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Parth Shah
In preparation for the mission to Mars in 2020, NASA JPL and Caltech have been exploring the potential of sending a scout robot to accompany the new rover. One of the leading candidates for this scout robot is a lightweight helicopter that can fly every day for ~1 to 3 minutes. Its findings would be critical in the path planning for the rover because of its ability to see over and round local terrain elements. The inconsistent Mars magnetic field and GPS-denied environment would require the navigation system of such a vehicle to be completely overhauled. In this thesis, we present a novel technique for heading estimation for autonomous vehicles using sun sensing via fisheye camera. The approach results in accurate heading estimates within 2.4° when relying on the camera alone. If the information from the camera is fused with our sensors, the heading estimates are even more accurate. While this does not yet meet the desired error bound, it is a start with the critical flaws in the algorithm already identified in order to improve performance significantly. This lightweight solution however shows promise and does meet the weight constraints for the 1 kg Mars 2020 Helicopter Scout.
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NOMENCLATURE

**CAD.** Computer Assisted Drawing is the use of computer technology, such as SolidWorks, for design and design documentation.

**CV.** Computer Vision involves acquiring, processing, analyzing and understanding digital images to make decisions.

**EKF.** Extended Kalman Filter is the nonlinear version of a Kalman filter.

**HSV.** Hue-Saturation-Value is a common color model used for image encodings.

**IMU.** Inertial Measurement Unit, is an electronic device that measures and reports a body’s specific force and angular rate surrounding the body, using a combination of accelerometers and gyroscopes.

**JPL.** Jet Propulsion Lab is a federally funded research and development center that is managed by Caltech.

**KF.** Kalman Filter is an optimal estimator.

**MER.** Mars Exploration Rovers is an ongoing robotic space mission involving two Mars rovers, Spirit and Opportunity, exploring the planet Mars.

**NAVCAM.** Navigation cameras is a stereo pair of cameras, each with a 45-degree field of view to support ground navigation planning by scientists and engineers.

**Pancams.** Panoramic Cameras is a color, stereo pair of cameras that is mounted on the rover mast and delivers three-dimensional panoramas of the Martian surface.

**PSF.** Point Spread Function describes the response of an imaging system to a point source or point object.

**RGB.** Red-Green-Blue is the most popular color model and is also the most frequently used encoding for digital images.

**ROS.** Robot Operating System provides libraries and tools to help software developers create robot applications.

**WO.** Wheel Odometry is the use of wheel sensors to estimate position and heading.
Chapter 1

INTRODUCTION

1.1 The Mars Helicopter

Mars is the closest neighboring planet to Earth and is located approximately 33.9 million miles away. The planet’s surface, climate, and geography is heavily studied with the hopes of determining if the planet ever had the correct conditions to support microbial life. Recent findings from the Mars Reconnaissance orbiter mission have revealed a water deposit larger than the size of New Mexico on Mars’ Utopia Planitia region (Webster, 2016). The past orbiters and rover exploration missions have been critical in making such discoveries and setting up the groundwork. In order to further this work, NASA hopes to send a lander, Insight, in 2018 as a part of the NASA Discovery Program to study the deep interior of the planet. This will be followed with a rover, Mars 2020, in 2020 as a part of its Mars Exploration Program (Mission: InSight n.d.) (Mars 2020 Mission Overview n.d.).

The rover design for Mars 2020 will be based off of the Mars Science Laboratory mission architecture and will contain many of the successful elements. The rover will have a mass of ~900 kg and will operate for up to one Martian year (687 days) on the surface of Mars. Every single exploration program including Curiosity has performed motion planning and destination selection using a combination of satellite and on-board camera images. The on-board cameras provide a picture of the rover’s immediate surroundings but cannot look past obstacles such as crater walls or large rocks. This is due to the design limitations of where the cameras can be placed and their reduced field of views, ~16-45°, to produce higher quality images. As the mapping of Mars has increased, satellite image qualities have significantly improved but they still remain a limiting factor when planning the target for a rover. To combat this, a small helicopter, Mars 2020 Helicopter Scout, may accompany the rover as a part of the scientific payload. The proposed helicopter is depicted below in Figure 1.1.
1.2 Mission Requirements

The primary objective of this helicopter is to explore the terrain ahead of the rover. It will be able to provide overhead images with ~10x greater resolution than orbital images and will display features that may be occluded from the on-board cameras (Volpe, 2014). The current proposals call for a lightweight helicopter, ~1 kg, in order to generate the required thrust in Mars’ thin atmosphere. With a total mass of 1 kg, it would fly once every Martian day for approximately 3 minutes and cover up to 600 meters (Volpe, 2014).

Communication is another critical process for this helicopter. A radio signal can take up to 45 minutes to make the roundtrip between Mars and Earth. As a result, the Mars helicopter, with its 3-minute flight, will need to be almost completely autonomous. A human operator may be able to once a day sketch out the approximate patch of land that it wants the helicopter to survey, but the operator cannot reasonably administer finer commands then that. Therefore, the helicopter needs to be able to sense the environment sufficiently so it can autonomously navigate to the desired destinations and back to the home location.

For the safety of the rover, the helicopter will be deployed only after the rover has
left the drop off site. The communication systems onboard the rover will update the helicopter of the rover’s position so the helicopter explores the correct regions while always remaining a safe distance away from the rover. It would be a tragic failure for NASA if its exploration vehicles could not communicate with one another, so it is critical that the helicopter stays close enough to the rover so that it can relay its findings. Because of its limited flight times, the helicopter will have to convey the results once it has landed. This information can be sent in one of two ways back to the rover. If the rover is within close proximity, line of sight, the information can be sent directly to the rover. Otherwise, information will have to be conveyed via the network of satellites that orbit Mars. Unfortunately, this network is nowhere as robust as the one for Earth, and can result in communication delays of up to 45 minutes. It would be impractical to waste the helicopter’s power on hovering at an altitude above all local obstacles just to convey data directly to the rover from a slightly further location.

To ensure the helicopter is far enough from the rover to fly safely and close enough to the rover to communicate, the helicopter will rely on being able to accurately know and report its location. The process in which a system estimates its own state using system inputs and outputs is known as state estimation. In the case of planetary exploration this procedure draws upon data from the inertial measurement unit (IMU) for state prediction and additional sensors for state verification. The sensors used for state verification must draw upon external variables outside of the system. For the helicopter, this will mean magnetic fields, beacons, stars, or any other phenomena that occurs in a constant pattern.

1.3 Space Environment

Although there are many difficulties in designing an autonomous robot on Earth, this specific helicopter must also endure the harsh environment of Mars. There is a vast amount of research done on characterization of the Martian environment. The details will not be discussed in this paper but the key components will be highlighted and addressed as they pertain to the heading estimation task.

