CATION ERRORS OF THE

GLA^{SS} ELECTRODE AT HIGH TEMPERATURES

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Max F. Smith

A THESIS SUBNITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE MASTER OF SCIENCE May 30, 1939

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INTRODUCTION

Cremer (1) discovered that a definite potential existed between an acid and an alkaline solution when the two solutions were separated by a thin glass membrane. He surmised that the glass membrane was permeable only to hydrogen ions, from earlier work on ion migration through glass, but did not realize that the potential was a function of the hydrogen ion concentration in the two solutions. Haber and Klemensiewicz (2) were the first investigators to show that the glass membrane functioned as a hydrogen electrode and that the potential followed the Nernst equation

$$
E = \frac{RT}{F} \ln \frac{H_2}{H_r}
$$
 (1)

where H₁ and H₂ are the hydrogen ion concentrations in the solutions on either side of the membrane. The glass membrane used by these investigators was a simple thin-walled bulb blown on the end of a test tube. The tube was filled with a solution of fixed hydrogen-ion concentration and was immersed in other solutions of various hydrogen

ion concentrations. Calomel reference electrodes dipced into the internal and external solutions. The potential developed by the cell was measured by means of a potentiometer and quadrant electrometer. The bulb-type glass membrane was subsequently used by many investigators for the measurement of hydrosen ion concentration and became known as the Haber Glass Electrode.

The glass electrode is unique among hydrogen ion electrodes in that it is uneffected by the presence of oxidizing or reducing substances and is not poisoned by substances which often interfere with the use of other electrodes, such as the hydrogen, quinhydrone, antimony, etc. The glass electrode may be used in the presence of colloids and suspended solids and in various viscous materials. Deapite these advantages, the glass electrode was not widely used for many years because the high electrical resistance of the glass membrance necessitated the use of a cuadrant electrometer for the potential measurement. The development of modern electronic circuits which could be used in place of the delicate quadrant electrometer has brought about a wide-spread use of the glass electrode and today, the glass electrode is one of the most

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commonly used means for the measurement of hydrogen-ion concentration.

The glass electrode deviates in several respects from the behavior theoretically expected from a hydrogen-ion electrode. If identical solutions are placed on the two sides of the glass membrane and identical reference electrodes dipped into the two solutions, the theoretical potential between the two electrodes is zero. Actually there is usually a slight potential. known as the "Asymmetry Potential". The potential is presumably due to slight differences in the compositions of the two surfaces of the glass membrane. The potential usually does not exceed a few milli-volts and remains substantially constant over long periods of time, at room temperatures, so that no error from this source is ordinarily encountered in practical measurements. The glass electrode is usually standardized by means of buffer solutions of known hydrogen ion concentration (pH) so that the correction for asymmetry potential is automatically included in the standardization.

A more serious error of the glass electrode, from the standpoint of industrial pH measurements,

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is the error caused by high alkali-ion concentrations in the high pH region. Particularly in the presence of sodium ions, the glass electrode yields pH values which are smaller than the true pH values. The magnitude of the error increases with increasing off, increasing alkali-ion concentration and increasing temperature. Metallic cations other than sodium produce similar errors but their effects are very much smaller than that of sodium ions.

Dole (3) made an extensive study of alkaliion errors at 25° C. Dole and Wiener (4) measured sodium and lithium-ion errors at 10°, 25° and 50° C_{\bullet} . Gardner and Sanders (5) measured the sodium-ion errors of two commercial electrodes at 30°, 50° and 60° C. Unfortunately these investigators used electrical measuring equipment which was not provided with temperature compensation so that the published values combine sodium errors with an indefinite temperature error.

There is syidence that the magnitude of the alkali-ion error decends upon the composition of the glass from which the membrane is made. Ssokalov and Passynsky (6) stated that a lithium glass containing 80% S102. 10% CaO and 10% LipO showed much smaller errors than the soda-lime

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fig I Arrangement of Cell.

glass usually used. Gabbard and Dole (7) attempted to make glass electrodes of this composition but found them unsatisfactory. At present, commercial glass electrodes are made of a soda-lime-silica glass known as Corning 015, consisting of approximately 22% Na₂O. 6% CaO and 72% SiO₂.

