Numerical investigation of spinal neuron facilitation with multi-electrode epidural stimulation

Thesis by Jeffrey A. Edlund

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iv ABSTRACT

Approximately 1,275,000 people in the US have a spinal cord injury severe enough to cause some paralysis of the arms and/or legs. Epidural stimulation using implanted multi-electrode stimulating arrays over the lumbosacral spinal cord has recently shown promise in assisting individuals with severe spinal cord injuries to stand, walk, and even facilitate voluntary movement. Both animal model and human studies have shown that sub-threshold facilitation of motor recovery gives the best results. The underlying neural mechanisms by which sub-threshold epidural stimulation leads to motor recovery are incompletely known.

This thesis uses computational methods to study the *facilitation effect*. A neuron is facilitated if a sub-threshold synaptic input can cause a neuronal output under the influence of a stimulating electric field. The analysis in this thesis is based on a computational model of the epidural spinal stimulation process in the rat spinal cord. This model includes a time-domain finite element simulation (using COM-SOL®) of the various tissues in the spinal cord with the appropriate anisotropic and frequency-dependent complex relative permittivities. The voltages obtained from the finite element simulations were used as the extracellular voltage in NEURON simulations.

A population of neurons was simulated under a wide variety of conditions. These simulations highlight the effect of neuron orientation, location, and synaptic timing as key parameters which influence facilitation.

This study indicates that regions of the spinal cord that have previously been ignored may be actively involved in motor recovery. These results may also enable the design of specialized epidural electrode arrays and the design of new stimulation protocols.

v TABLE OF CONTENTS

Acknowl	edgements	iii
Abstract		iv
Table of (Contents	v
List of Ill	lustrations	iii
List of Ta	ables	xliii
Nomencl	lature	xlix
Chapter I	I: Introduction	1
1.1 F	Review of existing literature	6
1.2 (Contributions of thesis	9
Chapter I	II: Finite element modeling of a rat spinal cord	13
2.1 H	Building the 3D volume conductor model	13
	2.1.1 2d extrusion model with embedded electrode array model	14
	2.1.2 Electrical and physical model of epidural stimulating arrays	17
	2.1.3 Stimulation waveforms	19
	2.1.4 Modeling tissues and electrode materials	28
	2.1.5 Tissues	28
	2.1.5.1 4-Cole-Cole model	29
	2.1.6 Electrode array	33
	2.1.6.1 Parylene C	33
	2.1.6.2 Platinum	35
	2.1.7 Materials Summary	35
2.2 0	COMSOL simulations	35
	2.2.1 Stimulation patterns	37
	2.2.2 Computational details	41
2.3 \$	Summary	41
2.A A	Appendix: Conductivity and relative permittivity measurements	
f	from literature compared with 4-cole-cole fits	41
Chapter I	III: Building a NEURON model of a rat spinal interneuron	46
3.1 N	Model neuron properties	48
3.2 N	Model neuron physical geometry	51
3.3 N	Neurotransmitter models	54
	3.3.1 Synapse model: Exp2Syn	56
	3.3.2 Neurotransmitter release	57
3.4 N	Neuron characterization	58
	3.4.1 Resting potential of model neuron	58
	3.4.2 Current injection	60
	3.4.3 Synapse Thresholds	61
3.5 E	Error discussion	71
3.6 \$	Summary	73

3.A	Appendix: Current injection	74
3.B	Appendix: synapse thresholds at the soma for comparison	79
Chapter	r IV: Activating neurons using epidural stimulation in the absence of	
exci	itatory postsynaptic potentials (EPSPs)	82
4.1	Locations of simulated neurons	83
4.2	Extracellular voltage and neuron simulations	85
4.3	Active neurons for monophasic and biphasic stimulation	87
4.4	Comparison of membrane voltage distribution for monophasic and	
	biphasic stimulation	91
4.5	Neurotransmitter release with $\leq 5 \text{ V}$ of stimulation	101
	4.5.1 Monophasic stimulation	101
	4.5.2 Biphasic stimulation	105
4.6	Predicting neuron activation	118
4.7	Discussion	120
4.A	Appendix: Stimulation Thresholds	123
	4.A.1 Monophasic	123
	4.A.2 Biphasic	160
Chapter	r V: Facilitating sub-threshold synaptic input using epidural stimula-	
tion	to achieve neuron activation	196
5.1	Modeling of the Facilitation effect	200
5.2	Examples of facilitation	202
	5.2.1 Biphasic stimulation	204
	5.2.2 Monophasic stimulation	210
5.3	Total facilitated neurons for monophasic and biphasic stimulation	220
5.4	Predicting neuron facilitation	229
	5.4.1 Separating facilitated and non-activated neurons using static	
	features	231
	5.4.2 Separating facilitated and non-activated neurons using	
	stimulation-only membrane voltages	234
5.5		238
5.A	Appendix: Position of facilitated neurons	241
5.B	Appendix: More examples of facilitation	247
	5.B.1 Biphasic stimulation with $V_s > 0$ and a distal tip synapse	247
	5.B.2 Biphasic stimulation with $V_s < 0$ and a mid-dendrite synapse	255
	5.B.3 Biphasic stimulation with $V_s > 0$ and a mid-dendrite synapse	262
	5.B.4 Monophasic stimulation with $V_s < 0$ and a mid-dendrite	200
	synapse	269
	5.B.5 Monophasic stimulation with $v_s > 0$ and a mid-dendrite	275
5 0	Annendive Symplementory for separating facilitated and non	213
J.C	Appendix. Supplementary lightes for separating facilitated and non-	201
5 D	Annandix: Supplementary figures for separating facilitated and non	201
5.D	Appendix. Supplementary lightes for separating facilitated and non-	204
Chapter	WI: Conclusions	304
6 1		321
0.1		551

6.2	Comparing with the literature
6.3	Future work
Bibliog	raphy

viii LIST OF ILLUSTRATIONS

Number

Page

- 2.1 MRI data of the spinal cord of an adult female Sprague Dawley rat showing vertebra T13-L4. The vertebra are labeled with colors: L4, L3, L2, L1, and T13. The CSF, white matter, gray matter, and nerve fibers are labeled green except for the L1 gray matter which is uncolored. Subfigures: (a) shows a sagittal slice (down the middle of the spinal cord) with the dorsal direction to the right, the ventral direction to the left, the rostral direction to the top, and the caudal direction to the bottom of the page. (b) shows a 3D mesh representation of the segmented data.
- 2.2 Transverse slices of the MRI data of the spinal cord of an adult female Sprague Dawley. Each subfigure shows a slice in the approximate middle of each vertebra: (a) T13 vertebra, (b) L1 vertebra, (c) L2 vertebra, (d) L3 vertebra, and (e) L4 vertebra. The CSF, white matter, gray matter, and nerve fibers are labeled green except for the L1 gray matter which is uncolored. The dorsal direction is to the right of the page.
- 2.3 Transverse MRI slice of rat spinal cord from the middle of L1 vertebra. The dorsal direction is to the right of the page. Materials are labeled with colors: gray matter (yellow), white matter (red), cerebrospinal fluid (CSF)/roots/fibers (green), and bone (purple). 17

Dimensions of flat electrode array. The small (0.50 mm by 0.20 mm)	
rectangles are the platinum electrodes. See Table 2.1 for electrode	
labels and array orientation. Figures 4.1 and 4.2 show the labeled	
electrode array in the simulated spinal cord	17
Sketch of the spinal cord geometry and electrode array on top of	
the segmented image. Regions in the segmented image are indicated	
by color: gray matter (yellow), white matter (red), CSF/roots/fibers	
(green), and bone (purple). See Figs. 2.6 and 2.7 for a better view of	
the electrode array after extrusion.	19
After the sketch in Fig. 2.5 was extruded to a length of 23.1 mm,	
10 µm-thick electrodes were placed in the parylene. This figure	
shows a slice through one of the electrode rows. The cerebrospinal	
fluid is labeled CSF. The dorsal white matter, ventral white matter,	
and gray matter are labeled WD, WV, and GM respectively. See	
Fig. 2.7 for a close up view of the electrodes	20
Close up view of the electrode array seen in Fig. 2.6. Electrodes	
are gold and indicated with dashed gold circles. The parylene C is	
colored cyan. See Fig. 2.6 for more details on the other materials	20
A partially transparent view of the model showing the placement of	
the 27 electrodes. See Figs. 2.6 and 2.7 for material labels	21
Plots of $S_{\text{mono}}(t, w = 200 \mu\text{s})$, $S_{\text{bi}}(t, w = 200 \mu\text{s})$, and $S_{\text{SqExp}}(t, w = 100 \mu\text{s})$	
200 µs)	22
Plots of power spectral density for monophasic square pulse	
$(\tilde{S}_{mono}^2(f, w = 200 \mu s))$, biphasic square pulse $(\tilde{S}_{bi}^2(f, w = 200 \mu s))$,	
and biphasic square exponential $(\tilde{S}_{SqExp}^2(f, w = 200 \mu s))$	24
	Dimensions of flat electrode array. The small (0.50 mm by 0.20 mm) rectangles are the platinum electrodes. See Table 2.1 for electrode labels and array orientation. Figures 4.1 and 4.2 show the labeled electrode array in the simulated spinal cord

