the highest temperature, a volumetric check is made at 100°F to determine any possible changes which have

occurred in the sample or apparatus during the run. The changes must amount to less than 0.2% or lie within the accuracy of the experimental results.

8) In order to obtain data in the low-pressure range, the sample is reduced to approximately one-eighth of its former size by removing a known weight of sample from the chamber by means of a weighing bomb technique. The sample size reduction must necessarily be done with the sample in a homogeneous state in order to avoid a change in composition of the sample. After the reduction of sample size, a check of the bubble-point pressure at 100°F is made to show that no change in composition has resulted. At each temperature, measurements are made with the small sample in the same manner as with the large sample, except that a lower pressure range is used.

The composition of coexisting phases in the propene-l-butene system was determined by removing a sample of dew-point gas at a given equilibrium pressure and temperature from the PVT chamber and analyzing the sample. Various methods of analyzing the composition of gaseous samples of 1-butene and propene were investigated including the use of a mass-spectrometer (14)(15). Four different mixtures of propene and 1-butene were prepared with known compositions and were used to test the accuracy possible with a mass-spectrometer analysis. Of the four mixtures analyzed with the mass-spectrometer of the General Petroleum Corporation, Torrance, California, two analyses agreed within 0.1% of the known compositions. The other two analyses deviated by approximately 1% from the known compositions, and the reproducibility of the analyses varied over a range of several per cent. The Consolidated

Engineering Corporation, Pasadena, California, advised that analysis accuracies of the order of 0.1-0.2% could be obtained for approximately equimolal mixtures only with difficulty and by use of special techniques. As these facts discouraged the use of the mass spectrometer, it was decided to employ a gas density method which had proven successful in this laboratory in the analysis of dew-point gas for the methanepropane system.

Samples of propene and 1-butene were added to the PVT chamber by weighing bomb techniques, with the composition of the mixture adjusted to lie somewhere in the two-phase region at the prescribed pressure and temperature. After equilibrium had been attained in the PVT chamber as shown by constancy of pressure and volume readings, the equilibrium pressure was recorded; approximately a one-gram sample of dew-point gas was withdrawn from the chamber and throttled into an evacuated 500 milliliter glass sample bulb, as shown schematically in Figure 1. During the withdrawal of the sample, the phase equilibrium within the chamber must not be disturbed and the equilibrium pressure must be maintained. Withdrawals were made with the agitator within the chamber turned off, and the period of time required for withdrawal was kept at a minimum. The displacement pressure of the dew-point gas was maintained at a relatively constant value during a withdrawal through the use of an auxiliary air chamber of approximately two cubic feet capacity. This vessel was connected to the air chamber of the PVT apparatus, and the pressure adjusted to the equilibrium value desired for the withdrawal. The relatively small change in volume of the total system caused by the withdrawal of the sample resulted in variations in pressure of less than three pounds per square

inch from the equilibrium value. It is believed that the withdrawal technique did not cause significant changes in the composition of the dew-point gas from the equilibrium conditions. The volumes of the glass sample bulbs had been determined by previous calibrations with pure hydrocarbons. The estimated uncertainty in volume was within 0.15%. The pressure of the gas in the sample bulbs was approximately one atmosphere and was measured by means of a mercury manometer and a cathetometer to within±.02 centimeters of mercury. The sample bulbs were brought to a constant temperature in a box through which air was circulated at room temperature. After a constant temperature had been reached by the sample bulb as shown by a mercury-in-glass thermometer calibrated to 0.1°F, values of pressure and temperature were recorded for the gas sample and the bulb stopcock closed. Duplicate samples of dew-point gas were withdrawn for each phase analysis.

The density of the gas mixture in the sample bulb was determined with a Christian-Becker analytical balance of the chainomatic type and with calibrated stainless steel weights. The method of substitution was employed in all weighings. That is, the calibrated weights and sample bulb were placed on the same pan of the balance and a tare weight was placed on the other pan. After the evacuated weight of the sample bulb had been increased by the weight of the sample, an equivalent weight had to be removed from that pan since the same tare weight was being used for both weighings. Errors due to unequal balance arm lengths were cancelled out in this weighing procedure. An identical glass sample bulb filled with air at atmospheric pressure was used as a tare weight to eliminate buoyancy corrections. The tare bulb was handled and conditioned in exactly the same manner as the sample bulbs

in order to compensate for conditioning errors. From the known PVT properties of propene and 1-butene and the weight of sample, the composition of the dew-point gas could be determined. This method of calculation is described in detail in the appendix and did not make use of the assumption of ideal solutions. The average value obtained from the duplicate analyses was the one reported. It is believed that the experimental results have an accuracy within 0.25%. As a check on the method, analyses of dew-point gas of a known composition were made with agreement within 0.2%.

IV. EXPERIMENTAL RESULTS

The volumetric properties of the propene-1-butene system in the single phase region are presented in Table I. Four experimental mixtures were employed for gathering data for the system. The experimental data for the 17.050, 33.153, and 69.050 mole % 1-butene mixtures were obtained by Farrington (6). After the fourth mixture had been completed, Farrington's data were rechecked and smoothed against the composition of the system to assure consistency among all mixtures and the pure components. This procedure resulted in minor corrections to the data tabulated in Farrington's thesis and in addition allowed his data to be augmented in the low-pressure region.

The experimental results for the 81.739% 1-butene mixture were obtained by the author. The volumetric data in the liquid region were smoothed against pressure and temperature in a manner similar to that described by Farrington (6). After the results for the mixture were consistent, smoothing against composition of the system was employed. In the dew-point and attenuated-gas region the experimental data were used to construct isothermal curves on residual volume-pressure plots for each experimentally studied mixture. The isotherms were extrapolated to zero pressure. The values of residual volume obtained at zero pressure were smoothed by the use of a method attributed to Dr. R. H. Olds, formerly of this laboratory. This method makes use of equations of the following form:

> At P = 0 : 1) $\nabla = \frac{\Delta}{T} + \beta$ 2) $\nabla = An_{E}^{2} + Bn_{E} + C$

Where \checkmark and β are empirical coefficients dependent upon the composition of the system; A, B, and C are empirical coefficients dependent upon the temperature of the system.

From smooth isothermal curves joining the V values at zero pressure with the experimentally determined values at higher pressures, the volumetric behavior of the mixtures at intervening pressures were determined. All experimental data were obtained at irregular pressures and have been interpolated to even values of pressure for convenience in use. The graphical methods employed were carried out on 50 x 75 centimeter size millimeter coordinate paper with scales chosen consistent with the accuracy of the data. It is believed that no uncertainties greater than 0.1% were introduced by these methods and that the smoothing operations should have the effect of increasing, rather than decreasing, the accuracy of the data. The accuracy of the data in the single phase region is thought to be of the order of 0.2% except in the vicinity of the critical region where an added uncertainty of as much as 0.1% may be expected. Figure 2 shows the effect of change of composition within the system on the relation of compressibility factor to pressure.

Values of specific volume and compressibility factor within the heterogeneous region of the 81.739 mole % 1-butene mixture are presented in Table II. Isothermal curves of compressibility factor versus pressure were used for smoothing the data and for making interpolations to even values of pressure. Experience has shown the compressibility factor to be of the most value in relating volumetric properties within the two-phase region. Because the data in the twophase region could not be smoothed against temperature, greater un-

certainties may be expected in the two-phase region than in the singlephase region. Also the scattering of experimental data was greater in the two-phase region than in the single-phase region, which fact indicates difficulty in attaining equilibrium in the time allowed. It is thought that the recorded values of two-phase specific volume may involve uncertainties up to 0.5%.