On Earth, multirotor systems utilize a compass for heading estimation. However, extraterrestrial environments like Mars often have weak or inconsistent magnetic fields rendering compasses useless. Instead, planetary exploration missions have capitalized on the presence of stars for navigation purposes (Eisenman, Liebe, and Perez, 2002). Because of the thin atmosphere and weak magnetic field on Mars, the
Sun becomes a critical feature for localization on Mars. As displayed in Figure 1.2, a strong global magnetic field does not exist on Mars and the scattered local magnetic fields are about a 100 times weaker than the magnetic field of Earth (Acuña et al., 2001).

Figure 1.2: Isomagnetic contours of Mars drawn at 10, 20, 50, 100, 200 nT from ~400 km to demonstrate the weak and varying magnetic field (Connerney et al., 2001). A compass could only be used for state estimation if the image had little to no color variation. The inconsistency of the magnetic field renders the compass useless for state estimation on Mars.

The atmosphere on Mars is a 100 times thinner than that on Earth and is composed of mainly carbon dioxide. The gravity on Mars is approximately \( \frac{1}{3} \) of that on Earth. The thin atmosphere overshadows the benefits of reduced gravity and results in exponential growth of propeller length in order to generate the required thrust. The abundance of carbon dioxide dampens the greenhouse gas effects, as a result, severe weather patterns such as clouds are much less pronounced, thus increasing the likelihood of locating key features such as stars. Dust storms, on the other hand, are frequent and assumed to be the common natural occurrence that could hamper the visibility of the Sun and stars, and damage some of the equipment onboard.

To successfully design a helicopter that can autonomously navigate on Mars, it is imperative that the correct facets of the environment are capitalized upon. Different planetary exploration missions in the past have implemented the required state estimation techniques using a variety of approaches.
1.4 Roadmap

The thesis is divided into 3 main parts. The first three chapters set the scene for the thesis and delineate the goals. Chapters four and five describe the methods and necessary environment in detail. Finally, chapters six and seven present the results and discuss the impacts of the findings before recapping the accomplishments and suggesting future work for autonomous navigation on Mars using a fisheye camera in chapter eight.
Chapter 2

BACKGROUND

2.1 Navigation Requirements

Navigation is the act in which a vehicle determines its location with respect to a reference using its sensors. It is a critical component of autonomous vehicles because it is used to guide them to their targets or goals. In the case of the Mars helicopter, the target is a region specified by a human operator. Arriving at this location and exploring it is much more important than what paths or waypoints are traveled on the way there.

As state earlier, the goal of the Mars helicopter is to scout out operator suggested areas around the rover with short, daily flights. The helicopter should return home to a position that is far enough away from the rover to maintain the safety buffer zone. The position accuracy for similar missions in the past has been 10% (Eisenman, Liebe, and Perez, 2002). To reasonably bound the helicopters state estimation error within a range it can still communicate through line of sight, ~30 m, the position accuracy must be 5% or better. The helicopter must be able to accept commands from the human operator via the rover, autonomously navigate and survey the desired area, and communicate its findings back to Earth via the rover’s communication equipment.

It should be noted that all autonomous navigation will be done during the day, when there is enough light for sensing and reacting. The rover will also play no role in the navigation process forcing the helicopter to rely exclusively on its onboard sensors.

2.2 Navigation Methods

There are two main categories of navigation: by reference and by dead reckoning. Navigation by reference requires for there to exist external objects in the environment whose location is either fixed or known at a given time. If a network of beacons were set up within a mile radius of the rover, and their positions were communicated to the helicopter, then it would be able to navigate through this surrounding region. This is of course assuming that the required beacons are in line of sight of the helicopter. Dead reckoning, a method that only draws upon internal variables, on the other hand is a self-sufficient process but is subject to unbounded error growth. Unfortunately,
the high quality instruments necessary to keep the error low will not fit the weight constraint of the helicopter, 1 kg. Therefore, the low quality, lightweight versions of the instruments must be cleverly combined to meet the real-time position estimation requirements of the helicopter while attempting to keep it within its predefined bounds using reference based navigation.

As discussed above, one of the sensors will need to reference a heading. On Mars, the magnetic field is weak and uneven. However, the atmosphere and weather provide easy access to the Sun and other stars. The helicopter will be flying during the daytime. As a result, the logical reference to use in the sky will be the Sun. Historically, sun sensors have provided accuracies as high as 0.001 degrees for active implementation (Psiaki, 1999). It will be critical to draw from these past inspirations for the case of the helicopter.

2.3 Past Solutions

In the past, the Sun has been used to guide a plethora of space missions, including satellites and the descent stages of rovers. Sun sensors of different sorts are used to calculate the attitude of the satellite or spacecraft. For example, the Mars Exploration Rover (MER) used a visual odometry system that combined the estimates from integrating the IMU and the encoders on the wheels with the information extracted from the NAVCAM images (Eisenman, Liebe, and Perez, 2002). The position estimate can accumulate a couple degrees of drift from repeatedly integrating the IMU data. To eliminate this error, the direction of the gravity vector measured by the IMU is combined with a vector pointed at the sun and the knowledge of the current local solar time (Maimone, Leger, and Biesiadecki, 2007). The Panoramic Cameras (Pancams) are located 1.5 meters high on the mast of the rover and are used to calculate the sun vector. The Pancams have a 16° by 16° field of view (FOV) and are mounted with a 1° shoe on a 2 axis gimbal at the top of the mast. The Pancams are positioned with respect to the sun vector such that the sun appears in the center for the image. The error is then determined by identifying the location of the sun in the image and from this the updated sun vector is calculated (Eisenman, Liebe, and Perez, 2002).

Other solutions include a star tracker, an optical device that measures the position of stars, or a network of photodiodes. The photodiodes are a low cost solution for satellites that can determine the sun vector for navigation purposes (Springmann, 2013). The MER descent stage combined a sun sensor with a star tracker to estimate
the attitude of the plummeting rover. These methods however will be impossible to implement on the Mars helicopter; the MER Pancams or a star tracker weigh on the order of a couple kilograms and will not fit in the weight budget of the 1 kg helicopter. As for the network of photodiodes, they may not work as effectively because the sun will only be illuminating the top surface of the helicopter and therefore the network of photodiodes would only be able to discern two of the three dimensions of the sun vector.

An alternative that draws from the past implementation on MER is a camera. This camera would not serve multiple additional functionalities like the Pancams does and would ideally have a much larger field of view than the Pancams because relying on a gimbal on top of a helicopter would be relatively heavy. Fisheye cameras are a lightweight option with wide fields of view. The four most common types of fisheye cameras are stereographic, equidistant, equisolid, and orthographic. The unique mapping functions and benefits for these different fisheye cameras are displayed in Table 1. An equidistant fisheye camera maintains angular distances making it the ideal candidate for measuring angular differences in the Sun’s position. The camera normally weighs on the order of 100 grams and boasts a 180° field of view.