- Plots of a Gaussian monophasic pulse $G_{\text{mono}}(t, \varsigma_{\text{mono}})$ and Gaus-2.11 sian biphasic pulse $G_{\rm bi}(t, \varsigma_{\rm bi})$. Where $\varsigma_{\rm mono} \approx 112.84\,\mu {\rm s}$ and $\varsigma_{\rm bi} \approx 166.04\,\mu {\rm s}$ cause $G_{\rm mono}(t, \varsigma_{\rm mono})$ and $G_{\rm bi}(t, \varsigma_{\rm bi})$ to have the same amount of power as a square pulse with width $w = 200 \,\mu\text{s}$ and Plots of power spectral density for the monophasic Gaussian pulse 2.12 $\tilde{G}_{\text{mono}}(f, \varsigma_{\text{mono}})$ and the biphasic Gaussian pulse $\tilde{G}_{\text{bi}}(f, \varsigma_{\text{bi}})$ used in 2.13 Conductivity and real relative permittivity for parylene C 34 2.14 The finite element mesh used in all the volume conductor simulations. 37 Comparison of combination translations along the \hat{z} axis. Note the 2.15 edge effects in row 1 and 7. The histogram includes all three single row combinations (ANpBNn,ANpCNn,BNpCNn) (where N is the row number) and stationary simulations run at $f_{mono}^{max} = 0 \text{ Hz}$ and $f_{\rm bi}^{\rm max} \approx 958.5 \,\mathrm{Hz}.$ 39 Comparison of combination (A4 = 1V, B4 = -1V) with mirrored 2.16 combination (C4 = 1V, B4 = -1V). The mean difference is 0.229 mV (indicated by vertical line) and the maximum difference was 1.49 mV. The histogram includes stationary simulations run at $f_{\text{mono}}^{\text{max}} = 0 \text{ Hz and } f_{\text{bi}}^{\text{max}} \approx 958.5 \text{ Hz.}$ 40 2.17 Data and Cole-Cole fits for Muscle. The 4-Cole-Cole fit is only for transverse muscle even though data is available for both parallel and transverse. Data from (C. Gabriel and S. Gabriel, 1997) and (Josef Ladenbauer, 2008). 43 Data and Cole-Cole fits for bone. Data from (C. Gabriel and S. 2.18 Gabriel, 1997) and (Josef Ladenbauer, 2008). 44
- Х

2.19	Data and Cole-Cole fits for cerebro spinal fluid (CSF). Data from (C.	•				
	Gabriel and S. Gabriel, 1997) and (Josef Ladenbauer, 2008)	44				

2.20	Data and Cole-Cole fits for isotropic white matter. Data from (C.
	Gabriel and S. Gabriel, 1997) and (Josef Ladenbauer, 2008) 45
2.21	Data and Cole-Cole fits for gray matter. Data from (C. Gabriel and

S. Gabriel, 1997) and (Josef Ladenbauer, 2008).	•	•	•	•	•	•	•	•			••		45
---	---	---	---	---	---	---	---	---	--	--	----	--	----

3.1 Neuron compartment circuit model for arbitrary compartment n including all modeled ion channels, a synapse, and extracellular voltage ($E_{extracellular}$). Points (A_n, B_n, C_n) connect to the corresponding points on the right hand side of compartment n - 1. Starting from the bottom and going left to right, the components in the circuit are: the passive properties of the compartment which are modeled by the following components in the bottom left: the membrane capacitance (C_m) , the membrane leakage conductance (g_l) , and the reversal potential of the leakage current (e_{pas}) . To the right of that is the sodium channel with variable conductance g_{na} (given by Eq. (3.1)) and e_{na} which is the reversal potential of Na^+ ions. To the right of that is the fast potassium channel with variable conductance g_{K_A} (given by Eq. (3.2)) and e_k which is the reversal potential of K^+ ions. The potassium delayed rectifier conductance $(g_{K_{dr}})$ is also connected to e_k and is given by Eq. (3.3). The synapse channel (only present if the compartment has a synapse attached) consists of the variable synaptic conductance g_{syn} (given by Eq. (3.5)) and the reversal potential of the synapse (e_{rev}) . The axial resistance inside the neuron is modeled by resistance R_a . The upper portion of the circuit is the extracellular voltage mechanism of NEURON and is described in more detail in the NEURON documentation. $R_{xraxial}$ is the resistance of the extracellular medium along the axial direction. g_{xg} is the conductance of the extracellular medium between the extracellular potential and the membrane surface. C_{xc} is the capacitance of the extracellular medium (by default $C_{xc} = 0$ indicating an open circuit). $e_{extracellular}$ is the extracellular voltage which is obtained from the volume conductor models. Points $(A_{n+1}, B_{n+1}, C_{n+1})$ connect to the corresponding points in the next compartment (n + 1).

49

- 3.3 This figure shows the sections of the model neuron from the axon tip on the left side to the distal tip of one of the dendrites on the right side. Only one of the 5 dendrites is shown (since the rest only differ in orientation). Each section type is labeled by color (see legend). The diameter of the various sections is indicated by the size of the section on the vertical axis and the length of each section on the horizontal axis. The horizontal axis also indicates the path length distance from the axon tip. The center of each segment inside each section is indicated by a blue circle and labeled with a black number. The distal tip of the axon is labeled. Location "A" is in the middle of the distal section of the dendrite with segment number 8. Location "B" is at the distal tip of the distal section of the dendrite with segment number 16. These locations will be used for probe points in Chapters 3 to 5 and synapse locations in Chapters 3 and 5. Note that because there are 5 dendrites, there are 5 location "A"s and 5 location "B"s on each neuron. These will be distinguished (if it matters) by indicating the orientation of the dendrite the location is on. See Fig. 3.2 for a 3D view of the entire neuron. 55 Amount of neurotransmitter released (in millimolar concentration) 3.4

- 3.6 Synapse weight (g_M) (y-axis in μ S) necessary for a synapse at that distance (x-axis in μ m) from the axon tip to cause the specified membrane voltage (see legend: -60 mV to 10 mV in steps of 10 mV) at the axon tip after a single synapse event. Note that as the synapse location is farther from the soma, the synapse weight necessary to cause a given membrane voltage at the axon tip increases. Lines and symbols for -50 mV through 0 mV are plotted on top of each other. 63
- 3.7 The time required for the axon tip to reach maximum membrane voltage (y-axis in µs) when a synapse triggered at that distance from the axon tip (x-axis) with the synapse weight necessary (see Fig. 3.6) to reach the specified membrane voltage (see legend) is triggered. . . 64

- 3.10 Time series of the internal state of the neuron model after a single EPSP was triggered at a synapse located in the middle of a distal dendrite section with a synaptic weight of 3.45 nS. Each subplot plots a different variable ((a) V_m, (b) m_{IKdrSM}, (c) m_{IKaSM}, (d) h_{IKaSM}, (e) m_{INaSM}, and (f) h_{INaSM}) against simulation time (ms) for probes on axon-soma (a through f top) and dendrites (a through f bottom).

- 3.15 The time required for the axon tip to reach maximum membrane voltage (y-axis in µs) when a 0.1 ms square current pulse is injected at that distance from the axon tip (x-axis) with the current necessary (see Fig. 3.6) to reach the specified membrane voltage (see legend).75
- 3.17 The time required for the soma to reach maximum membrane voltage (y-axis in µs) when a 0.1 ms square current pulse is injected at that distance from the axon tip (x-axis) with the current necessary (see Fig. 3.16) to reach the specified membrane voltage (see legend). . . . 77

- 3.18 Maximum membrane voltage vs the amplitude of a 0.1 ms square current pulse injected at the soma (top) and time to reach that maximum (from simulation start (pulse occurs at 1ms)) vs injected current (bottom). Each colored line corresponds to a probe location labeled by (section type, axis direction, segment number). This figure corresponds to the threshold of 6.944nA for the simple neuron model given in Table 3.4.
- 3.20 The time required for the soma to reach maximum membrane voltage (y-axis in µs) when a synapse triggered at that distance from the axon tip (x-axis) with the synapse weight necessary (see Fig. 3.19) to reach the specified membrane voltage (see legend) is triggered.