Table III lists the experimental coexisting-phase data obtained from the volumetric studies and from the dew-point gas analyses. It is of interest to note that for the 81.739 mole % 1-butene mixture the phenomenon of retrograde dew-point was observed at 280°F. The values of bubble-point pressure and volume were determined from the volumetric data by the method described by Sage, Backus, and Lacey (16), and the dew-point values were obtained by a similar method employing the abrupt discontinuity which occurs with the compressibility factor at the dew point. The properties of coexisting liquid and gas phases in the propene-1-butene system are presented in Table IV. These properties have been interpolated to correspond with even values of pressure for convenience in use.

In cases where experimental results were not available, graphical methods were employed to obtain the necessary values from other experimental data. Volumetric values for the pure components at 250°F were obtained by graphical interpolation between 220° and 280°F values. The vapor pressures of 1-butene at 40°F and 70°F were obtained from the literature (5), and the volumes of bubble-point liquid at these temperatures were obtained by extrapolation of isothermal curves on volume-pressure plots and checked by cross plotting against temperature and against composition of the system. Approximate values of compress-

ibility factor at 40°F and 70°F were obtained for the dew-point gas of 1-butene by extrapolation of the isothermal curves of pressure versus compressibility factor for the pure substance. These values of compressibility factor were checked by cross plotting against temperature and against composition of the system. Values of residual volume were calculated from the compressibility factors by means of the equation:

$$\underbrace{V}_{P} = (1 - Z) \underbrace{bT}_{P}$$

The dew-point locus for 1-butene was drawn on a pressure- \underline{V} plot and extrapolated to values of \underline{V} at 70°F and 40°F. These extrapolated values of \underline{V} had to agree with the values of \underline{V} calculated from the above equation. By working back and forth between Z and \underline{V} plots, consistent values were obtained for the dew points at 40°F and 70°F. Because of the high sensitivity of the residual volume function, it was thought that satisfactory accuracy was obtained.

The dew-point properties of all mixtures at 40°F, of all mixtures except the 17.050% mixture at 70°F, and of the 81.739% mixture at 100°F had to be determined by graphical methods. The dew-point pressures were obtained from isothermal curves on pressure-composition plots and checked on a pressure-temperature diagram. Values of dew-point compressibility factor were derived by plotting diagrams of Z versus pressure and Z versus temperature for each mixture and by cross plotting against composition. The three plots were made mutually consistent and values of residual volume were calculated from the compressibility factor values. The dew-point locus for each mixture was plotted on a pressure-V diagram and extrapolated to the value at 40°F. The procedure used in obtaining consistent values of Z and of V was similar to the one employed with pure 1-butene.

All experimental coexisting-phase data were plotted as isothermal curves on pressure-composition diagrams as illustrated in Figure 3. Cross plots were made of temperature-composition at pressures of 50, 100, 200, 300, 500, 588, and 610 pounds per square inch absolute, and also of pressure-temperature for the experimental compositions used. Figures 4 and 5 show these diagrams. Smooth curves were obtained with all plots, which showed that the data were consistent. Values of the gas-liquid equilibrium constant (K = y) were calculated from bubblepoint and dew-point compositions at various selected pressures which were taken from the pressure-composition plots. Figure 6 shows a plot of PK versus P for propene and 1-butene. The product of pressure and equilibrium constant was chosen as a coordinate in order to provide a magnified scale for the plotting of equilibrium constants. The PK versus P plot has been smoothed in conjunction with the curves on the pressure-composition diagram so that the two plots are mutually consistent. The smoothing of the above-mentioned curves also resulted in a small amount of additional smoothing performed on the temperaturecomposition and pressure-temperature plots to make all diagrams consistent.

Isothermal curves on specific volume-composition plots were constructed which allowed values of specific volume to be obtained for any desired composition of bubble-point liquid or dew-point gas.

The properties in the critical region have been estimated since insufficient experimental data were available within this region. These properties are presented in Table V. It is believed that the critical envelope of the system was established within 1% uncertainty.

The critical values of propene and 1-butene were available from the literature (7)(1), and the critical pressure at 280°F was known within narrow limits. The critical envelope could be drawn through these points on the pressure-temperature diagram as a smooth curve. This critical locus determined points by intersection at 220°F and 250°F. The dew-point and bubble-point curves were extrapolated on the pressurecomposition and pressure-temperature diagrams, keeping the curves mutually consistent at all times. This extrapolation on the pressuretemperature diagram determined the critical points of the mixtures within narrow limits. Plots of P versus Z and Z versus composition were constructed to aid in further delineating the critical region. Critical volumes of the mixtures were obtained by applying the rule of rectilinear diameters (17) to each mixture. The loci of the critical volumes plotted versus temperature and versus composition were in the form of smooth curves.

Each cricondentherm, or value of maximum temperature at which two coexisting phases occur for a given mixture composition, was obtained by drawing in a smooth locus on the pressure-temperature diagram. The cricondentherm volumes were obtained from the density versus pressure plots constructed for use with the method of rectilinear diameters.

The propene-1-butene system results may be compared with calculated ideal values. The deviations of the actual bubble-point pressures of mixtures from predictions by Raoult's Law are shown at 160°F in Figure 7. From the assumptions of Raoult's and Dalton's Laws, the following "ideal vapor pressure" is obtained:

 $P''_{r} = x_{3}P''_{3} + x_{4}P''_{4}$

$$\underline{\mathbf{P}}^{\mathbf{n}} = \mathbf{P}_{\mathbf{r}}^{\mathbf{n}} - \mathbf{P}^{\mathbf{n}}$$

The percentage deviation of actual specific volumes from those volumes calculated on the basis of ideal solutions is presented in Figure 8 for pressures of 100, 600, and 10,000 pounds per square inch absolute at 160°F. The ordinate for this figure is defined by the equation:

% deviation
$$(V_{ideal} - V)(100)$$

Videal

The values of V_{ideal} are given by the relation:

$$V_{ideal} = x_3V_3 + x_4V_4$$

It is interesting to note that the liquid mixtures at 10,000 pounds per square inch are more nearly ideal solutions than are the gaseous mixtures at 100 pounds per square inch.

Equilibrium constant values may be calculated from consideration of Raoult's and Dalton's Laws which may be combined to give:

> (1) $x_k P_k^n = y_k P$ or (2) $K_k = \frac{y_k}{x_k} = \frac{P_k^n}{P}$

> > and

(3)
$$PK_k = P_k^n$$

Equation (3) indicates that for a given temperature the calculated value of PK_k will be equal to the vapor pressure of the pure component. A horizontal line for each temperature and for each component will result on the PK versus P plot shown in Figure 6.

Hadden (18) has presented values of ideal gas-liquid equilibrium constants for a number of hydrocarbons as a result of correlations of experimental data and fugacities. It is of interest to compare his ideal K values, read from a nomogram, for propene and 1-butene with the actual experimental values.

T	P	Experim	ental	Hadden	(18)
°F	PSI abs.	K3	K4	K ₃	K4
40	50	1.772	•485	2.00	.55
70	100	1.420	.439	1.61	.44
100	200	1.096	.43	1.20	.37
160	300	1.299	.619	1.37	.52
220	400	1.428	.834	1.60	.71
250	500	1.342	. 89 6	1.55	.74
280	600	1.172	.966	1.50	.75

The deviations from ideal behavior shown above for the system are between 0 - 28%. As pressures approach the critical region, ideal equilibrium constants become less valid.