<table>
<thead>
<tr>
<th>Stereographic</th>
<th>Equidistant</th>
<th>Equisolid</th>
<th>Orthographic</th>
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<td>Mapping Function</td>
<td>$R = 2 f \tan \left( \frac{\theta}{2} \right)$</td>
<td>$R = f \theta$</td>
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Table 2.1: The mapping functions and strengths of the four most common fisheye camera types (Schneider, Schwalbe, and Maas, 2009)

Combining the lightweight fisheye camera with other lightweight dead reckoning sensors will be key for developing the desired state estimation platform for the helicopter.
Chapter 3

OBJECTIVES

The goals for this senior thesis are as follows:

1. Easy -
   - Track the Sun using a fisheye camera and output heading estimates while being stationary
   - Model a Kalman filter for providing heading estimates by fusing a variety of data sources

2. Intermediate -
   - Explore advanced image processing techniques to improve heading estimates
   - Track the Sun using a fisheye camera and implement the Kalman filter to provide heading estimates while onboard a planar vehicle (TurtleBot)

3. Advanced -
   - Integrate the Sun tracking fisheye camera with JPL’s visual inertial navigation filter
   - Create a comprehensive error budget

To achieve goals a couple key tasks are required to lay the proper foundation. First, a comprehensive literature review must be completed to understand how similar problems have been successfully solved. This review will require reading journal articles and space agency documents in order to understand the true complexity of the problem. Then begins the project specific research. Journal articles and textbooks will be critical for differentiating the types of fisheye lenses. Based on the pros and cons of each type and the availability, a fisheye lens will need to be purchased.

Next, the environment to connect all the sensors and perform all the computation must be properly setup. In this case it will require properly installing the complete
Indigo release of Willow Garage’s robotic operating system (ROS) on the compatible Ubuntu release. Then ROS needs to be connected to OpenCV, a C++ computer vision library that is also now available in Python, Matlab, and Java, for image processing. The specific fisheye camera then needs to be appropriately mounted so it is compatible with the aforementioned operating systems. Once this has been completed, the fisheye camera can capture an image while running through ROS and then can be processed in OpenCV. There exist a handful of tutorials online to familiarize oneself with these open source technologies.

The final task of preparation that needs to be done is the solar ephemeris approximations. Using the solar ephemeris it is possible to calculate the approximate position of the sun in the sky based on one’s latitude and longitude and absolute time. These equations can be identified very easily for earth and have been converted into cosines and sines for simplicity. The other calculation that needs to be performed is the size of the sun in an image. The Sun is known to be a certain angular measurement in the sky. As a result, this value can be translated in a square of pixels. This square will be used to sweep the image when searching for the sun. The size of this square is dependent on the resolution of the fisheye camera used. It will also be dependent on the approximate position of the Sun in the fisheye camera because fisheye cameras distort objects in certain manners for different parts of images.

Three additional performance optimization topics that may be explored in preparation for the advanced goals include rectilinear reconstruction, point from spread deconvolution, and Kalman filters. One of the most common type of fisheyes is an equidistant fisheye. To reconstruct a rectilinear image from an equidistant fisheye image the image has to be split up into a central region and four peripheral ones before being reconstructed using geometric transformations [12]. The current approach calls for bypassing this computationally intensive step, but if the errors are too high then some sort of a reconstruction may need to be implemented to meet the desired performance specifications. Another phenomena that is computationally intensive to combat is PFS - point from spread. PFS causes the dilution of pixels. If the error budget reports a large error, then it may be worth investigating if a generic deconvolution can be reasonably applied to enhance the quality of the image. Finally, the sun detection algorithm will output information about its heading versus its expected heading. From this information, the sun vector and the associated heading error can be calculated. To correct this naturally growing error, the information will be fed back into an extended Kalman filter. All three of these
topics will be addressed in following sections. Ideally the working algorithm and sensor are integrated with JPLs visual inertial navigation extended Kalman filter. In general, Extended Kalman Filters are commonplace for autonomous navigation of robots, especially rotorcrafts.
The first step of this experiment is to conduct a review of fisheye lenses. The main way fisheye lenses vary is the mapping function they implement. The four leading types are stereographic, equidistant, equisolid angle, and orthographic. The characteristics that need to be considered in this review include mass, resolution, reconstruction technique, and related point from spread functions. From the review, the findings appear to favor an equidistant fisheye camera. They are the cheapest, and most commonly available fisheye camera that interface with our desired platforms and meet the weight constraints. The mapping function for these fisheye cameras also tends to be the simplest of them all.

Figure 4.1: An image of a room from a camera with (a) a normal perspective lens and (b) a fisheye lens (Courbon et al., 2007).

Now that the type of fisheye lens has been selected, a camera that fits the desired specifications will be utilized for all future experiments. There are a couple extra tests that can be performed if one would like to further analyze fisheye cameras. The first extra test that can be performed is a simple validation of the selected mapping model. Using a simple object with a bright color and defined edges, a series of images can be captured using the fisheye camera. The location of the object will vary from the center to the edges of the image. The location of the object will also
be measured with respect to the defined center of the image. The radial position will be predicted and compared to the ideal case mapping function that is provided in literature. The second test that can be performed is to fit a fifth order polynomial, the polynomial fish eye transform, to create a secondary model that accounts for manufacturing errors (Hughes et al., 2010). It can be pursued to further understand the radial distortion introduced by the fisheye lens. Both these tests extend the analysis performed on the selected fisheye camera to ensure the user understands any special phenomena or irregularities in the lens or camera.

\[ r_d = \sum_{n=1}^{\infty} k_n r_u^n = k_1 r_u + k_2 r_u^2 + \ldots + k_n r_u^n \]

The high level algorithmic review can now proceed, given that the appropriate hardware has been selected. The algorithm that will be developed for the vehicle will need to first acquire images that are being broadcasted by the camera in our ROS architecture. From there it will have to convert it to the appropriate encoding and data structure so that our analysis library, OpenCV, can use it. From the raw image, we will have to extract the location of the Sun. To do this a couple different techniques can be implemented. One approach to consider might be similar to the MER Pancams – a window that sweeps the image. Another approach might include searching for contours and biasing the size or location of these contours. After a final technique has been implemented for extracting the location of the Sun, it has to be calibrated to the real world location to produce a heading estimate. Once it has been calibrated, the calibration transform can be applied to every new reading to predict the next heading estimate as the vehicle travels.

The algorithm can be made even more robust by combining other fundamental technique of state estimation to improve the heading estimate. When extending the system to planar vehicles, wheel odometry, is the leading candidate. As for aerial vehicles, we look to include visual odometry. This techniques provide extra information that may need to be passed through a filter but should improve the heading estimates when combined with the estimates output from the fisheye camera.