4.3	The total number of active neurons (neurons with axon tip mem-	
	brane voltage > -10 mV) for all 18 bipolar stimulation combinations	
	(listed in Section 2.2.1), all neuron locations, and all 6 axon orien-	
	tations. For each type of stimulation and stimulation voltage magni-	
	tude, 14,256 neurons were tested	87
4.4	The total number of active neurons (neurons with axon tip membrane	
	voltage > -10 mV in response to stimulation, as plotted in Fig. 4.3)	
	separated by location in the transverse plane, for all 18 bipolar stim-	
	ulation combinations (listed in Section 2.2.1), all neuron locations,	
	and all 6 axon orientations. Note that GM1 is most dorsal, GM2 is	
	most ventral, and GM3 is in between. For each type of stimulation,	
	stimulation voltage magnitude, and position in the transverse plane,	
	4,752 neurons were tested.	88
4.5	The total number of active neurons (neurons with axon tip membrane	
	voltage > -10 mV in response to stimulation, as plotted in Fig. 4.3)	
	separated by axon orientation, for all 18 bipolar stimulation combi-	
	nations (listed in Section 2.2.1) and all neuron locations. Axons are	
	labeled by the direction of the distal tip from the soma. Note that ax-	
	ons pointing in the $+\hat{y}$ direction are the easiest to activate, followed	
	by $-\hat{y}$ with monophasic stimulation. For each type of stimulation,	
	stimulation voltage magnitude, and axon orientation, 2,376 neurons	
	were tested	89

90

- 4.8 Maximum membrane voltage in mV at the axon proper middle (segment 8) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).
- 4.9 Maximum membrane voltage in mV at the initial segment (segment
 0) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).

- 4.10 Maximum membrane voltage in mV at the axon hillock (segment
 0) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).
- 4.11 Maximum membrane voltage in mV at the soma (segment 0) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).

- 4.12 Maximum membrane voltage in mV at the distal dendrite middle (segment 8) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).
- 4.13 Maximum membrane voltage in mV at the distal dendrite tip (segment 16) (y-axis) plotted against stimulation voltage in mV (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of simulated neurons exhibiting given the voltage level (see gray colorbar). The colored dots represent neurons selected because their axon tip has a membrane voltage greater than -10 mV (referred to in this thesis as activation) using less than or equal to 5 V of stimulation. The color of each dot indicates the lowest magnitude of stimulation voltage required to activate that neuron (see right colorbar).

Membrane voltage (V_m) vs time, for a neuron with axon pointing to-4.14 wards Yp located at GM1_L_r5 exposed to 2.75 V of monophasic stimulation using combination A4pA5n. Each subfigure (a-f) plots V_m on a each segment of a different neurite: (a) $-\hat{x}$ dendrite, (b) $+\hat{x}$ dendrite, (c) $-\hat{y}$ dendrite, (d) $-\hat{z}$ dendrite, (e) $+\hat{z}$ dendrite, and (f) $+\hat{y}$ axon + soma. For each subfigure (a-f): The horizontal axis is the simulation time in ms. Each segment plot is labeled on the right side with (section type, orientation, segment number). The range of the vertical axis for the segment plots is indicated in the lower left corner. The minimum and maximum V_m for each segment is in the middle of each segment plot. Red areas under each segment plot indicate time periods in which V_m at that segment exceeds -10 mV. Subfigure (f) shows an antidromic action potential starting at the axon tip followed by an orthodromic action potential starting at the IS. The second action potential fails to cause neurotransmitter release most 4.15 (top): Membrane voltage (in mV) at different locations on a simulated neuron as a function of stimulation voltage (in mV, axis shared with bottom plot) for monophasic stimulation with combination A4pA5n, location GM1_L_r5, and axon in the $+\hat{y}$ direction. This is one of the configurations that results in neuron activation with the minimum amount of monophasic stimulation (in this case 2.75 V). The legend labels in the top plot are in the format (section type, orientation, segment number). See Fig. 3.3 for segment number locations by section type. Note that the axon tip (AxonProper, Yp, 16) is most stimulated compared to other probe locations if the stimulation voltage amplitude is less than 2.75 V. (bottom): The time of the maximum membrane voltage (in ms) for each probe vs stimulation voltage (in mV). The time of the maximum membrane voltage helps explain which parts of the neuron reach maximum first. Note that the stimulation pulse starts at 1 ms and peaks at

(top): Membrane voltage (in mV) at different locations on a 4.16 simulated neuron as a function of stimulation voltage (in mV, axis shared with bottom plot) for biphasic stimulation with combination A4pA5n, location GM1_L_r5, and axon in the $+\hat{y}$ direction. This is the same configuration as in Fig. 4.15, except biphasic instead of monophasic stimulation. This is one of the configurations that results in neuron activation with the minimum amount of biphasic stimulation (in this case 3.25 V). The legend labels in the top plot are in the format (section type, orientation, segment number). See Fig. 3.3 for segment number locations by section type. Note that the axon tip (AxonProper, 'Yp', 16) is most stimulated compared to other probe locations and linear as expected from Fig. 4.7b. (bottom): The time of the maximum membrane voltage (in ms) for each probe vs stimulation voltage (in mV). The time of the maximum membrane voltage helps explain which parts of the neuron reach maximum first. Note that the stimulation pulse starts at 1 ms the middle of the pulse is at 2.66 ms and the maximum amplitudes of the pulse occur at 2.66 ms \pm 0.16 ms. The first maximum amplitude occurs at 2.5 ms and the maximum in the axon proper tip, and the

Membrane voltage (V_m) vs time, for a neuron with axon pointing to-4.17 wards Yp located at GM1_L_r5 exposed to 3.25 V of biphasic stimulation using combination A4pA5n. Each subfigure (a-f) plots V_m on a each segment of a different neurite: (a) $-\hat{x}$ dendrite, (b) $+\hat{x}$ dendrite, (c) $-\hat{y}$ dendrite, (d) $-\hat{z}$ dendrite, (e) $+\hat{z}$ dendrite, and (f) $+\hat{y}$ axon + soma. For each subfigure (a-f): The horizontal axis is the simulation time in ms. Each segment plot is labeled on the right side with (section type, orientation, segment number). The range of the vertical axis for the segment plots is indicated in the lower left corner. The minimum and maximum V_m for each segment are in the middle of each segment plot. Red areas under each segment plot indicate time periods in which V_m at that segment exceeds -10 mV. Subfigure (f) shows that no action potential occurs and instead the stimulation pulse causes V_m at the axon tip to exceed -10 mV (and

 4.19 (top): Membrane voltage (in mV) as a function of stimulation voltage (in mV, axis shared with bottom plot) for biphasic stimulation with combination A4pA5n, location GM1_L_r5, and axon in the $-\hat{y}$ direction. This is the same configuration as in Fig. 4.16 except the axon is in the $-\hat{y}$ direction. This configuration results in an orthodromic action potential starting at the initial segment (IS) with 8 V of stimulation. This is one of the few neurons in Fig. 4.7b with a nonlinear response in the axon tip above 8 V. The legend labels in the top plot are in the format (section type, orientation, segment number). See Fig. 3.3 for segment number locations by section type. (bottom): The time of the maximum membrane voltage (in ms) for each probe vs stimulation voltage (in mV). The time of the maximum membrane voltage helps explain which parts of the neuron reach maximum first. Note that the stimulation pulse starts at 1 ms the middle of the pulse is at 2.66 ms and the maximum amplitudes of the pulse occur at 2.66 ms \pm 0.16 ms. The first maximum amplitude occurs at 2.5 ms and the maximum in the $+\hat{y}$ distal dendrite tip

- Maximum membrane voltage in mV at the axon distal tip (segment 4.22 16) (y-axis) plotted against the static extracellular voltage at the axon distal tip minus the static extracellular voltage at the soma (x-axis) for all neuron locations and all 18 electrode pair combinations using monophasic stimulation (top plot) and biphasic stimulation (bottom plot). The gray rectangles are a 2d histogram of the number of neurons (see gray colorbar). The colored dots are active neurons (axon tip has a membrane voltage greater than -10 mV) and are colored based on the stimulation voltage (see right colorbar). The red dotted horizontal line indicates the activation threshold (dots and gray
- 4.23 Monophasic stimulation using combination -A4pB4n. Electrode B4 has a positive phase and is labeled red. Electrode A4 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds $-10 \,\mathrm{mV}$ with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach $V_m > -10 \text{ mV}$. List of location, axon direction, and threshold: (GM1_L_r4, Yp, 9.5 V), (GM1_L_r4, Xn, 3.75 V), (GM3_L_r4, Xn, 10.0 V), and (GM1_R_r4, Yn, 7.0 V). . . . 124

- 4.28 Monophasic stimulation using combination A4pA5n. Electrode A4 has a positive phase and is labeled red. Electrode A5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r5, Yp, 2.75 V), (GM3_L_r5, Yp, 6.0 V), (GM2_L_r5, Yp, 8.25 V), (GM1_L_r4, Xp, 5.75 V), (GM1_L_r5, Xn, 6.25 V), (GM1_L_r4, Yn, 4.25 V), (GM3_L_r4, Yn, 9.75 V), (GM1_L_r4, Zp, 10.0 V), (GM1_L_r4and5, Zp, 5.75 V), (GM3_L_r4and5, Zp, 8.5 V), and (GM1_R_r4and5, Zp, 10.0 V).