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V. NOMENCLATURE
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b = specific gas constant = $\frac{R}{M}$, (lb/in²)(ft³/lb)/^OR R = 10.73185 $M_3 = 42.079$ $M_4 = 56.105$ Propene b = 0.25504Mixture containing 17.050% 1-butene b = 0.24133 Mixture containing 33.153% 1-butene b = 0.22966 Mixture containing 69.050% 1-butene b = 0.20732 Mixture containing 81.739% l-butene b = 0.20043 1-Butene b = 0.19128 $K = gas-liquid equilibrium constant = \frac{y}{x}$ n = mol fraction of a component P = pressure, lb./sq. in. abs. P"= residual vapor pressure, 1b./sq. in. abs. P"= vapor pressure of pure component at a given temperature, lb./sq. in. abs. P":= reference vapor pressure, lb./sq. in. abs. T = absolute temperature, °F absolute, °R V = specific volume, cu. ft./1b. $V = residual volume = \frac{bT}{D} - V$, cu. ft./lb. x = mol fraction of a component in liquid phase y- mol fraction of a component in gas phase $Z = \text{compressibility factor} = \frac{PV}{NT}$

Subscripts

3 refers to propene 4 refers to 1-butene

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Figure 2. Compressibility Factor for the Propene-l-Butene System at 280°F.



Figure 3. Pressure-Composition Diagram for the Propene-1-Butene System



Figure 4. Temperature-Composition Diagram for the Propene-1-Butene System



Figure 5. Pressure-Temperature Diagram for the Propene-1-Butene System



Figure 6. Equilibrium Constants for Propene and 1-Butene in the Propene-1-Butene System





Deviation of Actual Specific Volume From Ideal Solution for Fropene-1-Butene Mixtures at 160°F

TABLE I. Single-Phase Volumetric Behavior of Four Experimental Mixtures of Propene-1-Butene

Temperature 40° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	1.815 (60.0) ^a	0.903	2.3155 (45.6)	0.9201
B. P.	0.02874 (82.8)	0.0197	0.02814 (70.5)	0.1729
0		1.000		1.000
14.7	8.039	0.9796	7.627	0.9768
20	5.860	0.9719	5.554	0.9679
30	3.845	0,9565	3.635	0,9502
40	2.8336	0,9399	2.6714	0,9311
50	2.2238	0,9220		
60				
80		and and	0.02804	0.0196
100	0.02877	0.0239	0.02802	0.0244
125	0,02875	0,0298	0.02800	0.0305
150	0.02873	0.0357	0.02799	0.0366
200	0.02870	0.0476	0.02796	0,0487
300	0.02863	0.0712	0.02790	0.0729
400	0.02857	0.0948	0.02785	0.0971
500	0.02850	0.1182	0.02779	0.1211

^aFigures in parentheses are dew-point or bubble-point pressures expressed as pounds per square inch.

Temperature 40° F

Mole Fraction 1-Butene as Follows:-0.17050 0.33153

Pressure Lb/Sq In Absolute		Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	ł	Compress- ibility Factor
600		0.02844	0.1415	0.02774		0.1450
800	4	0.02831	0.1878	0.02763		0.1926
1000		0.02820	0.2339	0.02752		0.2398
1250		0.02806	0.2909	0.02741		0.2986
1500		0.02792	0.3473	0.02730		0.3568
1750		0.02780	0.4034	0.02719		0.4146
2000		0.02768	0.4591	0.02708		0.4719
2250		0.02756	0.5142	0.02698		0.5290
2500		0.02744	0,5689	0,02688		0.5856
2750		0.02733	0.6232	0.02678		0.6417
3000		0.02724	0.6777	0.02670		0.6980
3500		0.02703	0.7845	0.02652		0.8088
4000		0.02683	0.8900	0.02634		0.9181
4500		0,02665	0.9945	0,02616		1.0258
5000		0.02647	1.0975	0.02600		1.1328
6000	·	0,02615	1.3011	0.02570		1.3437
7000		0.02586	1.5011	0.02545		1,5524
8000		0.02561	1.6990	0.02518		1.7553
9000		0.02537	1.8934	0.02495		1,9567
10000	a.	0,02516	2.0864	0.02475		2.1567

Temperature 40° F

Mole Fraction 1-Butene as Follows: 0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	3.280 (29.7)	0.9403	3.626 (26.1)	0.945
B. P.	0.02695 (43.6) 0.0113	0.02659 (34.9)	0,0093
0		1.000	5m2 2+2	1.000
14.7	6,848	0.9713	6.609	0.9698
20	4.976	0,9606	4.799	0,9584
30		Start (+4)	84114	and set
40		654 FM	0.02659	0,0106
50	0.02695	0.0130	0.02658	0.0133
60	0.02694	0.0156	0.02657	0,0159
80	0,02692	0,0208	0.02656	0,0212
100	0.02690	0,0260	0.02654	0.0265
125	0.02687	0.0324	0.02653	0,0331
150	0.02685	0,0389	0.02651	0.0397
200	0.02680	0.0517	0.02647	0.0529
300	0.02675	0.0775	0.02643	0.0792
400	0.02667	0,1030	0.02637	0.1053
500	0.02662	0,1285	0.02633	0.1315
600	0.02657	0.1539	0,02628	0.1574

Temperature 40° F

Mole Fraction 1-Butene as Follows: -0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.02648	0.2045	0.02619	0,2092
1000	0,02640	0.2548	0.02612	0,2608
1250	0.02630	0,3173	0,02601	0.3246
1500	0.02619	0,3792	0.02591	0,3881
1750	0.02610	0.4409	0.02583	0,4513
2000	0,02601	0,5021	0,02576	0.5144
2250	0.02594	0,5634	0,02569	0.5772
2500	0.02586	0.6240	0.02561	0,6393
2750	0.02579	0.6846	0.02554	0,7013
3000	0.02571	0.7445	0.02546	0.7627
3500	0.02557	0.8639	0.02531	0,8845
4000	0.02542	0.9815	0.02515	1.0045
4500	0.02528	1,0981	0.02500	1.1233
5000	0.02514	1.2133	0.02487	1.2416
6000	0.02488	1.4409	0.02461	1.4744
7000	0.02465	1.6655	0.02442	1.7068
8000	0.02445	1.8880	0.02424	1,9363
9000	0.02426	2.1075	0.02404	2.1604
10000	0.02410	2,3263	0.02390	2.3864

Temperature 70° F

Mole Fraction 1-Butene as Follows: 0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	1.060 (103.6)	0.859	1,363 (78,8)	0.8830
B. P.	0.03013 (130.6)	0.0308	0.02942 (111.3)	0.0269
0	2009 Start	1.000	part90	1.000
14.7	8.551	0.9830	8.118	0,9806
20	6.243	0.9767	5.921	0.9734
30	4.110	0.9645	3.891	0,9595
40	3.042	0,9519	2.8743	0.9451
50	2.4000	0,9387	2.2628	0,9300
60	1.9711	0.9252	1,8539	0,9144
80	1.4321	0.8962	द्वाला १४४६	Bigd
100	1.1057	0.8650	D mna	and and
125	and \$50	6m (60)	0.2941	0.0302
150	0.03013	0.0354	0.02939	0,0362
200	0.03010	0.0353	0,02935	0.0483
300	0.02998	0.0704	0.02925	0.0721
400	0,02990	0.0936	0.02916	0.0959
500	0.02981	0.1166	0.02907	0,1195
600	0.02971	0.1395	0,02899	0.1430