There are a couple other features that might need to be built into the algorithm, if their effects significantly impact the outcomes. The first is the point spread function. To begin the impact of the point spread function would need to be determined. In general the point spread function blurs out a point-like object and spreads it out to a certain minimal size. Its effects are generalized as a convolution of the object and the
estimated point spread function. If the impacts of the point spread function are large, quantified by a pixel blurring kernel, then a deconvolution needs to be performed to the image to restore the original image. Deconvolution however requires a large amounts of computing power and may not be feasible with the onboard electronics. Performing a deconvolution of only the sun may be possible if a simple and generic transform can be calculated off-board beforehand and then stored onboard.

The next feature is rectifying the image. If the algorithm struggles to identify the Sun in the distorted regions of the image then the image will need to be rectified. The theory behind rectilinear transforms call for splitting the image into 5 sections and applying different transforms to each portion to rectify the image. If we end up rectifying the image, we will most likely end up referring to existing library functions or procedures instead of implementing our own. Once rectified, the size of the Sun should not change significantly based on its location in the image and a tighter bound can be given to the search component of the algorithm.

This technique has to then be integrated into the frame of a helicopter. The helicopter does not ensure that the camera’s normal vector is always facing up when taking images. As a result, the tilt of the helicopter must be accounted for. A couple different methods will be explored in this section. First a horizon tracking methodology may be implemented to approximate the tilt of the helicopter at any given time. Another approach integrates a tilt sensor and utilizes its output when calculating the location of the Sun.

Now that that main hardware and software components have been discussed at a high level it is time to turn our attention towards the detailed implementations and results. The next chapter will address the environment and necessary setup procedures before we move into developing and testing the algorithm.
In this chapter, we will be addressing how the environments necessary for this project were setup. This will involve discussing where different packages and drivers were downloaded from and how they were installed properly. Because a majority of the components were only compatible with Linux, it was critical that a distribution of that was installed first.

5.1 Linux
With Linux, there are many distributions that can be installed. Some distributions are commercially backed, such as Ubuntu or Fedora, while others are community-driven, like Debian and Gentoo. The one I had dabbled into in the past was Ubuntu, so I choose to install that. Ubuntu recently released Ubuntu 16.10, Yakety Yak, in October 2016. Instead of downloading the latest release, I decided to install Ubuntu 14.04, Trusty Tahr. The reason I installed Ubuntu 14.04 was because of the ROS release it was associated with. The new release Kinetic Kame is tied to Ubuntu 16.10 and lacks some of the libraries with the appropriate drivers for mounting USB cameras. They rely on the user downloading the desired extra packages from external sources, such as poorly maintained Github repositories, and compiling them in the appropriate directories. In the beginning, this was something I was not very comfortable doing and had a lot of trouble with. I learned that the ROS release of Indigo however interfaced with these older libraries much better. As a result, I wiped the Windows 10 from my ASUS U32U and installed Ubuntu 14.04 with a bootable USB. Figure 5.1 below, shows the operating system up and running with 4 GB RAM, 320 GB SSD, and an AMD E450 processor.
5.2 ROS

As discussed above, the Indigo release of ROS was selected because of the supported packages related to USB cameras. Also a quick Google query illustrated that there was much more thorough documentation related to bugs and common problems for Indigo as opposed to Kinetic Kame. With that in mind, I followed the installation steps outlined on the ROS website (http://wiki.ros.org/indigo/Installation/Ubuntu). I opted for the full desktop install, as this machine was entirely devoted towards running Linux, ROS, and OpenCV for this project. The first additional stack that had to be installed was the camera_umd stack. Inside of this stack were three libraries: camera_umd, jpeg_streamer, and uvc_camera. It was the last library, uvc_camera that I was most interested in because this library had the launch files for USB cameras. While this library made it possible to run the USB camera as a node in the operating system, it did not allow for the user to see the image. To display the image, the aptly named image_view library was utilized. The simplest way of using that library just subscribed to the user identified topic, and streamed the images from the camera to the user in a window. The figure below shows the USB camera successfully running on ROS and being displayed via image_view.
5.3 OpenCV

OpenCV is a library of programming functions that are geared for real-time computer vision. It was originally developed by Intel and is now managed by Itseez. It is an open source software that can be downloaded from Github and easily installed. For this project I tried to download one of the most recent releases, OpenCV 3.1. Unfortunately, after installing it and trying to use it in conjunction with cv_bridge, the program kept segfaulting. After trying to debug this issue with Dr. Kun Li, we finally discovered a StackOverflow question that declared there was still not fix to solve the compatibility issues between OpenCV 3 and cv_bridge. As a result, I had to uninstall this release and download OpenCV 2.4.13 instead. The files were finally installed and the OpenCV environment was built.

5.4 cv_bridge

To connect ROS to OpenCV I used a library built into ROS called cv_bridge. There was an online tutorial on the ROS wiki that demonstrated how to convert an image from the ROS encodings to the OpenCV encodings and then display it after transforming it into a numpy matrix. The figure below illustrates a successful transport to OpenCV in which the image is displayed after drawing a red circle in
the upper left corner.

A simple break down of how cv_bridge works is that it subscribes to a specified topic. It also establishes a publisher that is normally called image_converter. So the packages are received from the topic that is predetermined and then the cv_bridge transports it into OpenCV format. A display of this working is displayed below.

![Figure 5.3: The display window on the left is the output from the image in OpenCV. The display window on the right is the direct stream from the fisheye camera itself. The reason for the discrepancy between the images is the different encodings the image takes on in the two systems.](image)

5.5 External Hardware

In order to get the whole system to work as a single unit in space, the camera had to be successfully mounted on a stand. This stand was designed in SolidWorks and fabricated using the Dimension 3D Printer in the shop. The CAD for the stand is displayed below. The board for the camera already had four pre-drilled holes in the corner. The design capitalized on those holes as mounting points and locked in the camera so that the lens faced directly up. The first iteration includes no way of tilting the camera.
Figure 5.4: A screenshot of the fisheye camera housing that I created in SolidWorks. It will be fabricated using a 3D printer.

The housing was designed so that the pillars in the 3D print would interact with the pre-drilled holes in the chip as a slip fit. After printing the housing, it became clear that the tolerances were not as fine as they appeared to be in the CAD. As a result, the fit transitioned from a slip fit to a press fit and the caps were no longer necessary. The installed version of the first iteration is displayed in Figure 5.5.

Figure 5.5: The fisheye camera successfully installed into the 3D printed housing.

Moving the project onto a quadcopter will be a very different task. Instead of having a display and running the tasks through the host laptop, a small computer, Raspberry Pi or comparable, will have to be loaded with rOS and OpenCV along
with the commands necessary to start the camera as a node and run the programs for finding the Sun.
IMAGE PROCESSING TO FIND AND TRACK THE SUN

6.1 Camera Parameters

Blooming is the phenomena where light streaks out of a light source saturating other pixels. This is often seen in cameras when trying to capture very bright objects such as the sun. With the fisheye camera that is being used, there are few variables that can be manipulated. These different camera properties need to be best manipulated in order to reduce the blooming effect of the Sun. The three variables that can be varied are: white balance temperature, gain, and gamma of the image. Below I present a side by side comparison of how each of these variables effects a LED light source and the Sun.