Despite future improvements in glass which may provide better glass electrodes, there is an immediate need for reliable and extensive measurements of alka i-ion errors of electrodes made from the O15 glass. The recent extension of glass electrode applications into high temperature regions wakes high temperature values particularly desirable. The present work was undertaken for the purpose of supplying the needed data.

APPARATUS

The glass electrodes were supplied by the National Technical Laboratories and were made as follows: Corning 015 glass was blown into a bulb on the end of a ten millimeter diameter lead glass tube; the lead glass being of very high resistivity, reduced the electrical leakage to a minimum. The glass membranes themselves were about 0.0075 of an inch thick and had resistances at

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fig. II Potentiometer Circuit

tig II Hydrogen Gas Train

 25^o C. of 100 to 150 megohms. Permanent internal solutions and electrodes were sealed in. Shielded leads extended into the electrode to within an inch of the bottom so that electrostatic disturbances were completely avoided.

The glass electrodes were compared directly with hydrogen electrodes in the cell illustrated in figure 1, There were fifteen openings for; six glass electrodes, three hydrogen electrodes, one calomel electrode, a hydrogen inlet and outlet, a thermometer, a glass tube for adding and a siphon tor removing solution. The cell was supported in an oil-filled thermostat.

The circuit used for measurement of the potentials is shown in figure 11. The glass and hydrogen electrode leads were connected to a Beckman pH meter amplifier through a mult1-po1nt high resistance switch which made the comparison of many glass electrodes a simple matter. The potentiometer was a Leeds and Northrup student type, which could be read within \sim 0.1 mv.

Hydrogen electrodes made of plat1n1um **wire** were entirely satisfactory. The platinizing solution was prepared by dissolving cleaned waste platinium wire in aqua regia, evaporating the

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solution to dryness, adding water and evaporating to dryness again. The residue was dissolved in distilled water and was used without further treatment such as the addition of lead acetate. It was found that the pH of the platinizing solution made very little difference in the action of the hydrogen electrodes as long as a steady stream of hydrogen was used. The electrodes were cleaned in aqua regia and then purged of chlorine by electrolizing in 1.0 N. H₂SOA for fifteen minutes or by dipping alternately in boiling concentrated HNO3 and boiling 10% sodium acid sulphite. The same effect was produced by allowing them to stand in distilled water for two or three days.

A Beckman sleeve-type saturated KCl-calomel electrode was used for the reference electrode. This electrode was checked against two other saturated KCl-calomel electrodes and three O.1 N. KCl-calomel electrodes. An experiment to determine the leakage of KCl solution out of this type of electrode showed a maximum value of 0.003 moles of KCl in twentyfour hours; this was not enough to effect the results of the experiments in any way.

The cell used for the comparison of the glass and hydrogen electrodes was kept in a thermostat filled with low conductivity transformer oil. The constant temperatures that were required

were maintained by a 100 c.c. mercury regulator. connected through a vacuum tube relay to two knife heaters. An electric motor was used for agitating the oil bath, but.it was disconnected while the readings were being taken. A seperate thermoatat was kept at 25° C.: this thermostat contained two standard cells and the O.l N. KCl-ealomel half-eells.

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The hydrogen gas train is shown in figure lll. Thick-walled rubber tubing connections were used where necessary; this tubing was first boiled in concentrated NaOH and then impregnated with paraffin. The hydrogen was saturated with water vapor before entering the cell in order to keep the concentration of the cell solution constant during a run.

EXPERIMENTAL PROCEDURE

The procedure was a modification of that used by $Dole(8)$ in which the concentration of the cation is kept constant during the experiment. The glass and hydrogen electrodes were compared 1n the same solution as was first done by Hughes (9) .