4.30 Monophasic stimulation using combination A4pB5n. Electrode A4 has a positive phase and is labeled red. Electrode B5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_R_r5, Yp, 3.5 V), (GM1_L_r5, Yp, 7.0 V), (GM3_L_r5, Yp, 7.25 V), (GM1_L_r4, Xp, 5.5 V), (GM1_L_r4, Yn, 4.25 V), (GM3_L_r4, Yn, 10.0 V), (GM1_L_r4, Zp, -1.0 V), (GM1_L_r4and5, Zp, 6.5 V), (GM1_R_r4and5, Zp, 7.75 V), and (GM3_L_r4and5, Zp, 9.0 V).

4.31 Monophasic stimulation using combination -A4pC5n. Electrode C5 has a positive phase and is labeled red. Electrode A4 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds –10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > –10 mV. List of location, axon direction, and threshold: (GM1_L_r4and5, Zn, 7.25 V), (GM3_L_r4and5, Zn, 9.75 V), (GM1_L_r4, Yp, 2.75 V), (GM3_L_r4, Yp, 6.0 V), (GM2_L_r4, Yp, 8.25 V), (GM1_L_r4, Xn, 6.0 V), (GM1_R_r5, Xn, 5.25 V), (GM1_R_r5, Yn, 4.25 V), and (GM3_R_r5, Yn, 9.75 V).

- 4.32 Monophasic stimulation using combination A4pC5n. Electrode A4 has a positive phase and is labeled red. Electrode C5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_R_r5, Yp, 2.75 V), (GM3_R_r5, Yp, 6.0 V), (GM2_R_r5, Yp, 8.25 V), (GM1_L_r4, Xp, 5.25 V), (GM1_R_r5, Xp, 6.0 V), (GM1_L_r4, Yn, 4.25 V), (GM3_L_r4, Yn, 9.75 V), (GM1_L_r4and5, Zp, 7.75 V), (GM3_R_r4and5, Zp, 9.75 V).
- 4.33 Monophasic stimulation using combination -B4pB5n. Electrode B5 has a positive phase and is labeled red. Electrode B4 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_R_r4and5, Zn, 6.75 V), (GM1_L_r4and5, Zn, 6.75 V), (GM3_R_r4and5, Zn, 9.25 V), (GM3_R_r4and5, Zn, 9.25 V), (GM1_L_r5, Yn, 6.0 V), and (GM1_R_r5, Yn, 6.0 V). 134
- 4.35 Monophasic stimulation using combination -A3pA5n. Electrode A5 has a positive phase and is labeled red. Electrode A3 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3and4, Zn, 9.0 V), (GM1_L_r4and5, Zn, 9.75 V), (GM1_L_r3, Yp, 3.0 V), (GM3_L_r3, Yp, 6.25 V), (GM2_L_r3, Yp, 8.25 V), (GM1_L_r5, Xp, 6.0 V), (GM1_L_r3, Xn, 7.0 V), (GM1_L_r5, Yn, 4.5 V), and (GM3_L_r5, Yn, 9.75 V).

- 4.36 Monophasic stimulation using combination A3pA5n. Electrode A3 has a positive phase and is labeled red. Electrode A5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r5, Yp, 3.0 V), (GM3_L_r5, Yp, 6.25 V), (GM2_L_r5, Yp, 8.5 V), (GM1_L_r3, Xp, 6.0 V), (GM1_L_r5, Xn, 7.0 V), (GM1_L_r3, Yn, 4.5 V), (GM3_L_r3, Yn, 9.75 V), (GM1_L_r3and4, Zp, 9.75 V), and (GM1_L_r4and5, Zp, 9.0 V).

- 4.39 Monophasic stimulation using combination -A3pC5n. Electrode C5 has a positive phase and is labeled red. Electrode A3 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3and4, Zn, 9.0 V), (GM1_R_r4and5, Zn, 10.0 V), (GM1_L_r3, Yp, 3.0 V), (GM3_L_r3, Yp, 6.25 V), (GM2_L_r3, Yp, 8.5 V), (GM1_L_r3, Xn, 6.75 V), (GM1_R_r5, Xn, 6.0 V), (GM1_R_r5, Yn, 4.5 V), and (GM3_R_r5, Yn, 9.75 V).

- 4.40 Monophasic stimulation using combination A3pC5n. Electrode A3 has a positive phase and is labeled red. Electrode C5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_R_r5, Yp, 3.0 V), (GM3_R_r5, Yp, 6.25 V), (GM2_R_r5, Yp, 8.25 V), (GM1_L_r3, Xp, 6.0 V), (GM1_R_r5, Xp, 6.75 V), (GM1_L_r3, Yn, 4.5 V), (GM3_L_r3, Yn, 9.75 V), (GM1_L_r3and4, Zp, 10.0 V), and (GM1_R_r4and5, Zp, 9.0 V).
- 4.41 Monophasic stimulation using combination -B3pB5n. Electrode B5 has a positive phase and is labeled red. Electrode B3 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3and4, Zn, 10.0 V), (GM1_R_r3and4, Zn, 10.0 V), (GM1_L_r3, Yp, 3.75 V), (GM1_R_r3, Yp, 3.75 V), (GM1_L_r5, Yn, 6.25 V), and (GM1_R_r5, Yn, 6.25 V). 142

- 4.42 Monophasic stimulation using combination B3pB5n. Electrode B3 has a positive phase and is labeled red. Electrode B5 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r5, Yp, 3.75 V), (GM1_R_r5, Yp, 3.75 V), (GM1_L_r3, Yn, 6.25 V), (GM1_R_r3, Yn, 6.25 V), (GM1_L_r4and5, Zp, 10.0 V), and (GM1_R_r4and5, Zp, 10.0 V). . . . 143
- 4.43 Monophasic stimulation using combination -A3pA6n. Electrode A6 has a positive phase and is labeled red. Electrode A3 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 3.25 V), (GM3_L_r3, Yp, 6.75 V), (GM2_L_r3, Yp, 9.0 V), (GM1_L_r6, Xp, 6.5 V), (GM1_L_r3, Xn, 7.5 V), and (GM1_L_r6, Yn, 4.75 V). 144

- 4.45 Monophasic stimulation using combination -A3pB6n. Electrode B6 has a positive phase and is labeled red. Electrode A3 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 3.25 V), (GM3_L_r3, Yp, 6.75 V), (GM2_L_r3, Yp, 9.0 V), (GM1_L_r3, Xn, 7.5 V), (GM1_R_r6, Yn, 6.75 V), and (GM1_L_r6, Yn, 6.75 V). . . . 146

- 4.51 Monophasic stimulation using combination -A2pA6n. Electrode A6 has a positive phase and is labeled red. Electrode A2 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r2, Yp, 3.5 V), (GM3_L_r2, Yp, 7.25 V), (GM2_L_r2, Yp, 9.5 V), (GM1_L_r6, Xp, 7.0 V), (GM1_L_r2, Xn, 7.75 V), and (GM1_L_r6, Yn, 5.0 V). 152

- 4.52 Monophasic stimulation using combination A2pA6n. Electrode A2 has a positive phase and is labeled red. Electrode A6 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds –10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > –10 mV. List of location, axon direction, and threshold: (GM1_L_r6, Yp, 3.5 V), (GM3_L_r6, Yp, 7.25 V), (GM2_L_r6, Yp, 9.5 V), (GM1_L_r2, Xp, 7.0 V), (GM1_L_r6, Xn, 8.0 V), and (GM1_L_r2, Yn, 5.0 V). 153
- 4.53 Monophasic stimulation using combination -A2pB6n. Electrode B6 has a positive phase and is labeled red. Electrode A2 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r2, Yp, 3.5 V), (GM3_L_r2, Yp, 7.25 V), (GM2_L_r2, Yp, 9.5 V), (GM1_L_r2, Xn, 7.75 V), (GM1_L_r6, Yn, 7.25 V), and (GM1_R_r6, Yn, 7.0 V). . . . 154

- 4.55 Monophasic stimulation using combination -A2pC6n. Electrode C6 has a positive phase and is labeled red. Electrode A2 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r2, Yp, 3.5 V), (GM3_L_r2, Yp, 7.25 V), (GM2_L_r2, Yp, 9.5 V), (GM1_L_r2, Xn, 7.75 V), (GM1_R_r6, Xn, 7.0 V), and (GM1_R_r6, Yn, 5.0 V). . . . 156

- 4.56 Monophasic stimulation using combination A2pC6n. Electrode A2 has a positive phase and is labeled red. Electrode C6 has a negative phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds –10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > –10 mV. List of location, axon direction, and threshold: (GM1_R_r6, Yp, 3.5 V), (GM3_R_r6, Yp, 7.25 V), (GM2_R_r6, Yp, 9.5 V), (GM1_L_r2, Xp, 7.0 V), (GM1_R_r6, Xp, 8.0 V), and (GM1_L_r2, Yn, 5.0 V). . . 157

- 4.60 Biphasic stimulation using combination A4pB4n. Electrode A4 has a positive phase first followed by a negative phase and is labeled red. Electrode B4 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mVwith no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach $V_m > -10 \text{ mV}$. List of location, axon direction, and threshold: (GM1_R_r4, Yp, 4.0 V), (GM3_R_r4, Yp, 9.0 V), (GM1_L_r4, Xp, 6.5 V), and (GM1_L_r4, Xn, 9.0 V). 161
- 4.61 Biphasic stimulation using combination -A4pC4n. Electrode C4 has a positive phase first followed by a negative phase and is labeled red. Electrode A4 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r4, Yp, 4.0 V), (GM1_R_r4, Yp, 8.75 V), (GM3_L_r4, Yp, 8.0 V), (GM1_L_r4, Xn, 5.5 V), (GM1_R_r4, Xn, 5.0 V), (GM3_R_r4, Xn, 7.0 V), (GM1_L_r4, Yn, 8.5 V), and (GM1_R_r4, Yn, 7.0 V).