First we need to present the control. In the figures below the LED light and the Sun is captured with all three variables set to their minimum, which is the default. In the control picture of the Sun, the blooming effect is clearly visible. As for the image of the LED light, it is important to focus on how the areas surrounding the LED light change. It is also important to note the presence of the halo from the glare of the Sun.

![Figure 6.1: The control image of the two light sources with the camera parameters set to their defaults.](image)

Next we increase the white balance temperature to its maximum of 6500 Kelvin. In photography the white balance temperature is used to denote the approximate temperature of the light source. With the Sun as the light source, the white balance...
temperature should be set close to 5800 Kelvin. The images below display the difference produced when the white balance temperature is set to its maximum. The most obvious result is that the camera adds warm tones to the raw image, specifically notice how the walls become yellower.

Figure 6.2: Outdoor and indoor images with the white balance temperature set to its maximum value of 6500 Kelvin. The camera adds warmer tones to the raw image.

The second variable that was increased to its maximum value of 6 was the gain. The gain is used to boost the brightness of an image in low light conditions. However, the gain cannot be used to reduce the brightness of an image, as is required when shooting the Sun. The result of changing the gain from 0 to 6 is not very noticeable as the two environments that we have captured are not poorly lit.

Figure 6.3: Increasing the gain value did not have much of an effect on the image. The gain effect only effects images that are taken in dark environments.

The final variable manipulated was the gamma value. Gamma defines the relationship between the value a pixel carries and the luminescence it outputs. Interestingly,
this value ranges from 72 to 500. Normally this value is set at its minimum of 72. By increasing this value to 500, the image should transform to a much brighter one. This is clearly what is observed in the set of images below. The blooming effect is definitely less noticeable with this change of gamma. However, it is not clear whether increasing the gamma and making the image very bright will be worth the reduction of the blooming effect. As a result, the gamma value will be set to its minimum value of 72 unless stated otherwise.

![Figure 6.4: Increasing the gamma value may have actually reduced the blooming effect but it came at the cost of the entire image becoming a lot brighter, thus making it more difficult to differentiate objects.](image)

The final set of parameters that will be used with the camera include: white balance temperature of 6500 Kelvin, gain of 0, and a gamma of 72. The image format will be JPEG. The size of the image will be determined later when optimizing the performance of the function against some error bound.

### 6.2 Encoding

The next experiment that will have to be performed before beginning the image analysis is the encoding for the image in OpenCV. There are many different formats the image can be reformatted to in OpenCV. It originally is transported to OpenCV in RGB8. This is displayed below.
Figure 6.5: The original image published by the camera node. It is transported to OpenCV and its encoding at that point is RGB8.

It is clear that there exist a plethora of different encodings for images that are compatible with OpenCV. Just to name a few, some of the possible encodings include: GRAY (black and white), HSV (hue, saturation, and value), YUV (luma and chrominance), and Bayer (half the pixels are filtered green). Initially it was thought that transforming the RGB image to GRAY, as displayed below, would be the dominant strategy because then it would be easy to isolate the white objects, the sun, in the image.

Figure 6.6: Using the cvtColor function the image is transformed to the GRAY colorspace.
However, after seeking advice from users familiar with image encodings another encoding emerged as a possibility, HSV. HSV appeared to be another candidate because it separated the image into three different matrices: hue, saturation, and value. The object that we are concerned with is going to normally be the brightest object in the image. For this reason, this value matrix is important because it quantifies the magnitude of the brightness of that specific pixel in the image. The hue matrix is displayed below in Figure 6.7. In reality, we will discard the hue and saturation matrices and only focus on the value one.

![Figure 6.7: Again using the cvtColor function in OpenCV the original RGB image is transfored to the HSV space. This figure displays the H (hue) matrix of this colorspace.](image)

### 6.3 Thresholding

Once the value matrix of the image has been attained it needs to be thresholded. This procedure will impose a mask on the value matrix. All values that are below the predefined threshold will be set to 0. The resulting matrix, as displayed in Figure 6.8, only reveals the brightest features. All the scales in the HSV encoding range from 0 to 255. Originally the image was thresholded to accept the entire hue spectrum, the entire saturation spectrum, but only the upper end, values above 225, of the value spectrum.
Figure 6.8: The masked image after it has been successfully thresholded. The white spaces are the only parts of the image that had value score greater than 225. The three objects on the left are lights in the room, and the large object on the right is the sky that is being illuminated by the sun.

Of course the thresholding bounds had to be iterated a few times before finally arriving to the desired limit for the sun. Originally the threshold was tested on LED lights inside of Gates-Thomas and the 225 value was sufficient. Unfortunately, when testing the threshold function outside on a cloudy day, a limit of only 225 picked up a lot of extraneous white objects such as clouds and white walls that reflect the sun light. To reduce the number of extraneous objects that remain after the thresholding the bound was increased to only accept value readings that were between 253 and 255.

6.4 Finding and Tracking

Originally the strategy to find the Sun was to sweep the image with a square approximately the size of the Sun and determine what region had the highest value score. This approach however has a runtime of $O(n^2)$ and there exist more efficient methods to find objects in an image. After thresholding, our matrix is essentially a binary matrix. There exist a set of functions already built into OpenCV that can help us identify the groups of 1’s in the matrix. First we run the function findContours which identifies all the groups of 1’s in the matrix by constructing convex hulls around them. Then we create a circle that can enclose the convex hull using the minEnclosingCircle function. This returns the center and radius of the enclosing circle that has been found. We store these values in two separate arrays to remember
all the different contours we have found.

Now that we have all the different contours we need to identify which one is the sun. Normally the Sun tends to be the largest contour in the image when we have thresholded the image so strictly. For this reason we determine the index of the contour with the largest radius and that is determined to be the Sun. Using the OpenCV circle function, we can overlay a circle on the original image to denote the contour with the Sun. The results of the first attempt to run this script is displayed in Figure 6.9.

![Figure 6.9: The result of the Sun finding script. The contour seems to have included a part of the cloud as well, and as a result the radius of the enclosing circle is larger than desired.](image)

In Figure 6.9, the Sun is clearly partially obstructed by the roof. The threshold also does not appropriately eliminate the entirety of the cloud that is near the Sun. As a result the contour denoting the Sun is larger than it needs to be and includes a part of the cloud. To fix this the threshold bounds need to be adjusted. It might also be necessary to introduce a bias factor that bounds selected contour sizes above and below. As of now we only have below in order to remove contours that appear as a result of random white noise. By bounding the contour size above, we will bias the script to only select contours that are similar to the size of the Sun. Further data needs to be gathered to tune the bounds as to account for the size discrepancies based on the distortion of the image.