Temperature 700 F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.02955	0.1849	0,02883	0,1896
1000	0.02938	0,2298	0.02866	0,2356
1250	0,02919	0.2854	0.02848	0,2926
1500	0.02900	0,3403	0.02830	0.3490
1750	0.02883	0.3947	0.02815	0,4050
2000	0.02867	0,4486	0.02800	0.4603
2250	0.02850	0,5016	0.02785	0.5151
2500	0.02835	0,5544	0.02773	0,5617
2750	0.02821	0,6069	0.02761	0.6241
3000	0.02808	0.6590	0.02750	0,6782
3500	0.02784	0.7623	0.02729	0.7852
4000	0.02763	0.8646	0.02710	0.8911
4500	0.02743	0,9656	0.02691	0.9954
5000	0.02725	1.0659	0.02675	1.0995
6000	0,02690	1,2626	0.02641	1,3026
7000	0.02659	1,4561	0.02610	1.5018
8000	0.02630	1.6459	0.02579	1,6960
9000	0.02602	1.8320	0.02553	1.8883
10000	0.02574	2.0136	0.02530	2.0797

Temperature 70° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	1.9702 (50.6)	0.9078	2.158 (45.0)	0.914
B. P.	0.02795 (70.9)	0.0180	0.02760 (57.4)	0.0149
0	tentagen a	1.000	SHERM	1.000
14.7	7.292	0,9758	7.039	0.9743
20	5,308	0,9666	5.121	0,9646
30	3,473	0,9488	3.346	0,9456
40	2,5527	0.9298	2.4560	0,9253
50	1.9976	0.9095	den di i	Quel (grav)
60	and find	sari dent	and we	2nabang
80	0.02795	0,0204	0.02757	0,0208
100	0.02793	0,0254	0.02755	0.0259
125	0.02791	0.0318	0.02753	0,0324
150	0.02790	0.0381	0.02751	0.0389
200	0.02786	0.0507	0.02746	0,0517
300	0.02780	0.0759	0.02740	0.0774
400	0.02774	0.1010	0.02733	0.1030
500	0.02767	0.1260	0,02726	0.1284
600	0.02760	0.1508	0.02722	0.1538

Temperature 70° F

Mole Fraction 1-Butene as Follows:-0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.02749	0,2003 .	0.02710	0.2042
1000	0.02737	0.2492	0.02700	0.2543
1250	0.02723	0.3099	0.02688	0,3165
1500	0.02710	0.3702	0.02677	0.3782
1750	0.02697	0.4298	0.02666	0.4394
2000	0.02685	0,4890	0.02656	0,5003
2250	0.02674	0.5479	0.02646	0,5608
2500	0.02664	0.6064	0.02636	0,6207
2750	0.02653	0.6643	0,02627	0.6804
3000	0.02644	0,7223	0.02616	0.7392
3500	0.02626	0.8369	0.02600	0,8571
4000	0.02610	0.,9506	0.02584	0.9735
4500	0,02595	1.0633	0.02569	1.0889
5000	0,02580	1.1746	0.02554	1.2028
6000	0.02550	1.3932	0.02524	1,4264
7000	0.02523	1,6082	0,02500	1.6483
8000	0.02499	1,8204	0.02476	1.8657
9000	0.02476	2.0291	0.02455	2.0811
10000	0,02456	2,2364	0.02436	2.2944

Temperature 100° F

Mole Fraction 1-Butene as Follows: -0.17050 0.33153

P L A	ressure b/Sq In bsolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
	D. P.	0.6767 (161.4)	0.8086	0.8752 (124.4)	0.847
	B. P.	0.03185 (195.3)	0.0461	0.03090 (166.9)	0.0401
	0	gand over 1	1.000	and land	1.000
	14.7	9,058	0,9856	8.604	0.9837
	20	6,621	0,9803	6.285	0.9778
	30	4.369	0.9704	4.142	0,9666
	40	3,243	0,9603	3,070	0,9554
	50	2,5667	0.9501	2,4268	0,9440
	60	2.1157	0.9398	1.9974	0.9324
	80	1,5507	0.9184	1,4595	0,9083
	100	1,2100	0,8958	1.1346	0.8827
	125	0.9344	0.8647	Geology	2003 (2019)
	150	0.7458	0.8282	suite-it	years Devi
	200	0.03184	0.0471	0.03085	0,0480
	300	0.03170	0.0704	0,03073	0.0717
	400	0.03156	0.0935	0.03061	0.0953
	500	0.03142	0,1163	0,03050	0,1186
	600	0.03129	0,1390	0,03039	0.1419

Temperature 100° F

-Mole Fraction 1-Butene as Follows: -0.17050 0.33153 Sp Volume Compress-Sp Volume Compress-Pressure Cu Ft/Lb Cu Ft/Lb Lb/Sq In ibility ibility Absolute Factor Factor 800 0.03104 0.1838 0,03017 0.1878 0.03081 1000 0.2281 0.02997 0.2332 1250 0.03055 0.2827 0.02974 0.2892 1500 0.03030 0.3365 0.02952 0.3445 1750 0.03007 0.3896 0.02931 0.3990 2000 0.02985 0.4420 0.02913 0,4532 2250 0.02965 0.4939 0.02895 0.5067 2500 0.02945 0.5451 0,02878 0.5597 0.02928 2750 0.5961 0.02863 0.6125 0.02847 3000 0.02911 0.6466 0.6645 3500 0.02882 0.7468 0.02820 0.7679 4000 0.02857 0.8461 0.02795 0.8698 0.02834 0.9442 0.02774 0.9711 4500 5000 0.02811 1.0406 0,02753 1.0709 6000 0.02770 1.2305 0.02715 1.2673 0.02734 1.4169 0.02679 7000 1.4589 0.02700 1,5992 0.02645 8000 1.6462 9000 0.02668 1.7777 0.02615 1.8309

1.9516

0.02586

2.0118

10000

Temperature 100° F

Mole Fraction 1-Butene as Follows:-0.69050 0.81739

Pressure Lb/Sg In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	1.2501 (80.8)	0.8705	1.3622 (72.3)	0.878
B. P.	0.02920 (108.4)	0.0273	0.02865 (89.4)	0.0228
0	400 GD7	1.000	sent jao	1.000
14.7	7.734	0.9796	7.467	0,9783
20	5.639	0.9720	5.442	0.9702
30	3,704	0.9576	3.570	0.9546
40	2.7344	0,9426	2.6319	0,9385
50	2,1511	0,9270	2.0674	0,9215
60	1.7604	0,9103	1.6888	0.9032
80	1.2652	0.8723	Bud wet	ano ant
100	Suite Server	1004 2014	0.02865	0.0255
125	0.02918	0.0314	0,02863	0,0319
150	0,02915	0.0377	0,02861	0.0383
200	0.02910	0.0502	0.02859	0.0510
300	0.02900	0.0750	0.02848	0.0762
400	0,02890	0.0996	0.02840	0.1013
500	0.02881	0.1241	0.02832	0,1262
600	0.02873	0.1486	0.02825	0.1511

