ICP ETCHING OF SILICON
FOR MICRO AND NANOSCALE DEVICES

Thesis by
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In Partial Fulfillment of the Requirements for the degree of
Doctor of Philosophy

CALIFORNIA INSTITUTE OF TECHNOLOGY
Pasadena, California
2010
Defended May 19, 2010
I would like to dedicate this thesis to multiple people:

Most importantly I dedicate this work to my wife Shaleigh.

I also dedicate this work to the scientists and engineers who have invested much of their time to mentor, teach, and inspire me: Stuart Shacter, Brian Anderson, Axel Scherer, and especially Mike Henry – my Father.

Finally, I dedicate this work to my sisters Lara, Gina, and Ann.
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ACKNOWLEDGEMENTS

I would like to first, gratefully acknowledge the Fannie and John Hertz Foundation for their generous support for 5 of my years performing research at the California Institute of Technology. Both the financial support and mentoring received from the Foundation has been nothing less than spectacular. For this I offer my sincerest gratitude. I would also like to thank the Robert J. Lang scholarship for a summer of research support.

Scherer Nanofab Research Group: Working for Dr. Axel Scherer and his group has been one of the highest privileges I have had at Caltech. I have enjoyed learning from him vacuum technologies, hearing about all the etching stories, and generally learning from him how to be a balanced and ethical researcher. Kate Finigan has been not only a fantastic admin, but also a friend. I am indebted to her willingness to help me through these challenging years. I have closely worked with Andrew Homyk, whom I must say has greatly impressed me with his knowledge and abilities, and would like to thank him for all of his help and friendship. Mike Shearn has been one of my closest friends, colleagues, and my technical diving partner; I have greatly enjoyed working with him and sincerely hope to continue doing so. I would like to thank Sameer Walavalkar for his collaborating and friendship over the years. I have always learned from others, including those that were once my students and are now my peers; thank you Tom Gwinn, Aditya Rajagopal and Dvin Adalian. I would like to offer my best wishes to them on their future endeavors. I would also like to extend my gratitude to JQ Huang for her tireless efforts helping me and correcting my errors.

Professors and Mentors: There are those whom give their most precious commodity, time, to better others. It is a selfless act which I hope to pay forward. Every now and then
they receive a small reward for their efforts; however small this is I hope they receive this acknowledgment and thanks as such. My most sincerely thanks goes to Tom Tombrello for always entertaining and encouraging my ideas and directing me forward. I extend my thanks to Mike Tyszka for his countless work in teaching me NMR and MRI and guiding my science. Several men at National Semiconductor have spent countless hours teaching me integrated electronics and design; thank you Stuart Shacter, Greg Smith, and Wade Leitner. I would like to thank my undergraduate advisor and my very good friend, Brian Anderson, for introducing physics and quantum mechanics to me. He has spent many hours teaching and helping me. I am at this point in my education, to a large extent, because of you.

Caltech Colleagues and Collaborators: Research is no longer the efforts of a single person; it is now in the realm of the many. I am grateful to this because it has generated many wonderful friendships and collaborations. I would like to extend my gratitude to Julia Greer and Andrew Jennings for their efforts and time to teach and work with me investigating mechanical properties. I hope that our work together continues, mostly because they are very enjoyable people to work with. I would also like to thank all the people of the Kavli Nanoscience Institute for all of their efforts and time spent driving my work forward: Mary Sikora, Guy Derose, Melissa Melendes, and Bophan Chimm. I would like to particularly thank Nils Asplund. He is the most talented machinist I have ever encountered and any time I have needed any work done, he immediately has taken care of it. He has also been a good friend, for that I also thank him.

Friends: Throughout all my successes and failures at Caltech there have always been the friends whom encourage, support and inspire me. They have always given me their very best and I hope that I might give them mine. For those that I have already mentioned
earlier, you are still in this category. My thanks go to: Raviv Perahia, Tom Johnson, Chris Michaels, Ryan Briggs, Carrie and Doug Hoffmann, Anna Beck, Andy Downard, Auna Moser, David Scherer, Chad Weiler, and Uday Khankhoje. I would especially like to thank my very closest friends whom have been my wingmen in my very best and worst times and whom I gratefully think of as my greatest friends: Brandon and Matt Blair, Eric Brown, Matt Eichenfield, and Mike Shearn.

Family: I would like to especially thank those who have stood by me longest. For their love, understanding and help through the many years, thank you: my wife and very best friend - Shaleigh Henry, Mike Henry, Carol Price, Lara Sparks, Gina Henry, Ann Hickox, Shari Henry, Kenny Price, Bill Sparks, Scott Lentine, Brian and Cindy McArdle, Brian McArdle, Bill and Rae Polkinhorn, Bill and Carla Bergschneider, Anita and Harrison Noe, Trina Polkinhorn, Ally Polkinhorn, the Whitlows, and the Yosts.