Achieving the most rudimentary requirements for tracking is relatively easy. The ROS node for the camera publishes an image once every second. The script we
are running is set to find the Sun on every tenth image. We are also saving the image after the Sun has been identified in a folder on the Desktop. The location of the contour, the center of the circle, is written to a separate text file every time an image is saved. This process blindly meets the requirement for tracking the Sun in sequential images. However there are definitely more intuitive methods that can be implemented to make the process more efficient.

6.5 Gaussian Blurring and Sobel Kernels
The next step is to see if some clever image processing tricks can be applied to get around the bloom phenomena. The first is to see if it was normally distributed. This does not appear to be the case because in consecutive images the phenomena tends to appear in the same place. As a result it is not feasible to gather a large number of images at once and then average the phenomena over the samples collected to remove its impact. The other image processing trick that confirms that it is not normally distributed is Gaussian blurring. This procedure takes a square matrix and sweeps it over the image while reassigning the center pixel the average value of the pixels in the matrix. This will ideally remove any streaky or randomly distributed features in the image. Figure 6.10 illustrates the result of Gaussian blurring. It diminishes some of the isolated bloom regions but also strengthens some of the highly concentrated bloom regions. By strengthening these areas it does not remove the shift in the centroid estimation, which is the root cause of error in heading estimates.

![Figure 6.10](image.png)

Figure 6.10: The image on the left is the original thresholded image. The one on the right is after a Guassian blur of size 3 has been passed over the image. Some of the streakier bloom phenomena are removed by the blurring, but the dense bloom region on the right side of the Sun becomes stronger. Because the phenomena is not normally distributed, a Gaussian blur alone does not help improve the performance of the algorithm.
The other image processing technique that can be implemented is an edge detector, the Sobel kernel. The idea here is that maybe if the edge is better isolated and apparent the contour fit might be tighter. The Sobel kernel takes the gradient in the x and y direction before combining them to output the edge. The result of one pass of the Sobel kernel is displayed in Figure 6.11. Unfortunately, the regions of bloom do not falter and are present after the kernel has passed over. As a result, the contour still finds the same expected fit and the error in the heading estimate persists.

![Figure 6.11: The image shows the result of the edge detector, Sobel kernel. The bumpy outline of the Sun is due to the bloom phenomena. The roughness causes the centroid to be off, thus influencing the heading estimates.](image)

Neither of these techniques seem as if they alone can impact the original finding and tracking algorithm to nullify the presence of the bloom effect.

### 6.6 Erosion and SimpleBlobDetection

After discussing these issues with content experts, the persistence appears to be dependent on the choice of preprocessing and estimation functions. Once the image has been converted into the appropriate encoding and masked, there appear to be some white streaks that occasionally influence the results of the findContour function. A function that is strong in removing these patchy and streaky phenomena is erosion. It takes a kernel similar to the one used in GaussianBlur, but instead turns the center pixel to 0 if all its neighbors are 0 as well. A couple iterations of this function leads to the removal of any streaky phenomena present around the Sun or randomly in the image.
The erosion function also helps remove the bloom effect, ever so slightly. Given an ellipse, the erosion function will chip away at some of the awkward perimeter pixels equally. But with the bloom effect present, because it increases the perimeter in that region, it results in a slightly higher expected erosion in that region in comparison to the rest of the perimeter of the Sun.

Once this modification has been applied to the image, only a circular or slightly elliptical object should be left in the image. The findContour function would identify this contour and then return the minimum bounding circle for the contour. While this is a reasonable approach, even the slightest remains of the bloom effect could cause significant changes in the heading estimate. The simpleBlobDetect function however finds a blob and then returns a circle that best fits inside the blob. The difference between the two functions is displayed in Figure 6.12 and in turn will hopefully reduce the effects of the bloom effect.

![Figure 6.12: The blue circle indicates "the Sun" as found by the findContour function. The red circle is the improvement after implementing a series of preprocessing functions along with simpleBlobDetect.](image)

### 6.7 No Rectification or PSF

Calibrating the camera is important because it allows us to remove any distortions and rectify the original image. This process can make it easier to determine where the Sun actually is in order to calculate the error of the state estimation system. ROS has a built in node, camera_calibration, that already has the necessary files to create the appropriate calibration file. It requires the user to first print out a standard pattern and input the pattern type and its dimensions before running the camera calibration.
The .yaml file that will be created will contain the camera matrix, distortion vector, and rectification and projection matrices. These matrices play a critical role in rectifying the image before running the scripts to find and track the Sun.

In our case however, we do not appear to need to rectify the image. The simple-BlobDetect should be able to outperform the traditional sweep we had originally discussed. If the sweep of a constant size window was implemented, then the rectification will be crucial. As a result, the matrices for the rectification for the fisheye camera have been stored, but will not be used unless the algorithm reverts back to sweeping a constant size window across the image in search for the Sun.

The PSF also does not play a large role in this image processing portion because we have already determined that the bloom effect is not normally distributed. As a result, if we are to apply the deconvolution to remove the PSF, the Wiener filter, it will not isolate and remove the bloom effect. As a result we disregard this phenomena for now and focus on minimizing the impact of the bloom effect.

6.8 Further Improvements

A simple improvement that can be made to the tracking algorithm involves storing the center location of the Sun in the prior image. This would require modifying the desired data structure, to take the form of a modified linked list. The script can then be changed to focus on blobs that are located near the prior center. This is all under the assumption that there are no rapid maneuver performed with the robot. This is reasonable because its path should be relatively predictable and this restriction can be imposed on the planning algorithm. The only time there could be a quick change in pose could be when the robot decides to make an aggressive maneuver and return back to its home location. At this time the robot or helicopter will rotate quickly to find the shortest path back to the home location while avoiding the rover.
Chapter 7

ESTIMATING HEADING

7.1 True Position

To acquire the true position data of the Sun we had to find an online calculator published by a reputable source. The National Renewable Energy Laboratory has two such calculators. Their first one is called SOLPOS and has valid data between 1950 to 2050 within a hundredth of a degree. Their other calculator has valid data between -2000 and 6000 within a couple hundred thousandth of a degree. The SOLPOS calculator exported the desired data between a certain time period as a zip file very conveniently, so that is the one we used.

The user had to input the latitude, longitude, and time zone of their location along with the desired output values. During this first iteration only the azimuth and zenith angles of the Sun were output assuming the user was in Pasadena, California. We asked the calculator to output data for ideal dates of the mission. The mission is scheduled for 2020 and these types of missions normally have a lifespan of under a couple years. Just to be conservative we asked the calculator for a six year time period between 1/1/2020 and 1/1/2026. Unfortunately, the calculator only outputs less than a million data points in one go. So the frequency of the data had to be decreased to once every ten minutes. The text file containing the data for this six year period had a size of 3.43 megabytes.