- 4.63 Biphasic stimulation using combination -A4pA5n. Electrode A5 has a positive phase first followed by a negative phase and is labeled red. Electrode A4 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r4and5, Zn, 7.0 V), (GM1_L_r4, Yp, 3.25 V), (GM1_L_r5, Yp, 7.5 V), (GM3_L_r4, Yp, 6.75 V), (GM2_L_r4, Yp, 9.25 V), (GM1_L_r5, Xp, 7.25 V), (GM1_L_r4, Xn, 8.0 V), (GM1_L_r4, Yn, 8.0 V), and (GM1_L_r5, Yn, 6.0 V).

4.64 Biphasic stimulation using combination A4pA5n. Electrode A4 has a positive phase first followed by a negative phase and is labeled red. Electrode A5 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r4, Yp, 7.5 V), (GM1_L_r5, Yp, 3.25 V), (GM3_L_r5, Yp, 6.75 V), (GM2_L_r5, Yp, 9.25 V), (GM1_L_r4, Xp, 7.25 V), (GM1_L_r5, Xn, 7.75 V), (GM1_L_r4, Yn, 6.0 V), (GM1_L_r5, Yn, 8.0 V), and (GM1_L_r4and5, Zp, 7.25 V).

- 4.65 Biphasic stimulation using combination -A4pB5n. Electrode B5 has a positive phase first followed by a negative phase and is labeled red. Electrode A4 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r4and5, Zn, 7.5 V), (GM1_L_r4, Yp, 3.5 V), (GM1_R_r5, Yp, 8.0 V), (GM1_L_r5, Yp, 7.75 V), (GM3_L_r4, Yp, 6.75 V), (GM2_L_r4, Yp, 9.5 V), (GM1_L_r4, Xn, 7.75 V), (GM1_L_r4, Yn, 8.0 V), (GM1_R_r5, Yn, 8.5 V), and (GM1_L_r5, Yn, 8.5 V).
- 4.66 Biphasic stimulation using combination A4pB5n. Electrode A4 has a positive phase first followed by a negative phase and is labeled red. Electrode B5 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r4, Yp, 7.5 V), (GM1_R_r5, Yp, 3.75 V), (GM1_L_r5, Yp, 3.75 V), (GM1_L_r4, Yp, 7.0 V), (GM1_L_r4, Yn, 6.0 V), (GM1_L_r4and5, Zp, 8.0 V), and (GM1_R_r4and5, Zp, 9.5 V).167

- Biphasic stimulation using combination -A4pC5n. Electrode C5 has a positive phase first followed by a negative phase and is labeled red. Electrode A4 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach $V_m > -10 \text{ mV}$. List of location, axon direction, and threshold: (GM1_L_r4and5, Zn, 8.5 V), (GM1_R_r4and5, Zn, 9.75 V), (GM1_L_r4, Yp, 3.5 V), (GM1_R_r5, Yp, 7.75 V), (GM3_L_r4, Yp, 6.75 V), (GM2_L_r4,

Yp, 9.25 V), (GM1_L_r4, Xn, 7.5 V), (GM1_R_r5, Xn, 7.0 V),

4.67

- 4.73 Biphasic stimulation using combination -A3pB5n. Electrode B5 has a positive phase first followed by a negative phase and is labeled red. Electrode A3 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 3.75 V), (GM1_R_r5, Yp, 8.5 V), (GM1_L_r5, Yp, 8.5 V), (GM1_L_r3, Xn, 8.75 V), (GM1_L_r3, Yn, 8.75 V), (GM1_R_r5, Yn, 8.75 V), and (GM1_L_r5, Yn, 8.75 V). 174

- 4.76 Biphasic stimulation using combination A3pC5n. Electrode A3 has a positive phase first followed by a negative phase and is labeled red. Electrode C5 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach $V_m > -10 \text{ mV}$. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 8.25 V), (GM1_R_r5, Yp, 3.75 V), (GM3_R_r5, Yp, 7.0 V), (GM2_R_r5, Yp, 9.5 V), (GM1_L_r3, Xp, 8.0 V), (GM1_R_r5, Xp, 8.75 V), (GM1_L_r3,

- 4.81 Biphasic stimulation using combination -A3pB6n. Electrode B6 has a positive phase first followed by a negative phase and is labeled red. Electrode A3 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach V_m > -10 mV. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 4.0 V), (GM1_R_r6, Yp, 9.25 V), (GM1_L_r6, Yp, 9.25 V), (GM1_R_r6, Yn, 9.25 V), and (GM1_L_r6, Yn, 9.5 V).

- 4.86 Biphasic stimulation using combination B3pB6n. Electrode B3 has a positive phase first followed by a negative phase and is labeled red. Electrode B6 has a negative phase first followed by a positive phase and is labeled blue. All other electrodes are floating and labeled purple. Soma, AH, IS, and AP are displayed as red lines for those neurons whose axon tip membrane voltage exceeds -10 mV with no more than 10 V of stimulation. Dendrites are not displayed. The color of the cube at each axon tip indicates stimulation voltages required for axon tip to reach $V_m > -10 \text{ mV}$. List of location, axon direction, and threshold: (GM1_L_r3, Yp, 9.0 V), (GM1_R_r3, Yp, 9.0 V), (GM1_L_r6, Yp, 4.5 V), (GM1_R_r6, Yp, 4.5 V), (GM3_L_r6, Yp, 9.0 V), (GM3_R_r6, Yp, 9.0 V), (GM1_L_r3, Yn,

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.1 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron's synapse is at segment 16 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to biphasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum pulse amplitudes occur at t=77.66ms \pm 0.16ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$, where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (-5.0V, 4.783nS, 10, 6), (-5.0V, 4.776nS, 9, 5), (-5.0V, 4.769nS, 9, 5), (-4.0V, 4.783nS, 8, 5), (-4.0V, 4.776nS, 8, 5), (-4.0V, 4.769nS, 8, 5), (-3.0V, 4.783nS, 8, 5), (-3.0V, 4.776nS, 8, 5), (-3.0V, 4.769nS, 7, 4), (-2.0V, 4.783nS, 8, 5), (-2.0V, 4.776nS, 7, 4), (-2.0V, 4.769nS, 7, 3), (-1.0V, 4.783nS, 6, 5), (-1.0V, 4.776nS, 5, 1), (-1.0V, 4.769nS, 5, 0), (-0.5V, 4.783nS, 6, 2), and (-0.5V, 4.776nS,

5.4 Stimulation + EPSP: Each subplot plots a different variable ((a) V_m , (b) m_{IKdrSM} , (c) m_{IKaSM} , (d) h_{IKaSM} , (e) m_{INaSM} , and (f) h_{INaSM}) against simulation time (ms) for probes on axon-soma (sub-top) and dendrites (sub-bottom). Measured on neuron GM1_L_r5_Yn exposed to -2.0 V of biphasic stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum amplitudes of the pulse occur at t=77.66ms ± 0.16ms. An Exp2Syn synapse was triggered at t=66.0 ms with a synaptic weight of 4.783nS. The synapse was located at segment 16 on the distal dendrite that points in the + \hat{x} direction. 209
Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.5 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 16 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to monophasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and has a maximum amplitude at t=77.13ms. This neuron is active without any EPSPs if exposed to -5.0V of stimulation. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (-4.0V, 4.783nS, 8, 7), (-4.0V, 4.776nS, 8, 7), (-4.0V, 4.769nS, 7, 7), (-3.0V, 4.783nS, 8, 3), (-3.0V, 4.776nS, 8, 3), (-3.0V, 4.769nS, 8, 3), (-2.0V, 4.783nS, 7, 0), (-2.0V, 4.776nS, 6, 0), (-2.0V, 4.769nS, 6, 0), (-1.0V, 4.783nS, 7, 0), (-1.0V, 4.776nS, 6, 0), (-1.0V, 4.769nS, 6, 0), (-0.5V, 4.783nS, 6, 0), (-0.5V, 4.776nS,