A buffered solution of the acetate and phosphate of the oation under investigation wae placed 1n the cell; the electrodes were then placed 1n poe1t1on and the entire assembly lowered into the thermostat. The hydrogen was started through

the cell and through the flask containing the base solution to be used for changing the pH of the cell solution. When the hydrogen electrodes gave constant values, usually in two to two and one-half hours, the potentials of the glass and hydrogen electrodes were recorded. The pH of the solution in the cell was then changed by closing the stopcock on the hydrogen outlet fron the flask and letting the pressure of the hydrogen force the base solution from the flask into the cell. When the stopcock was opened the base solution in the line to the cell ran back into the flask. Since the base added had been saturated with hydrogen and it was introduced without allowing oxygen to enter the cell, the hydrogen electrodes came to equilibrium at once. The potentials of the glass electrodes became constant in about ten minutes; they took somewhat longer in potassium solutions below 40° C. Thirty to forty minutes were usually allowed to make certain that equilibrium was reached.

The potentiometer circuit was standardized against the two standard cells that were kept in the 25° C. thermostat. The standardization was done through the amplifier. The low input current of the electronic carcuit ($2x10^{-13}$ amps.) allowed the standard cells to be connected without polarization even though the circuit might be far out of balance.

 $#$ \mathbb{G} $\#$

The cells which were considered in this investigation were:

Pt H_2 solutionx | saturated KCl | Hg_2Cl_2 | Hg 2. Ag $\left|\begin{array}{cc} \text{AgCl} & \text{Const.} \text{Cl} \\ \text{Const.} & \text{H} \end{array}\right|$ glass $\left|\begin{array}{cc} \text{solution X} \end{array}\right|$ saturated KCl Hg_2Cl_2 | Hg

If we subtract the potentials of these two cells we obtain the potential for the cell **3.** Pt H_2 solution X | glass $\begin{array}{|c|c|c|c|c|c|c|c|c|} \hline \text{const.} & \text{C1} & \text{AgCI} & \text{Ag} \\\hline \end{array}$

Using the same terminology as Dole and Wiener (4) and calling this potential ΔG , then by definition

 $\Delta G = E_1 - E_2$

It has been pointed out that at high pH ΔG varies with the metalic cation present, its concentration and the pH of the solution. If the potential which would be observed, if the glass electrode functioned as a perfect hydrogen-ion electrode, is called ΔG_{α} , then the error of the glass electrode ΔE can be found.

$$
\Delta E = 4G - \Delta G_{\odot}
$$

 ΔG_{Ω} is found by making measurements in the low pH range where the glass electrode does act as a perfect hydrogen-ion electrode. The preceding discussion will be illustrated later by the consideration of a specific case.

The pH of the buffer solutions at the various temperatures was determind by the hydrogen electrode; 1.e. the potential of cell 1. Since the E.M.F.-temperature relations of the saturated KC1-calomel electrode are not well established at the higher temperatures used in this investigation, the pH values were referred to 0.05 N. potassium hydrogen phthalate with the assumption that the pH of this solution does not change with temperature. Clark (10) gives the pH of this solution as 3.98. Recently MacInnes. Belcher and Shedlovsky (11) have recommened the values 4.00 at 12 $^{\circ}$ 0. 4.00 at 25 $^{\circ}$ C and 4.015 at 38 $^{\circ}$ C. Dispite the probable greater accuracy of this work, the value 3.98 was used in the following computations because the other values have not been widely accepted. The uncertainty in the pH values of the potassium hydrogen phthalate buffer at the various temperatures is only of secondary importance in this investigation for it does not enter directly into the alkali-ion errors. It appearsonly in the indicated pH values of the solutions. A large change in the pH values of these solutions would cause only a slight shift in the error curves shown in the following figures.