The data however included the position of the sun before sunrise and after sunset. A script can be written to remove all these useless readings to shrink the size of the file. Further investigation also needs to be done on whether the trajectory of the sun is constant and can be extrapolated from two data points. Because our flights will normally be less than ten minutes, we will have to rely on just two data points or increase the frequency of the data we have stored from the SOLPOS calculator. Ideally, we can just take the two nearest data points and extrapolate based on the time on the clock to get where the Sun is. This would definitely save us some memory that the file would otherwise take up.
7.2 Fixed Position, Heading Estimate Test

A couple different iterations of experiments were performed to test this algorithm. The first one focused on reducing all potential moving parts and determining the performance and accuracy of the algorithm. In this experiment the camera was placed on a table on the roof of Gates Thomas and the algorithm output the azimuth and zenith angles of the Sun. We did not have to worry about any motion of what the camera was mounted to because in this experiment it was fixed to a table on the roof.

Please note that from here on forward both the zenith and azimuth estimates will be provided. When estimating the heading, we will only need the azimuth reading. Both are provided as to further understand the impact between the variables altered.

There are a couple of parameters that should be noted before we dive into the results of this experiment. The resolution of the images passed from the camera to the algorithm was 640 by 480. The experiment was started at 10:30 am and ran till 6:30 pm. The table was placed on the gravel that was on the roof of Gates Thomas. This resulted in the surface of the table being slightly tilted. Using a cheap level, the table was tilted by approximately 1°. The first ten azimuth readings were also averaged and compared against the first ten expected azimuth readings. The difference between these values ended up being the rotation matrix applied to the rest of the data. The algorithm that was implemented was also limited to the advancements made while the findContour function was still in the code. The simpleBlobDetect function had yet to be implemented.

The azimuth and zenith approximations were off by an average of 2.4° and 5.6° respectively. Unfortunately, these results result in error bounds that are larger than what we targeted. Looking back on intermediate images saved along the way it is clear why the error is so large. Figure 7.1 shows the algorithm working as expected. It finds the Sun in the image and only encloses the Sun while discarding parts of the blooming effect that surround the Sun. Figure 7.2 however shows the opposite. Here the algorithm drastically failed at excluding the bloom phenomena from the Sun. As a result, the zenith approximation was off by 7°. The graphs off the approximations versus real angles are provided in Figure 7.3.
Figure 7.1: The algorithm successfully identifies the Sun while excluding any of the surrounding bloom phenomena. The resulting estimates are within 2° and 3° respectively.

Figure 7.2: Here the algorithm struggles to differentiate the Sun from the neighboring bloom phenomena. As a result the estimates are off by 5° and 8° respectively.
7.3 Second Iteration

In the next iteration of the experiment, the resolution of the images was changed from 640 by 480 to 2048 by 1560. The thresholding was also changed from 253 to 255 in an effort to reduce the impact of the bloom effect. As depicted in Figure 7.4, this resulted in the two approximations being off by an average of 3.6° and 6.6° degrees in the azimuth and zenith values, respectively. This was worse than the heading estimates produced when the image resolution was 640 by 480. Increasing the threshold from 253 to 255 did not reduce the bloom effect. Those neighboring pixels that are being saturated, tend to saturate to their maximum values, thus making it difficult to distinguish them from the actual light source. The increased image resolution allows for the bloom effect to be portrayed with a higher resolution. This clarity of this phenomena biases the centroid more consistently, causing the estimates to worsen with the change that was implemented. It is important to note that the algorithm still used findContour instead of simpleBlobDetect in this iteration. The next approach will definitely call for lower resolution images.
Figure 7.4: The two graphs showing the angle approximations against the true values for the second iteration with higher resolution images and increased threshold values. Both the zenith and azimuth approximations worsened with these changes.

### 7.4 Third Iteration

In the third iteration of the fixed position, heading estimate test the image size was reduced to 1024 by 768. The algorithm was also overhauled to include new preprocessing steps such as erosion and gaussianBlur. The findContour function was scrapped and was replaced with the simpleBlobDetect function. This experiment was only two hours long but produced an error of 3.5° for the azimuth approximation. This was definitely a step in the right direction. With a little bit more preprocessing, it clear that the error can be brought down drastically using a script centered around the simpleBlobDetect function.

Figure 7.5: The azimuth approximations with a new overhauled algorithm over the course of a two hours period produced a heading estimate error of 3.5°.
Optimizing preprocessing techniques and fusing the sensor output with other sources will improve the heading estimation accuracy.

7.5 Kalman Filter Model

In this section we will define the Kalman filter necessary to fuse the different heading estimates into one.

The linear state space that describes the heading and angular velocity:

$$\theta_k = \begin{bmatrix} \theta \\ \dot{\theta} \end{bmatrix}$$

From dynamics we can conclude that:

$$\theta_k = F \theta_{k-1}$$

where:

$$F = \begin{bmatrix} 1 & \Delta t \\ 0 & 1 \end{bmatrix}$$

$$G = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

so that:

$$\theta_k = F \theta_{k-1} + w_k$$

where:

$$w_k \approx N(0, Q)$$

$$Q = GG^T \sigma_a^2 = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \sigma_a^2$$

Suppose the measurement noise, $v_k$ is also normally distributed with mean 0 and std dev $\sigma_z$

$$z_k = H \theta_k' + v_k$$

where:

$$H = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
We know the initial starting state of the TurtleBot with perfect precision so we initialize it to:

\[
\hat{\theta}_{0|0} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}
\]
\[
P_{0|0} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}
\]

Now that we have identified all of the elements, we must show how they are used.

First you must predict. We will show the two predictions, predict state estimate and predict estimate covariance, respectively:

\[
\hat{\theta}_{k|k-1} = F_k \hat{\theta}_{k-1|k-1} + B_k u_k \\
P_{k|k-1} = F_k P_{k-1|k-1} F_k^T + Q_k
\]

Please note that we have no \(Bu\) term because we have no known control inputs. Instead we have a second source \(\theta'\) and \(G\) applies it to the state vector.

The update steps then follow. First you find the innovation:

\[
\tilde{y}_k = z_k - H_k \hat{\theta}_{k|k-1}
\]

Then calculate the innovation covariance:

\[
s_k = H_k P_{k|k-1} H_k^T + R_k
\]

Now the optimal Kalman gain:

\[
K_k = P_{k|k-1} H_k^T s_k^{-1}
\]

Finally update the state estimate and estimate covariance, respectively:

\[
\hat{\theta}_{k|k} = \hat{\theta}_{k|k-1} + K_k \tilde{y}_k \\
P_{k|k} = (I - K_k H_k) P_{k|k-1}
\]

Thus we have successfully derived the Kalman filter necessary to fuse different sensors inputs for a singular heading estimate.
7.6 TurtleBot Experiment

In this experiment we used a TurtleBot. By using the ROS package turtlebotbringup it was easy to command the robot to follow certain predefined commands in a python script. The camera was mounted using the ROS package uvc_camera. The script that was transferring the images to OpenCV and performing the analysis was a ROS package I have written myself, learning_cv_bridge.