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.9 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 16 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to monophasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and has a maximum amplitude at t=77.13ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (5.0V, 4.783nS, 7, 9), (5.0V, 4.776nS, 7, 9), (5.0V, 4.769nS, 6, 9), (4.0V, 4.783nS, 6, 10), (4.0V, 4.776nS, 6, 10), (4.0V, 4.769nS, 6, 10), (3.0V, 4.783nS, 5, 14), (3.0V, 4.776nS, 5, 13), (3.0V, 4.769nS, 5, 12), (2.0V, 4.783nS, 2, 14), (2.0V, 4.776nS, 2, 14), (2.0V, 4.769nS, 2, 13), (1.0V, 4.783nS, 1, 14), (1.0V, 4.776nS, 1, 14), (1.0V, 4.769nS, 1, 10), (0.5V, 4.783nS, 1, 14), (0.5V,

- 5.13 2d histogram of the number of facilitated neurons with synapses in the middle (segment 8) of the distal dendrite for: (a) monophasic and (b) biphasic stimulation. The y-axis of each 2d histogram shows the number of synapse trigger times which result in facilitation (or stimOnly if no EPSP is required to activate the neuron at that value of V_s). Understanding the x-axis of each 2d histogram requires looking at the background columns behind the histogram. The magnitude of stimulation voltage $(|V_s|)$ is represented by the color of each column (see right color bar to the right of each plot). The synapse weight of each column is indicated by the hatching of each column (see legend to the far right of each histogram). The number of neurons in each square is indicated by the gray-scale colorbar just to the right of the histogram. Each column consists of the results from simulating 71280 neurons under 18 electrode combinations (described in

5.14 2d histogram of the number of facilitated neurons with synapses at the distal tip (segment 16) of the distal dendrite for: (a) monophasic and (b) biphasic stimulation. The y-axis of each 2d histogram shows the number of synapse trigger times which result in facilitation (or stimOnly if no EPSP is required to activate the neuron at that value of V_s). Understanding the x-axis of each 2d histogram requires looking at the background columns behind the histogram. The magnitude of stimulation voltage ($|V_s|$) is represented by the color of each column (see right color bar to the right of each plot). The synapse weight of each column is indicated by the hatching of each column (see legend to the far right of each histogram). The number of neurons in each square is indicated by the gray-scale colorbar just to the right of the histogram. Each column consists of the results from simulating 71280 neurons under 18 electrode combinations (described in

Stacked bar charts showing the number of active neurons (from fa-5.15 cilitation or stimulation-only) where each column corresponds to a different pair of stimulation voltage ($|V_s|$) and synapse weight. These charts are for neurons with synapses in the middle (segment 8) of the distal dendrite and (a) monophasic and (b) biphasic stimulation. Each column consists of the results from simulating 71280 neurons under 18 electrode combinations (described in Section 5.3). Understanding the x-axis of each 2d histogram requires looking at the background columns behind the histogram. The magnitude of stimulation voltage $(|V_s|)$ is represented by the color of each column (see virdis (yellow-green-blue color map) color bar to the right of each plot). The synapse weight of each column is indicated by the hatching of each column (see legend to the far right of each histogram). The color of each bar in the stacks (see legend to the right of the colorbar) indicates the number of synapse trigger times which result in facilitation (or stimOnly if the stimulation by itself causes activation). The maximum of the y-axis is the total number of simulated

- Stacked bar charts showing the number of active neurons (from fa-5.16 cilitation or stimulation-only) where each column corresponds to a different pair of stimulation voltage $(|V_s|)$ and synapse weight. These charts are for neurons with synapses at the distal tip (segment 16) of the distal dendrite and (a) monophasic and (b) biphasic stimulation. Each column consists of the results from simulating 71280 neurons under 18 electrode combinations (described in Section 5.3). Understanding the x-axis of each 2d histogram requires looking at the background columns behind the histogram. The magnitude of stimulation voltage $(|V_s|)$ is represented by the color of each column (see virdis (yellow-green-blue color map) color bar to the right of each plot). The synapse weight of each column is indicated by the hatching of each column (see legend to the far right of each histogram). The color of each bar in the stacks (see legend to the right of the colorbar) indicates the number of synapse trigger times which result in facilitation (or stimOnly if the stimulation by itself causes activation). The maximum of the y-axis is the total number of simulated
- 5.17 These two figures show (a) the largest 3 synapse weights from Fig. 5.15a and (b) Fig. 5.16a. See those figures for detailed description. The y-axis is a \log_{10} scale with the total number of simulated neurons (71280) indicated by a red horizontal line. A greater number of neurons with synapses triggered on the distal tips of the distal dendrites have facilitation windows larger than 2 trigger time samples compared with synapses in the middle of the dendrite for synapse weights that are subthreshold by the same amount. 227

- 5.18 These two figures show (a) the largest 3 synapse weights from Fig. 5.15b and (b) Fig. 5.16b. See those figures for detailed description. The y-axis is a \log_{10} scale with the total number of simulated neurons (71280) indicated by a red horizontal line. A greater number of neurons with synapses triggered on the distal tips of the distal dendrites have facilitation windows larger than 2 trigger time samples compared with synapses in the middle of the dendrite for synapse weights that are subthreshold by the same amount. 228
- 5.19 Example histogram plot showing the regions of example feature x that can be used for prediction of facilitation. The y-axis is the number of trigger points facilitated above threshold (-10 mV). Each trigger corresponds with about 5 ms of time during which a triggered synapse would cause facilitation. For each feature, active and nonactive classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below for feature value f_0 , where T=1 and T=0 indicates that the neuron is active and non-active respectively.230

lxxxiii

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.21 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 16 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to biphasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum amplitudes of the pulse occur at t=77.66ms \pm 0.16ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (5.0V, 4.783nS, 9, 6), (5.0V, 4.776nS, 8, 6), (5.0V, 4.769nS, 8, 6), (4.0V, 4.783nS, 8, 6), (4.0V, 4.776nS, 8, 6), (4.0V, 4.769nS, 8, 6), (3.0V, 4.783nS, 8, 6), (3.0V, 4.776nS, 7, 6), (3.0V, 4.769nS, 7, 5), (2.0V, 4.783nS, 8, 6), (2.0V, 4.776nS, 7, 5), (2.0V, 4.769nS, 6, 4), (1.0V, 4.783nS, 7, 5), (1.0V, 4.776nS, 6, 0), (1.0V, 4.769nS, 5, 0), (0.5V, 4.783nS, 5,

- 5.23 Stimulation only: Each subplot plots a different variable ((a) V_m , (b) m_{IKdrSM} , (c) m_{IKaSM} , (d) h_{IKaSM} , (e) m_{INaSM} , and (f) h_{INaSM}) against simulation time (ms) for probes on axon-soma (sub-top) and dendrites (sub-bottom). All data measured using neuron GM1_L_r5_Yn exposed to 2.0 V of biphasic stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum amplitudes of the pulse occur at t=77.66ms ± 0.16ms. . 251

lxxxvi

lxxxvii

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.27 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 8 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to biphasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum amplitudes of the pulse occur at t=77.66ms \pm 0.16ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (-5.0V, 3.45nS, 9, 6), (-5.0V, 3.443nS, 8, 6), (-5.0V, 3.436nS, 8, 6), (-5.0V, 3.422nS, 7, 5), (-5.0V, 3.394nS, 7, 4), (-5.0V, 3.337nS, 7, 3), (-5.0V, 3.225nS, 6, 1), (-5.0V, 3.0nS, 4, 0), (-4.0V, 3.45nS, 8, 6), (-4.0V, 3.443nS, 7, 5), (-4.0V, 3.436nS, 7, 5), (-4.0V, 3.422nS, 7, 4), (-4.0V, 3.394nS, 6, 2), (-4.0V, 3.337nS, 6, 1), (-4.0V, 3.225nS, 4, 0), (-4.0V, 3.0nS, 2, 0), (-3.0V, 3.45nS, 8, 6), (-3.0V, 3.443nS, 7, 4), (-3.0V, 3.436nS, 7, 3), (-3.0V, 3.422nS, 6, 2), (-3.0V, 3.394nS, 5, 0), (-3.0V, 3.337nS, 4, 0), (-3.0V, 3.225nS, 1, 0), (-2.0V, 3.45nS, 6, 5), (-2.0V, 3.443nS, 5, 2), (-2.0V, 3.436nS, 5, 1), (-2.0V, 3.422nS, 4, 0), (-2.0V, 3.394nS, 3, 0), (-1.0V, 3.45nS, 6, 3), (-1.0V, 3.443nS, 4, 0), (-1.0V, 3.436nS, 3, 0),

lxxxviii

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.32 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 8 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to biphasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and the maximum amplitudes of the pulse occur at t=77.66ms \pm 0.16ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (5.0V, 3.45nS, 8, 7), (5.0V, 3.443nS, 8, 6), (5.0V, 3.436nS, 8, 6), (5.0V, 3.422nS, 7, 5), (5.0V, 3.394nS, 7, 4), (5.0V, 3.337nS, 7, 3), (5.0V, 3.225nS, 6, 1), (5.0V, 3.0nS, 5, 0), (4.0V, 3.45nS, 8, 7), (4.0V, 3.443nS, 7, 6), (4.0V, 3.436nS, 7, 5), (4.0V, 3.422nS, 7, 4), (4.0V, 3.394nS, 6, 3), (4.0V, 3.337nS, 6, 1), (4.0V, 3.225nS, 5, 0), (4.0V, 3.0nS, 1, 0), (3.0V, 3.45nS, 7, 6), (3.0V, 3.443nS, 7, 5), (3.0V, 3.436nS, 6, 4), (3.0V, 3.422nS, 6, 2), (3.0V, 3.394nS, 5, 0), (3.0V, 3.337nS, 4, 0), (3.0V, 3.225nS, 1, 0), (2.0V, 3.45nS, 7, 6), (2.0V, 3.443nS, 6, 3), (2.0V, 3.436nS, 5, 1), (2.0V, 3.422nS, 5, 0), (2.0V, 3.394nS, 4, 0), (1.0V, 3.45nS, 6, 3), (1.0V, 3.443nS, 4, 0), (1.0V, 3.436nS, 2, 0), (0.5V,