Temperature 100° F

Mole Fraction 1-Butene as Follows: -0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.02856	0.1969	0.02810	0,2004
1000	0.02841	0.2449	0.02796	0.2492
1250	0.02824	0,3042	0.02782	0.3100
1500	0.02806	0,3628	0.02768	0.3701
1750	0.02790	0,4208	0.02753	0.4295
2000	0.02775	0,4783	0.02740	0.4885
2250	0.02761	0.5354	0,02726	0,5468
2500	0.02749	0,5923	0.02714	0.6048
2750	0.02737	0.6487	0.02703	0,6626
3000	0.02726	0.7049	0.02693	0.7202
3500	0.02705	0.8160	0.02674	0.8343
4000	0.02685	0,9256	0,02656	0.9470
4500	0.02667	1.0343	0.02638	1,0582
5000	0.02650	1.1419	0.02618	1,1669
6000	0.02616	1.3528	0.02588	1.3842
7000	0,02585	1,5595	0.02559	1.5968
8000	0.02558	1.7637	0.02534	1.8071
9000	0.02532	1.9640	0.02509	2.0129
10000	0.02508	2.1615	0.02488	2,2179

Temperature 160° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	0.2864 (346	.9) 0.6643	0.3709 (276.3)) 0.7200
B. F.	0.03705 (389	.7) 0.0965	0.03509(334.3)) 0.0824
0	prove-calind	1.000		1.000
14.7	10.068	0,9894	9,568	0,9880
20	7.369	0,9855	7.000	0.9837
30	4.876	0,9782	4.628	0,9755
40	3.630	0,9708	3.442	0.9673
50	2.8814	0.9634	2.7300	0,9591
60	2.3823	0,9558	2.2554	0.9508
80	1.7581	0,9405	1.6619	0,9342
100	1.3829	0.9247	1.3053	0,9172
125	1.0821	0.9045	1.0194	0,8953
150	0.8807	0.8834	0.8279	0.8726
200	0.6266	0.8379	0,5851	0,8222
300	0.3640	0.7302	ager (and	Qued 4-515
400	0.03698	0,0989	0.03483	0.0979
500	0,03646	0.1219	0.03448	0.1211
600	0.03601	0,1448	0,03417	0,1441

Temperature 160° F

Mole Fraction 1-Butene as Follows:-0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.03527	0.1887	0,03363	0.1890
1000	0.03466	0,2318	0.03318	0,2331
1250	0.03404	0,2845	0.03277	0,2878
1500	0,03351	0,3361	0.03236	0.3411
1750	0.03306	0.3869	0,03202	0.3937
2000	0.03267	0,4369	0.03167	0.4451
2250	0.03232	0,4863	0.03137	0.4959
2500	0.03201	0,5351	0.03110	0.5467
2750	0.03172	0.5833	0.03084	0.5959
3000	0.03146	0,6311	0,03059	0.6448
3500	0.03099	0,7253	0.03019	0.7424
4000	0.03059	0.8182	0.02984	0,8387
4500	0,03023	0.9096	0.02950	0,9328
5000	0.02991	1.0000	0.02920	1.0259
6000	0.02935	1.1775	0.02868	1.2091
7000	0.02886	1,3509	0.02824	1,3890
8000	0.02842	1.5203	0.02782	1.5638
9000	0.02802	1.6863	0.02742	1.7340
10000	0.02765	1.8489	0.02703	1.8992

Temperature 1600 F

-Mole Fraction 1-Butene as Follows:-0.69050 0.81739 Sp Volume Compress-Compress-Sp Volume Pressure Cu Ft/Lb ibility Cu Ft/Lb ibility Lb/Sq In Factor Factor Absolute D. P. 0.5428 (184.1) 0.7778 0.6009 (163.7) 0.7920 0.03233 (224.9) 0.0566 B. P. 0.03156 (190.6) 0.0484 0 1.000 1.000 ------8,612 0.9851 8,320 0.9843 14.7 20 6.293 0,9797 6.078 0,9876 4,152 0,9695 4.007 0.9678 30 3.081 0,9591 2,9713 0,9568 40 0.9486 2.3494 0,9457 50 2,4374 2,0084 0.9380 1,9346 0,9345 60 1.4148 0.9112 80 1.4712 0.9161 0.8933 1.1015 0,8868 100 1.1476 0.8628 0.8483 0.8537 125 0,8868 150 0.7133 0,8328 0.6755 0.8157 0,0508 0.03153 200 ------300 0.03215 0,0751 0.03133 0.0757 0.03192 0.0994 0.03115 0.1003 400 0.03099 0.1247 500 0.03173 0.1235 0.03084 0.1490 600 0.03153 0.1473

Temperature 160° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.03119	0.1942	0,03056	0,1968
1000	0,03092	0,2407	0,03033	0.2442
1250	0.03062	0,2979	0,03003	0.3022
1500	0.03031	0,3539	0.02977	0.3595
1750	0.03007	0,4096	0,02953	0.4160
2000	0.02983	0.4644	0.02931	0.4719
2250	0.02964	0,5191	0.02913	0,5277
2500	0.02945	0,5731	0.02895	0,5827
2750	0,02925	0,6261	0.02879	0.6374
3000	0.02907	0.6788	0.02863	0.6915
3500	0.02874	0,7830	0.02833	0,7983
4000	0.02843	0.8852	0.02805	0.9033
4500	0.02815	0,9860	0.02779	1,0068
5000	0.02790	1.0859	0.02755	1,1090
6000	0.02743	1.2811	0.02713	1,3105
7000	0.02703	1.4728	0,02675	1,5075
8000	0.02670	1,6626	0.02645	1,7036
9000	0.02638	1.8481	0,02614	1,8941
10000	0.02608	2,0300	0,02590	2.0852

Temperature 220° F

Pressure Lb/Sq Ir Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Vol Cu Ft/:	ume Līb	Compress- ibility Factor
D. P.	\$ud:000	gand s-da	0,1488	(543.7)	0,5183
B. P.	6 at 22 5	Since the g	0.0459	3 (594.5)	0.1751
0	tona dana	1.000	Swat strig		1.000
14.7	11.073	0.9921	10,527		0,9911
20	8.113	0,9892	7.710		0,9879
30	5.379	0.9838	5,109		0,9818
40	4.012	0,9783	3,808		0.9757
50	3,191	0.9728	3.027		0,9696
60	2.6442	0,9672	2,5067		0,9635
80	1,9601	0,9560	1,8560		0.9512
100	1.5493	0,9445	1.4654		0,9388
125	1,2203	0,9300	1.1526		0,9230
150	1.0007	0,9151	0,9439		0,9070
200	0.7254	0,8844	0,6822		0,8741
300	0,4478	0,8189	0.4173		0,8020
400	0.3054	0.7447	0,2792	5	0.7156
500	0.2158	0.6577	0.1862	C	0,5964
600	0.1478	0,5406	0,0457	C	0.1757

Temperature 220° F

Mole Fraction 1-Butene as Follows: 0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.04681	0.2283	0,04090	0,2096
1000	0.04242	0,2586	0.03903	0,2500
1250	0,03992	0.3042	0.03745	0.2999
1500	0.03844	0,3515	0.03650	0,3507
1750	0.03743	0,3993	0.03569	0,4001
2000	0,03658	0,4460	0.03502	0.4487
2250	0.03538	0,4922	0.03441	0.4960
2500	0.03530	0.5380	0.03396	0,5439
2750	0,03480	0,5834	0,03352	0,5906
3000	0.03435	0.6282	0.03313	0.6367
3500	0.03357	0,7163	0.03247	0.7280
4000	0.03293	0.8030	0.03191	0.8177
4500	0.03236	0.8878	0.03143	0,9061
5000	0.03187	0,9715	0.03100	0,9930
6000	0.03106	1,1361	0,03028	1.1639
7000	0.03042	1,2982	0,02971	1,3323
8000	0.02986	1.4563	0.02921	1.4970
9000	0.02936	1.6109	0.02870	1.6547
1 0000	0.02893	1.7637	0,02828	1.8117