At each temperature the hydrogen and calomel electrodes were immersed in 0.05 N potassium hydrogen phthalate solution and the cell potential (E) determined. From the equation

$$
E - E^{\dagger} = \frac{2.30 \frac{3}{F} RT}{F} pH
$$
 (2)

the quantity E' was found for each temperature. This quantity includes the E.M.F. of the calomel reference cell, the liquid junction potential and the correction

 $-11-$

for the reduced partial pressure of the hydrogen gas at the hydrogen electrode. The experimental values are shown in the following table

TABLE 1

The experiments included in this investigation are the measurements of cation errors of the glass electrode at the following temperatures and concentrations.

Typical experimental data and computed results

are given in table II. The values are for 2.5 N sodium-ion at 50° C. H_1 , H_2 and H_3 are the measured potentials (in volts) of the cells composed of a calomel reference electrode and three indididual hydrogen electrodes. This is the potential of cell

1 given above. G_1 , G_2 -- G_7 are the corresponding potentials of the same calomel electrode and seven individual glass electrodes. This comprises cell 2 given above. The measurements were made on nine different solutions. The pH values shown were obtained by the use of cquation 2, the value of E' for the temperature in question and the average value of H_1 , H_2 and H_3 . ΔG_1 --- ΔG_7 are the algebraic differences between G_1 ---- G_7 and the average value of H_1 , H_2 and H_3 . This of course is the potential of cell 3. ΔE_1 --- ΔE_7 are the sodium-ion errors of the respective glass electrodes; i.e., the differences between the measured glass electrode-calomel electrode potentials and the corresponding potentials which would have been obtained if the glass electrode functioned as an ideal hydrogen-ion electrode. The latter potentials were obtained from the values of 4G in the low pH region, where the alkali-ion errors are negligible. This procedure will also eliminate the asymmetry potential. If there were no alkali-ion error, the values of 4G, for a given electrode, would remain constant with increasing pH. If the average value of 46 in the region of negligible cation error is called $A\mathbb{G}_0$, then the cation errors are obtained by subtracting ΔG_0 from the measured values of Δ .

The age of the glass electrode appears to have very little effect upon the cation errors except in the

case of sodium-ions. There is some evidence that freshly blown glass electrodes show somewhat smaller sodium-ion errors than are shown by old electrodes. In Table II, electrodes GA and Gy were freshly blown electrodes. The effect of age, however, appears to be less than the variations normally found among individual electrodes.

All experimental results are summarized in Figures 4 to 17. The points shown on the graphs represent the average values obtained for at least five glass electrodes in each case.

In Table III alkali-ion errors published by other workers are compared with the corresponding values obtained in this investigation. In general the agreement is satisfactory for most practical measurements. For refined pH determinations where large sodium-ion errors are involved and where the age of the glass electrode may be an important factor, direct determination of the sodium-ion error should be made under the actual operating conditions.

TABLE IIIa

Values in parenthesis are those of J. L. Gabbard and Dole (7).

TABLE IIID

Values in parenthesis are those of Dole and Wiener (4) .

TABLE II

 H_1 $\overline{.}$ 3 The potential in volts of three hydrogen electrodes. G_1 = 6 The potential in volts of six glass electrodes.

 Δ^{0} 1 - 6 The difference in volts of the potential of the average hydrogen electrode and the potential of the individual glass electrodes.

 $E_1 = 6$ $\Delta G - G_0$ or the increase of G caused by the presence of sodium ions.

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THEORY OF THE GLASS ELECTRODE

There are three general theories for glass electrode behavior: the phase boundary potential theory, the membrane-diffusion potential theory. and the ion adsorption theory. M. Cremer (1) , as stated before, assumed the glass was permeable only to hydrogen ions. He arr1ved at this conclusion because the work of E. Warburg showed that the electrical conductivity of glass was of electrolytic-type. Michaelis (19) extended this theory by considering the diffusion of other cations at high pH. Dole (3) showed this idea to be erroneous by doing two parallel experiments in which he measured the potentials between o.lN NaOH solution and (a) pure $0.1N$ HCl solution and (b) $0.1N$ HCl solution which was $0.1N$ with respect to sodium-ion; the two potentials were found to be the same. If the sodium error was due to the diffusion of sodium-ion, the potential would be a function of the sodium-ion concentration on both sides of the glass membrane.