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.37 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 8 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to monophasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and has a maximum amplitude at t=77.13 ms. This neuron is active without any EPSPs if exposed to -5.0V of stimulation. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (-4.0V, 3.45nS, 8, 8), (-4.0V, 3.443nS, 8, 7), (-4.0V, 3.436nS, 8, 7), (-4.0V, 3.422nS, 7, 7), (-4.0V, 3.394nS, 8, 7), (-4.0V, 3.337nS, 8, 7), (-4.0V, 3.225nS, 8, 6), (-4.0V, 3.0nS, 8, 5), (-3.0V, 3.45nS, 8, 4), (-3.0V, 3.443nS, 8, 4), (-3.0V, 3.436nS, 7, 3), (-3.0V, 3.422nS, 7, 3), (-3.0V, 3.394nS, 7, 2), (-3.0V, 3.337nS, 7, 0), (-3.0V, 3.225nS, 6, 0), (-3.0V, 3.0nS, 4, 0), (-2.0V, 3.45nS, 7, 2), (-2.0V, 3.443nS, 7, 1), (-2.0V, 3.436nS, 6, 1), (-2.0V, 3.422nS, 6, 0), (-2.0V, 3.394nS, 5, 0), (-2.0V, 3.337nS, 5, 0), (-2.0V, 3.225nS, 3, 0), (-1.0V, 3.45nS, 7, 0), (-1.0V, 3.443nS, 6, 0), (-1.0V, 3.436nS, 6, 0), (-1.0V, 3.422nS, 5, 0), (-1.0V, 3.394nS, 4, 0), (-0.5V, 3.45nS, 7, 0), (-0.5V, 3.443nS, 6, 0), (-0.5V, 3.436nS, 5, 0), and (-0.5V, 3.422nS,

Membrane voltage at the axon tip (V_m^{axontip}) vs synapse trigger 5.42 time for a neuron whose axon points in the $-\hat{y}$ direction located at GM1_L_r5. This neuron has a synapse triggered at segment 8 on the distal dendrite that points in the $+\hat{x}$ direction and is exposed to monophasic epidural stimulation using stimulating electrode combination A4pA5n. The stimulation pulse starts at t=76.0ms and has a maximum amplitude at t=77.13ms. The following list contains tuples of the form $(V_s, w, \#T_B, \#T_A)$ where V_s is the stimulation voltage, w is the synapse weight, and $(\#T_B, \#T_A)$ is the number of synapse trigger time samples (x-axis samples in the above graph) before or after the stimulation pulse, respectively, given the values of V_s and w that result in neuron activation (a value of V_m^{axontip} above -10 mV) : (5.0V, 3.45nS, 6, 9), (5.0V, 3.443nS, 6, 9), (5.0V, 3.436nS, 6, 9), (5.0V, 3.422nS, 6, 8), (5.0V, 3.394nS, 5, 7), (5.0V, 3.337nS, 5, 6), (5.0V, 3.225nS, 4, 4), (5.0V, 3.0nS, 3, 2), (4.0V, 3.45nS, 6, 10), (4.0V, 3.443nS, 6, 10), (4.0V, 3.436nS, 5, 9), (4.0V, 3.422nS, 5, 8), (4.0V, 3.394nS, 5, 7), (4.0V, 3.337nS, 4, 5), (4.0V, 3.225nS, 4, 2), (3.0V, 3.45nS, 4, 13), (3.0V, 3.443nS, 4, 11), (3.0V, 3.436nS, 4, 9), (3.0V, 3.422nS, 4, 7), (3.0V, 3.394nS, 3, 4), (3.0V, 3.337nS, 0, 1), (2.0V, 3.45nS, 0, 14), (2.0V, 3.443nS, 0, 11), (2.0V, 3.436nS, 0, 7), (2.0V, 3.422nS, 0, 3), (1.0V, 3.45nS, 0, 14), (1.0V,

5.47 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.0 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 537 are facilitated, and 426743 are non-active. 5.48 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.225 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 1647 are facilitated, and 425633 are non-active.

5.49 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.338 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 4248 are facilitated, and 423032 are non-active.

5.50 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.394 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 9670 are facilitated, and 417610 are non-active.

5.51 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.422 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 24532 are facilitated, and 402748 are non-active. 5.52 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.436 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 62471 are facilitated, and 364809 are non-active. . . . 287 5.53 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.443 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 110804 are facilitated, and 316476 are non-active.

5.54 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.45 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 257472 are facilitated, and 169808 are non-active.

- Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.769 nS using features $f_0 = V_{static}^{IS} V_{static}^{Soma}$, $f_1 = V_{static}^{Synapse} V_{static}^{Soma}$, $f_2 = avg_{\forall dendrites}(V_{static}^{DistalDendriteMiddle}) V_{static}^{Soma}$, and $f_3 = \min_{\forall dendrites}(V_{static}^{DistalDendriteMiddle}) V_{static}^{Soma}$. Each feature is on the
- $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 82986 are facilitated, and 344294 are non-active. 290

5.55

5.56 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.776 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 120616 are facilitated, and 306664 are non-active. . 291
Predicting facilitation for all combinations using biphasic epidural 5.57 stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.783 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 256925 are facilitated, and 170355 are non-active.

292

Predicting facilitation for all combinations using monophasic epidu-5.58 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.0 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 2562 are facilitated, and 424473 are non-active. . . . 293

Predicting facilitation for all combinations using monophasic epidu-5.59 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.225 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 6522 are facilitated, and 420513 are non-active.

294

Predicting facilitation for all combinations using monophasic epidu-5.60 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.338 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 16246 are facilitated, and 410789 are non-active. 295

Predicting facilitation for all combinations using monophasic epidu-5.61 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.394 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 46322 are facilitated, and 380713 are non-active. 296

Predicting facilitation for all combinations using monophasic epidu-5.62 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.422 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 87686 are facilitated, and 339349 are non-active. 297

Predicting facilitation for all combinations using monophasic epidu-5.63 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.436 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 133965 are facilitated, and 293070 are non-active. 298

Predicting facilitation for all combinations using monophasic epidu-5.64 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.443 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 185287 are facilitated, and 241748 are non-active. 299 5.65 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.45 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 =$ $V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \text{avg}_{\forall \text{dendrites}}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}, \text{ and}$ $f_3 = \min_{\forall dendrites} (V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and nonactive respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 319226 are facilitated, and 107809 are non-active. 300 5.66 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.769 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 = V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \operatorname{avg}_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}},$ and $f_3 = \min_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 176092 are facilitated, and 250943 are non-active. 301

Predicting facilitation for all combinations using monophasic epidu-5.67 ral stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.776 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 = V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \operatorname{avg}_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}},$ and $f_3 = \min_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 209901 are facilitated, and 217134 are non-active. 302

Predicting facilitation for all combinations using monophasic epidu-5.68 ral stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.783 nS using features $f_0 = V_{static}^{IS} - V_{static}^{Soma}$, $f_1 = V_{static}^{\text{Synapse}} - V_{static}^{\text{Soma}}, f_2 = \operatorname{avg}_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}},$ and $f_3 = \min_{\forall dendrites}(V_{static}^{\text{DistalDendriteMiddle}}) - V_{static}^{\text{Soma}}$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 278554 are facilitated, and 148481 are non-active. 303

Predicting facilitation for all combinations using biphasic epidu-5.69 ral stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.0 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 537 are facilitated, and 426743 are non-active. 305 5.70 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.225 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without

Predicting facilitation for all combinations using biphasic epidural 5.71 stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.338 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without

Predicting facilitation for all combinations using biphasic epidural 5.72 stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.394 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without

Predicting facilitation for all combinations using biphasic epidural 5.73 stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.422 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 24532 are facilitated, and 402748 are non-active. 309