Temperature 220° F

Mole Fraction 1-Butene as Follows: ~ 0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	0.2458 (365.4)	0,6375	0.2794 (324.2)	0,6650
B. P.	0.03777 (413.1)	0.1107	0.03622 (357.3)	0.0950
0	يەت مەت 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100 - 100	1.000	Guid unes	1,000
14.7	9#483	0,9891	9.163	0,9885
20	6,940	0,9851	8.704	0,9843
30	4,592	0,9776	4,434	0,9763
40	3,417	0.9699	3,298	0,9684
50	2.7122	0.9624	2.6165	0.9603
60	2.2422	0.9547	2.1621	0,9523
80	1.6543	0 * 9392	1,5935	0.9358
100	1.3011	0.9234	1.2517	0,9188
125	1.0180	0,9030	0,9776	0.8970
150	0.8286	0.8821	0.7940	0.8743
200	0,5902	0.8376	0,5618	0,8247
300	0.3441	0,7326	0,31.86	0,7016
400	6-val (2009	duer loci	0.03595	0.1056
500	0.03699	0,1313	0.03543	0,1300
600	0.03640	0.1550	0,03498	0.1541

Temperature 220° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.03544	0.2012	0.03426	0,2012
1000	0.03470	0,2463	0,03368	0.2472
1250	0.03400	0,3016	0,03308	0,3035
1500	0,03340	0.3555	0,03256	0,3585
1750	0,03290	0,4086	0,03213	0,4127
2000	0.03246	0.4607	0.03175	0,4661
2250	0.03208	0,5122	0.03141	0.5188
2500	0.03173	0,5629	0.03110	0.5707
2750	0.03141	0.6130	0.03083	0.6223
3000	0.03113	0,6628	0.03059	0.6736
3500	0,03062	0.7606	0,03013	0.7741
4000	0.03018	0,8567	0.02973	0,8729
4500	0.02979	0.9514	0.02937	0.9702
5000	0.02945	1,0450	0,02905	1.0662
6000	0.02886	1.2289	0.02850	1,2552
7000	0.02835	1.4083	0.02801	1.4393
8000	0,02793	1.5857	0.02760	1.6208
9000	0.02753	1.17584	0.02724	1.7996
10000	0.02715	1,9268	0,02687	1.9724

Temperature 250° F

Mole Fraction 1-Butene as Follows:-0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	vide (200	0m9 2-00	the same	Sure autor
B. P.	diver year	gauge Webse	P4864	
0	gung dant	1.000	8×0 9×0	1,000
14.7	11.575	0,9932	11.006	0.9923
20	8,484	0.9907	8.064	0.9895
30	5.629	0.9860	5.348	0.9843
40	4.202	0.9813	3,989	0,9790
50	3,345	0,9766	3.174	0.9737
60	2.7742	0.9719	2,6308	0,9685
80	2.0602	0,9623	1.9514	0.9578
100	1.6316	0,9526	1.5437	0.9471
125	1,2886	0,9404	1.2174	0,9337
150	1.0597	0.9281	0,9998	0,9201
200	0.7731	0.9027	0.7274	0.8925
300	0,4849	0.8494	0,4530	0,8338
400	0,3390	0.7917	0,3134	0.7691
500	0,2494	0,7282	0,22518	0.6908
600	0.1873	0.6560	0,16105	0,5929

Temperature 250° F

Mole Fraction 1-Butene as Follows: 0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.09743	0,4551	0.05629	0,2763
1000	0,05405	0,3156	0,04529	0.2779
1250	0.04579	0,3342	0.04157	0.3188
1500	0.04250	0.3722	0.03957	0.3642
1750	0.04070	0.4159	0,03818	0,4099
2000	0.03935	0,4595	0.03719	0.4563
2250	0.03823	0.5022	0.03644	0,5030
2500	0,03740	0,5459	0*03578	0,5488
2750	0.03670	0.5893	0.03522	0.5942
3000	0.03609	0,6322	0.03471	0,6389
3500	0.03509	0,7171	0.03386	0.7271
4000	0.03426	0.8001	0,03315	0,8135
4500	0.03358	0,8823	0.03255	0.8987
5000	0.03300	0,9634	0.03202	0,9823
6000	0.03200	1.1210	0.03116	1.1471
7000	0.03123	1.2764	0,03050	1.3099
8000	0.03061	1.4298	0,02993	1.4690
9000	0.03009	1.5812	0,02941	1,6240
10000	0.02960	1.7283	0.02892	1.7743

Temperature 250° F

Mole Fraction 1-Butene as Follows:-0.69050 0.81739

 Pressure Lb/Sq In Absolute	Sp Volum Cu Ft/Lh	ne D	Compress- ibility Factor	Sp Volum Cu Ft/Li	ne D	Compress- ibility Factor
D. P.	0.1560	(497.7)	0,5278	0.1827	(442.0)	0,5678
B. P.	0.04356	(540.8)	0.1601	0.04050	(472.5)	0.1345
0	Start cult		1,000	र्थ्याल स्थलन		1.000
14.7	9,918		0,9906	9,583		0,9901
20	7.263		0.9872	7,016		0,9865
30	4.810		0,9808	4.645		0.9797
40	3,584		0,9743	3,460		0.9729
50	2.8477		0.9677	2,7481		0,9660
60	2.3570		0.9612	2.2737		0.9591
80	1.7432		0.9479	1.6802		0.9450
100	1.3747		0.9343	1,3238		0,9307
125	1.0794		0.9171	1.0381		0.9123
150	0.8822		0.8994	0.8471		0.8933
200	0.6345		0.8624	0.6064		0.8526
300	0.3827		0.7804	0,3603		0,7600
400	0.24953		0.6784	0.22710		0,6386
500	Quil enve		834 8-4	0.04000		0.1406
600	0,04193		0,1710	0.03885		0,1639

Temperature 250° F

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0,03906	0,2124	0.03725	0,2095
1000	0.03758	0.2451	0.03619	0,2544
1250	0.03641	0.3093	0.03520	0.3093
1500	0,03550	0.3619	0.03443	0,3631
1750	0.03476	0,4134	0.03383	0.4162
2000	0.03414	0.4641	0.03332	0.4685
2250	0.03361	0,5140	0.03287	0.5199
2500	0.03315	0,5633	0.03246	0.5705
2750	0.03273	0.6118	0,03211	0.6208
3000	0.03236	0.6598	0.03179	0.6705
3500	0.03173	0,7548	0.03120	0.7677
4000	0.03119	0,8480	0.03070	0.8633
4500	0.03072	0,9396	0.03026	0.9573
5000	0,03031	1,0300	0.02989	1.0507
6000	0.02963	1,2083	0.02925	1.2338
7000	0.02905	1.3821	0.02867	1.4109
8000	0,02856	1,5529	0.02819	1.5855
9000	0.02813	1.7207	0.02778	1.7577
10000	0.02775	1.8861	0.02740	1,9263