First the robot would be launched using the minimal.launch file. This would get the TurtleBot live and ready. Then the fisheye camera would be mounted and the image processing script would be started. This would immediately start saving a stream of images. Then rosbag was used to record /mobile_base/sensors/imu_data_raw as well as /mobile_base/sensors/core. This would bag all the IMU and wheel encoder readings necessary for the experiment. Finally a python script, square.py was used to trace out a square with the TurtleBot. One the script terminated, all the other nodes were terminated in reverse order. The data from the rosbag was finally piped into a CSV file so it could be analyzed. The heading estimates from the fisheye camera were also outputted to a separate CSV file.

This experiment was performed on the cobblestone path beside Milikan Pond. The final heading once the robot at the end of its script was +25°, which is 0.4363 radians (or 6.7195 radians).

Figure 7.6: TurtleBot start location.
Before we dive into the results of the Kalman filter, let's first see what results inertial navigation, wheel odometry, and fisheye camera along output. Figure 2 below displays the heading estimates as a result of all the techniques individually. The inertial navigation outputs that the final heading estimate is 6.4904 radians. Wheel odometry on the other hand outputs 8.6727 radians. The fisheye camera reports a final heading estimate of 6.6450 radians. We will address the potential sources of error below.
Unlike the other two data sources, IMU and odometry, that provided over 5000 data points, the camera was only able to process and provide 37 data points. The fisheye camera was used to provide a second input for the angular velocity of the robot. With such few readings, the angular velocity had to be average in chunks over rather large time intervals. The Kalman filter with all 3 sensor inputs fused together output a final estimate of 6.7101 radians.

The results reveal that the Kalman filter heading estimate was the best. Fusing the information from all 3 sensors does provide a benefit and is very useful in estimating the heading angle.
7.7 High-level Error Budget

This section will address the variables currently in the system that maybe impacting the shortfall in results. Each error will be briefly described and will be followed by bullet points that suggests either future work or potential solutions.

1. Fisheye camera housing - The housing of the fisheye camera is made of 3D printed material and the camera does not sit flush on the top
   - Machine the housing out of some aluminum
   - Replace the press fit with a slip fit and locking mechanism

2. Improve Kalman filter experiment
   - Find flat surface as to reduce wheel slippage
   - Have a more robust ground truth system to compare against

3. Level - ensure experiment surface is level to a higher fidelity than just then unit place
   - Find a new roof or place to gather data
   - Use a digital level with higher accuracy

4. Location - only the approximate coordinates of Pasadena were provided
   - Use the exact coordinates of where the experiment is being performed

5. Atmospheric effects - refraction of the rays as they pass through the atmosphere
   - Better understand the physics of how the rays from the Sun bend or warp as they travel through the atmosphere and reach the location of the experiment. Also explore other environmental features that may impact readings
We have successfully demonstrated that it is possible to estimate heading using only a fisheye camera. We began by first estimating heading on a fixed vehicle. This experiment was designed to see how much the heading estimate would vary over the course of 4 hours for a fixed object. It also evaluated the impacts of external environmental factors that were not considered the first time around. In the first iteration of this experiment, using 640 by 480 pixel images, the heading estimates were within 2.4° and 5.4° for azimuth and zenith, respectively. The second iteration of this experiment utilized image sizes of 2048 by 1560 pixels. This resulted in the heading estimates regressing to 3.6° and 6.6° respectively. The final iteration of this experiment implemented a new algorithmic approach with images of size 1024 by 768 and resulted in what appeared to be much better identification of the Sun. The minimum enclosing circle was replaced by a maximum inscribing circle. This led to a slight improvement in the heading estimate to 3.5°. Further refinement of preprocessing techniques show solid potential for reducing this error even more now that we are working with maximum inscribing circles.

We extended this proof of concept and tried to implement it on a relatively planar, ground vehicle. The TurtleBot traced out a predetermined path, but no information of this path was included in the heading estimate. The data from the fisheye camera was fused with that of an IMU and wheel encoders through a Kalman filter. The output resulted in a more accurate heading estimate than each of those sensors performed individually. This experiment needs to be repeated and improved by varying path, improving testing surface, and integrating a more robust ground truthing technique. Algorithmic improvements will also lend to the production of more data points from the fisheye camera, increasing its presence and impact in the filter. Once this had achieved heading estimates under the desired threshold, the experiment can be lifted from planar robots to aerial robots.

In practice though, this technique is most useful for aerial vehicles because of their weight constraints. The Kalman filter that we have presented hear would be augmented to include the other sensors onboard the aerial vehicle. For example, some of these new inputs might include gyros, visual odometry, and tilt sensors. To
move the sun sensor onboard the aerial vehicle, its scripts and necessary software platforms would have to be loaded onto a smaller, onboard computer. This would allow for successful heading estimates from the sun sensor onboard an aerial vehicle.

Some of the next steps to further this project include increased collaboration with JPL. They have developed a visual inertial for aerial vehicles. Tuning it for extraterrestrial missions would require removing compass and GPS components and replacing it with our fisheye camera and its heading estimate functions. The assumed working code will require some minor tweaks including redefining some frame transforms for where the camera is mounted with respect to the vehicle.

The code also could use some major overhauls to optimize its performance. As of right now, both the fisheye and rectilinear image are stored throughout the entire estimation process. A decision should be made as to which schema will be used for the aerial vehicles, and this will ideally free up a large chunk of memory. The encodings can also be optimized. When transitioning to HSV from RGB, we only end up using the value channel. The final code change that comes to mind is a modification to the data structure. The hemispherical data structure can be extended into a linked hemispherical architectures so that it remembers the previous location of the Sun. This algorithm will be running often during the flight, so it would be a definite advantage to have a clue as to where to begin searching.

Once the code has been optimized and integrated into JPL’s extensive aerial vehicle navigation architecture it needs to undergo testing. There are two major testing components that come to mind. The first is the hostile environment testing for the physical sensor. It needs to be able to function in the cold temperature, endure the radiation present, and to withstand the rubbish kicked up by sandstorms. The second major test involves simulating the Mars atmosphere and sky. Unlike Earth where the sky is normally blue, the sky on Mars is a shade of orange. This might make it slightly more difficult to find the Sun because of the warmer color sky and the generally dustier environment. Also, because Mars is about 1.5 AU away from the Sun, the Sun will appear smaller on Mars then Earth. Once the fisheye camera and algorithm have passed all these test, it will start to be ready for integration on the Mars 2020 mission prototypes.