Predicting facilitation for all combinations using biphasic epidural 5.74 stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.436 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 62471 are facilitated, and 364809 are non-active. 310

cxxvii

5.75 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.443 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 110804 are facilitated, and 316476 are non-active. 311

cxxviii

5.76 Predicting facilitation for all combinations using biphasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.45 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 257472 are facilitated, and 169808 are non-active. 312

Predicting facilitation for all combinations using biphasic epidural 5.77 stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.769 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 82986 are facilitated, and 344294 are non-active. 313

Predicting facilitation for all combinations using biphasic epidural 5.78 stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.776 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 120616 are facilitated, and 306664 are non-active. 314

Predicting facilitation for all combinations using biphasic epidural 5.79 stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.783 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 400 are active without the EPSP, 256925 are facilitated, and 170355 are non-active. 315

Predicting facilitation for all combinations using monophasic 5.80 epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.0 nS using features $f_0 = \max_t(V_m^{AH}(t))$, $f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and } f_3 =$ $\max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without 5.81 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.225 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without

Predicting facilitation for all combinations using monophasic 5.82 epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.338 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 16246 are facilitated, and 410789 are non-active. 318

Predicting facilitation for all combinations using monophasic 5.83 epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.394 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without

Predicting facilitation for all combinations using monophasic 5.84 epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.422 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 87686 are facilitated, and 339349 are non-active. 320 5.85 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.436 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 133965 are facilitated, and 293070 are non-active. 321

cxxxviii

5.86 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.443 nS using features f_0 = $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 185287 are facilitated, and 241748 are non-active. 322

Predicting facilitation for all combinations using monophasic 5.87 epidural stimulation with a synapse triggered on a distal dendrite at segment 8 with weight 3.45 nS using features $f_0 =$ $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 319226 are facilitated, and 107809 are non-active. 323

Predicting facilitation for all combinations using monophasic 5.88 epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.769 nS using features f_0 = $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without

Predicting facilitation for all combinations using monophasic 5.89 epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.776 nS using features f_0 = $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 209901 are facilitated, and 217134 are non-active. 325 5.90 Predicting facilitation for all combinations using monophasic epidural stimulation with a synapse triggered on a distal dendrite at segment 16 with weight 4.783 nS using features f_0 = $\max_t(V_m^{\text{AH}}(t)), f_1 = \min_t(V_m^{\text{Synapse}}(t)), f_2 = \max_t(V_m^{\text{Synapse}}(t)), \text{ and }$ $f_3 = \max_{\forall dendrites} \max_t(V_m^{\text{DistalDendriteMiddle}}(t))$. Each feature is on the x-axis in a separate subplot above with the number of trigger points facilitated above threshold (-10 mV) as the y-axis. Each subplot consists of three 2D histograms (showing the number of neuron simulations in each square), shades of grey (unclassified), shades of red (classified as active), and shades of blue (classified as non-active). For each feature active and non-active classification regions of unclassified samples are drawn with a yellow and cyan background respectively. These classification regions are also written as rules below, where T=1 and T=0 indicates that the neuron is active and non-active respectively. The number of samples of neurons caught by each rule is specified in the comment after each rule. Using the decision regions in that subplot and those above, the percent of all samples classified (id), active samples classified (id+), and non-active samples classified (id-) are labeled in each subplot. There are a total of 427680 samples of which 645 are active without the EPSP, 278554 are facilitated, and 148481 are non-active. 326

cxliii LIST OF TABLES

1.1	This table summarizes the possible results of varying amounts of	
	stimulation and synaptic input for a neuron in the spinal cord. Sub-	
	threshold and super-threshold refer to the threshold of synaptic input	
	or stimulation voltage necessary for a given neuron to release neuro-	
	transmitters. Neurotransmitter release in response to sub-threshold	
	synaptic input can be facilitated by sub-threshold stimulation under	
	certain conditions as seen in Chapter 5	4
2.1	This table shows the names of the electrodes and the orientation of	
	the array in the spinal cord as if you are looking down at the back	
	of the rat with its head pointed towards the top of the page. (Note	
	that \odot means that the dorsal direction is pointing out of the page and	
	the \otimes symbol indicates that the ventral direction is into the page.)	
	Figures 4.1 and 4.2 show the labeled electrode array in the simulated	
	spinal cord	18
2.2	Cole-Cole parameters	31
2.3	Diffusion tensor coefficients for rat spinal cord obtained from (Gu-	
	lani et al., 1997)	33
2.4	Conductivity values with units S m^{-1} \ldots	35
2.5	Real relative permittivity values (unit less)	36
2.6	Number of unique bipolar combinations	40
3.1	Simple neuron ion channel conductances: the maximum conduc-	
	tances of the sodium channel $(g_{na,max})$, potassium fast channel	
	$(g_{K_A,max})$, and potassium delayed rectifier channel $(g_{K_{dr},max})$ for	
	each section type.	51

	cxliv	
3.2	Simple neuron physical parameters	54
3.3	Simple neuron segments based on "d_lambda" rule from (M. L.	
	Hines and N. T. Carnevale, 2001)	54
3.4	Current injection thresholds necessary for a current pulse with a	
	width of 0.1 ms (\square column) or 5 ms (\square column) injected into	
	the soma to cause the soma's membrane voltage to exceed -10 mV .	
	Three neuron models are presented: the simple neuron model used	
	in the rest of the thesis, a modified version of the simple neuron	
	with dendrites that are twice as thick, and the data from (Ostroumov,	
	2007) for comparison. Columns A_S , A_A , and A_D are the surface area	
	of the soma, axon, and all the dendrites respectively	61
4.1	Volume conductor simulation parameters. ς is the width parame-	
	ter used in the monophasic (Eq. (2.13)) and biphasic (Eq. (2.17))	
	stimulation waveforms. f^{max} is the dominate frequency of a single	
	stimulation pulse. This frequency was used to determine the material	
	properties in Tables 2.4 and 2.5. The volume conductor simulation	
	was run from $-t_{mag}$ to t_{mag} in steps with stepsize Δt	86
Monophasic simulations which result in the membrane voltage of 4.2 the axon tip being above $-10 \text{ mV} (V_m > -10 \text{ mV})$ while the stimulation voltage is below an amplitude of 5 V ($|V_{stim}| < 5$ V). The combo column indicates which electrodes are active. (Recall from Section 2.2.1 that electrode combinations use the notation [column letter][row number][p for +1V or n for -1V] repeated for each active electrode.) Nonactive electrodes are floating. A value of -1 in the sign column reverses the sign of the electrodes in the combination. The side, row, and dorsal-ventral columns indicate the location of the neuron. The axon column indicates the direction of the distal tip of the axon from the soma. In this table, column A16 captures the magnitude of the stimulation voltage necessary to cause the membrane voltage at the axon tip (segment 16) to exceed -10 mV. Column S-A16 tabulates the additional amount of stimulation necessary to cause the soma membrane voltage to exceed $-10 \,\mathrm{mV}$. Columns D8-A16 and D16-A16 are the additional amount of stimulation (beyond that in column A16) necessary to cause the membrane voltage of the middle (seg=8) and distal tip (seg=16) of the distal dendrite

- 4.3 Biphasic simulations which result in the membrane voltage of the axon tip being above $-10 \text{ mV} (V_m > -10 \text{ mV})$ while the stimulation voltage is below an amplitude of 5 V ($|V_{stim}| < 5$ V). The combo column indicates which electrodes are active. (Recall from Section 2.2.1 that electrode combinations use the notation [column letter][row number][p for +1V or n for -1V] repeated for each active electrode.) Nonactive electrodes are floating. A value of -1 in the sign column reverses the sign of the electrodes in the combination. The side, row, and dorsal-ventral columns indicate the location of the neuron. The axon column indicates the direction of the distal tip of the axon from the soma. In this table, column A16 captures the magnitude of the stimulation voltage necessary to cause the membrane voltage at the axon tip (segment 16) to exceed -10 mV. Column S-A16 tabulates the additional amount of stimulation necessary to cause the soma membrane voltage to exceed -10 mV. Columns D8-A16 and D16-A16 are the additional amount of stimulation (beyond that in column A16) necessary to cause the membrane voltage in the middle (seg=8) or distal tip (seg=16) of one of the distal dendrites respectively to exceed -40 mV. A value of OSR means Outside Search Range (i.e. more than ± 10 V of stimulation is necessary). 106 4.4 Biphasic simulations which result in an orthodromic action potential

- 5.6 Stimulation type: Monophasic, combination: A3pC5n. 245

cxlviii

5.7	Stimulation type:	Monophasic,	combination: -A3pC5n.		246
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cxlix NOMENCLATURE

neurite. Any projection from the neuron cell body; a dendrite or an axon.

sub-threshold. In this thesis sub-threshold indicates that the electrical stimulation or the synaptic input does not cause neurotransmitter release from the neuron(s) simulated.