Temperature 280° F

-Mole Fraction 1-Butene as Follows:-0.17050 0.33153 Pressure Sp Volume Compress-Sp Volume Compress-Lb/Sq In Cu Ft/Lb ibility Cu Ft/Lb ibility Factor Absolute Factor D. P. 0 1.000 1.000 ----Shell Hidd 0,9934 12.075 0,9941 11.483 14.7 20 8,854 0.9919 8.418 0,9910 30 5,878 0,9879 5.586 0.9865 40 4.391 0,9838 4.171 0,9820 3.498 50 0,9797 3.321 0.9775 2,9025 60 0.9756 2.7548 0.9730 80 2.1583 0.9672 2.0469 0.9639 100 1.7115 0,9588 1.6221 0.9549 125 1.3539 0,9480 1.2820 0.9433 150 1,1153 0,9371 1,0553 0,9318 200 0.8167 0.9150 0.7714 0,9082 300 0.5168 0.8686 0,4864 0.8589 0.3424 0.8062 400 0.3658 0.8196 500 0.27392 0.7672 0.25416 0,7481 600 0.21182 0.7120 0.19313 0.6821

Temperature 280° F

Mole Fraction 1-Butene as Follows:-0.17050 0.33153

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.13174	0,5904	0.10896	0,5131
1000	0,08233	0.4612	0,06172	0,3633
1250	0.05595	0.3915	0.04835	0.3558
1500	0.04839	0.4066	0.04403	0.3888
1750	0,04473	0.4385	0,4164	0,4290
2000	0.04261	0.4774	0.04001	0.4710
2250	0,04099	0,5166	0,03891	0,5153
2500	0.03973	0.5565	0.03792	0.5580
2750	0.03882	0,5980	0.03713	0.6011
3000	0,03810	0,6403	0.03645	0.6437
3500	0.03677	0.7209	0.03533	0,7279
4000	0.03570	0.8000	0.03444	0,8109
4500	0.03483	0,8780	0.03370	0.8927
5000	0.03411	0,9554	0,03308	0.9736
6000	0,03298	1,1085	0.03206	1.1323
7000	0.03209	1.2584	0.03128	1.2889
8000	0.03138	1,4063	0.03064	1.4429
9000	0.03077	1,5513	0.03006	1,5925
10000	0.03025	1.6946	0,02953	1.7383

Temperature 280° F

Mole Fraction 1-Butene as Follows: 0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
D. P.	Send Aller	144 m2	0.0715 (603.5)	0.291
geogra www.	Genty shate	9520-0340	0.1015 (590) ^b	0,404
0	- and \$500	1.000	245-460	1,000
14.7	10,351	0,9920	10.003	0,9915
20	7,583	0,9890	7.327	0.9884
30	5.027	0,9835	4.856	0,9826
40	3.749	0,9779	3.620	0.9767
50	2,9820	0,9723	2,8786	0,9708
60	2,4705	0,9666	2,3841	0,9648
80	1.8309	0,9551	1,7657	0.9527
100	1.4469	0,9435	1,3942	0.9404
125	1.1394	0,9288	1.0967	0,9246
150	0,9340	0.9136	0.8980	0,9085
200	0.6767	0,8825	0.6485	0.8748
300	0.4170	0.8157	0.3958	0.8009
40 0	0.28368	0.7400	0,26465	0.7141
500	0,19870	0,6479	0,17832	0.6013
600	0,13258	0,5187	and prof	\$430 mm

^bRetrograde Dew Point

Temperature 280° F

Mole Fraction 1-Butene as Follows:~ 0.69050 0.81739

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Sp Volume Cu Ft/Lb	Compress- ibility Factor
800	0.04739	0,2472	0.04240	0.2288
1000	0.04234	0.2761	0.03975	0.2681
1250	0.03942	0.3213	0.03785	0.3191
1500	0,03783	0.3700	0.03663	0,3706
1750	0.03687	0.4208	0.03573	0.4217
2000	0.03606	0.4703	0.03505	0,4728
2250	0.03533	0 _* 5183	0.03440	0,5220
2500	0.03470	0.5657	0,03390	0,5716
2750	0.03417	0.6128	0,03341	0.6197
3000	0.03371	0.6595	0.03301	0.6679
3500	0.03293	0,7516	0.03232	0.7630
4000	0.03229	0,8423	0,03174	0,8563
4500	0.03174	0.9314	0.03125	0,9485
5000	0.03126	1.0192	0.03080	1.0387
6000	0,03045	1.1914	0.03005	1.2161
7000	0.02980	1.3603	0.02940	1.3881
8000	0.02924	1.5254	0.02890	1,5594
9000	0.02873	1.6861	0.02845	1.7270
10000	0.02828	1.8441	0.02800	1.8886

Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor	Pressure Lb/Sq In Absolute	Sp Volume Cu Ft/Lb	Compress- ibility Factor
	40°F			220°F	
34 _* 9 ^b 30 31 32 33 34	0.02659 0.9074 0.6542 0.4438 0.27314 0.13108	0.0093 0.2718 0.2025 0.1418 0.0900 0.0445	357.3 ^b 324.2 ^d 325 330 335 340 345	0.03622 0.2794 0.27246 0.22622 0.18361 0.14476 0.11056	0.0950 0.6650 0.5480 0.4515 0.3613 0.2800
	<u>700</u> F		350 355	0.07932	0.2038
57,4 ^b 48 50	0.02760 0.9754 0.6837	0.0149 0.4410 0.3220		250°F	an fan galae
52 54 56	0.4522 0.26444 0.11129	0.2215 0.1345 0.0587	472,5 ^b 442.0 ^d 445 450	0.04050 0.1827 0.15940 0.12960	0.1345 0.5678 0.4987 0.4100
	<u>100°F</u>	-	455	0.09396	0.3441
89.4 ^b 74 76	0.02865 1.0157 0.7882	0.0328 0.6700 0.5340	465 470	0.06837 0.04963	0.2235 0.1640
78	0.6038	0.4198		_280°F	l Levelante L
82 84 86	0.3264 0.22650	0.2386	603.5 ^b 590.0 rd	0.0715 0.1015	0.291 0.404
88	0.07164	0,0562	b Bubble d Dew Po rd Betrog	Point int	~ +
roo ch	0.077.50	- 0.0404	10 01 05	Tado Dew IOI	110
190,6 ^b 163,7 ^d 165 167 169 171 175 179 183	0.03156 0.6009 0.5544 0.4946 0.4232 0.3643 0.26652 0.18888 0.12469	0.0484 0.7922 0.7365 0.6550 0.5758 0.5015 0.3755 0.2722 0.1837		-	
187	0,07054	0.1062			

TABLE II. Two-Phase Volumetric Data for a Mixture of Propene and 1-Butene with 81.739 Mole % 1-Butene

			5		
	Dew Pt.	Bubble Pt	\$	Dew Pt.	Bubble Pt.
Mole Fraction 1-Butene	Pressure PSI Absolute	Pressure PSI Absolute	Mole Fraction 1-Butene	Pressure PSI Absolute	Pressure PSI Absolute
0.00 0.1302 0.17050 0.33153 0.4131 0.5576 0.69050 0.81739	<u>40 Deg F</u> 97.5 69.1 40.8 34.3	97.5 82.8 70.5 43.6 34.9	0.2920 0.33153 0.69050 0.81739 1.00 0.6472	220 Deg F 571.8 543.7 365.4 324.2 282.6 250 Deg F 519.4	594.5 413.1 357.3 282.6
,,00,00	21.9 7 <u>0 Deg F</u> 152.1	152.1	0.81739 1.00	497.7 442.0 381.9	540,8 472,5 381,9
0.17050 0.33153 0.4154 0.6078 0.69050	103.6 69.5 54.9	130.6 111.3 70.9	0.81739 0.81739 1.00	280 Deg F 603.5 590.0*	Gad anti-gui gui gui gui gad tuta anti auto auto gad anti anti auto auto
1.00	38.2	57.4 38.2	T Deg F	P _c Pr	essure PSI
0.00 0.17050 0.33153	227.3 161.4 124.4	227.3 195.3 166.9	1-Butene 297.0	Ab	solute 588.0
0.4582 0.69050 0.81739 1.00	104.0 80.8 62.5	108.4 89.4 62.5	Propene 196.5 *Retrograde dew	point	667.2
<u>10</u> 0.00 0.17050 0.33153 0.69050 0.81739 1.00	50 Deg F 456.6 346.9 276.3 184.1 163.7 142.9	456.6 389.7 334.3 224.9 190.6 142.9			