Horovitz (12) assumed an ion adsorption on the glass surface. He later modified this theory to include an ion interchange between the glass surface and solution; he again changed his theory to take 1nto account the ionic mobility of the ions (13) and the heat of the mixture on the surface of the glass.

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Schiller (14) and Lengyel (15) also advanced ion adsorption theories. Lengyel used quartz for his work; it is doubtful if the action of quartz and glass membranes are similar since the quartz acts essentially as a condenser while the low-resistance glass does not.

Haber (2) , as already mentioned, advanced the first phase boundary theory. He neglected the action of metallic cations at high pH values. Hughes (16) stated that the buffer action of sodium silicate kept constant the hydrogen-ion concentration within the glass. While he mentions alkali-ion errors, he makes no attempt **to** explain them.

Gross and Halpern (17) attempted to account for the alkali-ion errors by assuming a dissolving of the glass in the water and the water in the glass. They postulate that in low pH regions the ionic concentration 1n the glass 1e due to hydrogen and hydroxol ions but at higher pH the metal ion also has an effect on the 1on1e concentration. In order to make these assumptions, it was necessary to assume a region of mutual solubility; it is difficult to visualize this film as existing 1n view of the slowness with which glass dissolves and the rapidity with which glass electrodes come to equilibrium.

Dole (3) used the Henderson and Planck formulas for liquid Junction potentials to derive an

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equation which fitted the measured alkali-ion errors up to a pH value of 12. The equation contained several constants that were neither constant nor theoretically determinable. Dole (18) later applied statistical mechanics to the problem and obtained an equation that predics increased cation error at higher temperatures.

on is: $\Delta E = \frac{RT}{F} \frac{\left(B_{me} \cdot C_{me} \cdot f_{me} \right) \left(\frac{Q_{me} - Q_H}{RT} + C_H f_H\right)}{C_H f_{me}}$ The equation is:

AE is the error of the glass electrode. R. T. and F have their usual significance. B is the ratio of the probability of a transition to the glass surface to the reverse transition at equilibrium. (Dole takes these as unity)

c is the concentration in moles per liter.

f is the activity coefficient.

Q is the difference between the energy of an ion in the interior of the solution and the energy of an ion on the glass surface.

The subscript Me refers to any cation other than H

Dole calculated values of $Q_H - Q_{M_{\rm R}}$ from measured errors and found them to be around 13 to 15 k. cal. per mole. The values increased with increasing pH, but at 50° C they became more constant.

The many constants in this equation can only be evaluated by experimental measurement and the experiment removes the need for the equation. It is, therefore, of no value from the standpoint of providing a means by

which glass electrode errors may be computed. Even though the constants could be evaluated, the equation fails to explain either the individual action of glass electrodes or the increasing reproducibility of the potassium-ion errors as the temperature is increased. The modified ionic exchange theory of Horovitz might offer a better explanation, but it would be of no greater value in predicting the glass electrode errors.

SUMMARY

1. The cation errors of Corning 015 glass electrodes were determined for various concentrations of lithium, potassium and sodium ions at 30° , 40° , 50° . 60° and 70° C and for calcium ion at 30° and 60° C. The errors were found to increase with incressing temperature.

2. Fresh glass electrodes showed slightly smaller errors than those which had been used for some time.

3. Potassium-ion errors, which were variable at low temperatures, became definate at temperatures above 40° C.

ACKNOWLEDGMENT

The writer wishes to take this opportunity to acknowledge his indebtedness to Dr. A. O. Beckman for his helpful suggestions and to the National Technical Laboratories for supplying the glass electrodes and much of the equipment used in this investigation.

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