TABLE	IV.	Properties of Coexisting Phases :	in
		Propens-1-Butene System	

Temp.,	Pressure Mole Fraction		Sp. Vo	l.,	Equilibrium		
F	PSI 1-Butene		Cu Ft/	Lh			
	Absolute	Liquid	Gas	Liquid	Gas	Propene	1-Butene
40	21.9 a	1.000	1.000	0.02610	4.146	3.954	1.000
	30	0.887	0.674	0.02639	3.234	2.908	0.759
	40	0.743	0.436	0.02680	2.603	2.190	0.587
	50	0.600	0.291	0.02720	2.197	1.772	0.485
	60	0.467	0.199	0.02761	1.910	1.502	0.426
	70	0.336	0.126	0.02813	1.648	1.315	0.375
	80	0.207	0.071	0.02860	1.422	1.171	0.341
	90	0.086	0.027	0.02918	1.238	1.064	0.316
	97.5 b	0.000	0.000	0.02969	1.123	1.000	0.303
70	38.2 a	1.000	1.000	0.02720	2.445	3.521	1.000
	40	0.983	0.943	0.02721	2.355	3.364	0.959
	50	0.888	0.698	0.02740	1.980	2.700	0.785
	60	0.793	0.531	0.02764	1.713	2.264	0.670
	80	0.606	0.319	0.02824	1.339	1.730	0.526
	100	0.429	0.188	0.02900	1.094	1.420	0.439
	125	0.216	0.080	0.02995	0.8795	1.174	0.370
	150	0.017	0.006	0.03107	0.7315	1.011	0.333
	152.1 b	0.000	0.000	0.03121	0.7207	1.000	0.330
100	62.5 a	1.000	1.000	0.02821	1.5245	3.136	1.000
	80	0.880	0.702	0.02850	1.262	2.472	0.798
	100	0.746	0.491	0.02900	1.055	2.002	0.658
	125	0.587	0.329	0.02960	0.8723	1.625	0.560
	150	0.404	0.213	0.03053	0.7295	1.382	0.494
	175	0.284	0.129	0.03119	0.6260	1.218	0.454
	200	0.144	0.062	0.03202	0.5454	1.096	0.431
	227.3 b	0.000	0.000	0.03318	0.4718	1.000	0.411
160	142.9 ^a	1.000	1.000	0.03092	0.6736	2.500	1.000
	150	0.970	0.930	0.03100	0.6450	2.337	0.959
	200	0.781	0.608	0.03178	0.5030	1.791	0.778
	250	0.604	0.410	0.03280	0.4110	1.491	9.679
	300	0.440	0.272	0.03402	0.3400	1.299	0.619
	350	0.284	0.166	0.03560	0.2838	1.165	0.585
	400	0.142	0.082	0.03745	0.2408	1.070	0.574
	456.6 ^b	0.000	0.000	0.03983	0.2002	1.000	0.581

Temp., F	Pressure PSI	Mole Fraction 1-Butene		Sp. Vol Cu Ft/L	Sp. Vol., Cu Ft/Lb		Equilibrium Constants	
	Absolute	Liquid	Gas	Liquid	Gas	Propene	1-Butene	
220	282.6 ^a 300 350 400 450 550 600 625 645 653 c	1.000 0.954 0.835 0.720 0.610 0.508 0.411 0.320 0.276 0.241 0.218	1.000 0.917 0.735 0.601 0.490 0.399 0.324 0.255 0.224 0.200 0.218	0.03472 0.03502 0.03603 0.03738 0.03865 0.04010 0.04222 0.04690 0.05200 0.0588 0.0691	0.3220 0.3016 0.2568 0.2180 0.1855 0.1630 0.1450 0.130 0.120 0.105 0.0691	1.918 1.817 1.590 1.428 1.309 1.221 1.151 1.096 1.073 1.054 1.000	1.000 0.961 0.880 0.834 0.803 0.786 0.790 0.797 0.810 0.830 1.000	
250	381.9 ^a 400 450 500 550 600 615 625 630 ^c	1.000 0.961 0.860 0.766 0.674 0.585 0.560 0.539 0.514	1.000 0.938 0.797 0.686 0.593 0.519 0.502 0.492 0.514	0.03800 0.03555 0.03984 0.04120 0.04440 0.0528 0.0580 0.0580 0.0618 0.0688	0.2220 0.2076 0.1778 0.1550 0.134 0.115 0.108 0.0950 0.0688	1.652 1.592 1.453 1.342 1.245 1.159 1.132 1.104 1.000	1.000 0.976 0.926 0.896 0.880 0.887 0.896 0.913 1.000	
280	506 a 525 550 575 600 604 c	1.000 0.966 0.920 0.878 0.835 0.822	1.000 0.952 0.893 0.842 0.807 0.822	0.4497 0.0450 0.0450 0.0503 0.0645 0.0683	0.1327 0.127 0.119 0.109 0.087 0.0683	1.443 1.400 1.347 1.294 1.172 1.000	1.000 0.986 0.970 0.959 0.966 1.000	

a Vapor pressure of 1-Butene

- ^b Vapor pressure of Propene
- c Critical state

TABLE V. Properties of Propene-1-Butene System in the Critical Region

Mole Fraction of 1-Butene	1.00	0.8174	0,6905	0,3315	0.1705	0
Critical State Pressure (lb/in ² abs) Temperature (°F) Volume (cu. ft/lb)	588.0 297.0 0.0686	604.0 280.0 0.0683	615.0 268.0 0.0685	643.0 233.0 0.0690	654.0 218.0 0.0692	667.2 196.5 0.0694
Point of Max. Temp. Pressure (lb/in ² abs) Temperature (°F) Volume (cu. ft/lb)		602.0 281.0 0.0826	612.5 269.0 0.0824	640.2 234.5 0.0813	651.5 219.5 0.0775	

I. METHOD OF CALCULATION EMPLOYED IN THE DETERMINATION OF DEW-POINT GAS COMPOSITION.

1) Calculate bZ =
$$\frac{PV}{mT}$$

where P = pressure of gas in sample bulb

 \underline{V} = volume of sample bulb

m = weight of gas in sample bulb

T = absolute temperature of gas in bulb

b = specific gas constant for sample of gas

- Assume an approximate composition of the mixture being analyzed.
- 3) Using assumed value of mixture composition, obtain value of Z from a graph of Z vs mole fraction 1-butene plotted with isothermal curves at a pressure of one atmosphere. This graph was constructed from experimental PVT data for the propene-1-butene system.

4) Calculate b =
$$\frac{bZ}{7}$$

5) Substitute the calculated value of b into equation

 $\underline{n_4} = \frac{.76514}{b} - 3.001$ to obtain an approximate value of $\underline{n_4}$ The above equation may be derived from the relations:

$$b = \frac{R}{\underline{n_3}M_3 + \underline{n_4}M_4} \quad \text{and} \quad \underline{n_3} = 1 - \underline{n_4}$$

 Repeat steps 2 through 5 using new value of composition for second trial. Make as many trial calculations as needed.