To these people, I humbly offer my most sincere gratitude.
ABSTRACT

The physical structuring of silicon is one of the cornerstones of modern microelectronics and integrated circuits. Typical structuring of silicon requires generating a plasma to chemically or physically etch silicon. Although many tools have been created to do this, the most finely honed tool is the Inductively Couple Plasma Reactive Ion Etcher. This tool has the ability to finesse structures from silicon unachievable on other machines. Extracting structures such as high aspect ratio silicon nanowires requires more than just this tool, however. It requires etch masks which can adequately protect the silicon without interacting with the etching plasma and highly tuned etch chemistry able to protect the silicon structures during the etching process.

In the work presented here, three highly tuned etches for silicon, and its oxide, will be described here in detail. The etches presented utilize a type of etch chemistry which provides passivation while simultaneously etching, thus permitting silicon structures previously unattainable. To cover the range of applications, one etch is tuned for deep reactive ion etching of high aspect ratio micro-structures in silicon, while another is tuned for high aspect ratio nanoscale structures. The third etch described is tuned for creating structures in silicon dioxide. Following the description of these etches, two etch masks for silicon will be described. The first mask will detail a highly selective etch mask uniquely capable of protecting silicon for both etches described while being compatible with mainstream semiconductor fabrication facilities. This mask is aluminum oxide. The second mask detailed permits for a completely dry lithography on the micro and nanoscale, FIB implanted Ga etch masks. The third chapter will describe the fabrication and in situ electrical testing of silicon nanowires and nanopillars created using the methods previously described. A unique method for contacting these nanowires is also
described which has enabled investigation into the world of nanoelectronics. The fourth and final chapter will detail the design and construction of high magnetic fields and integrated planar microcoils, work which was enabled by the etching detailed here. This research was directed towards creation of a portable NMR machine.
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ICP. Inductively Coupled Plasma

RIE. Reactive Ion Etch

CCP. Capacitively Coupled Plasma

RF. Radio Frequency

IADF. Ion Angular Distribution Function

LN2. Liquid Nitrogen

MFC. Mass Flow Controller

ARDE. Aspect Ratio Dependant Etching

SOI. Silicon on Insulator

SEM. Scanning Electron Microscope

TEM. Transmission Electron Microscope

FIB. Focused Ion Beam

**Pseudo Bosch.** Term describing a SF$_6$ / C$_4$F$_8$ mixed mode silicon etch

PMMA. Polymethylmethacrylate

CVD. Chemical Vapor Deposition

EDX. Energy Dispersive X-Ray Spectroscopy

SCLI. Space Charge Limited Current

SNR. Signal to Noise Ratio

a-Si. Amorphous Silicon
Although ultimately this thesis is in partial fulfillment of the requirements for PhD, this work is also meant for continuity of group knowledge (referred to in the Navy as ‘tribal knowledge’). The layout of this work is setup to ensure that what I have come to understand with etching and fabrication are available for the future generations of the Scherer Nanofabrication Group and users of the Kavli Nanoscience Institute at Caltech. The basis of the knowledge I have gained has come from installing, repairing, calibrating, and using four different Inductively Coupled Plasma Reactive Ion Etchers and a Plasma Enhance Chemical Vapor Deposition tool from Oxford Systems. If others find some use or value from my work, then I am further rewarded.

Chapter I describes, in a general manner, Inductively Coupled Plasma Reactive Ion Etching using Oxford Systems Plasma Lab 180 and 380s. Working from this general description, three etches are detailed: Cryogenic silicon etching, Pseudo Bosch silicon etching, and Silicon Dioxide etching. Data and measurements are displayed showing specifics needed for tuning etches over a limited phase space with explanations of how to qualitatively understand these etches. Chapter II then details a few etch masks we have come to heavily utilize due to the quality resulting from them. Specifically by using a sputtered alumina etch mask, high aspect ratio silicon nanowires were achievable; better than 50:1. By using an ion implanted Ga etch mask, a completely dry lithography fabrication sequence was achieved to fabricate nanoscale devices. This etch mask also provided the ability to create very low resistance contacts to the silicon nanowires. Chapter III details the results of probing the silicon nanowires using a SEM and tungsten probe tips. Details and techniques are also provided for using this tool for other potential
applications. Chapter IV provides details on creating microscale devices. Designs and measurements are provided for devices such as a homogenous 1 Tesla magnetic field, high ‘Q’ integrated silicon planar microcoils, and vertical micropillars. In the appendices, one can find calculations detailing all of the fabrication recipes I have developed and used: calculations useful for understanding problems associated with ICP etching, code for calculating magnetic fields from microcoils, and calculations for understanding how bonding wires act to reduce the expected sheet resistance of planar resistors.
Chapter I

Inductively coupled plasma reactive ion etching

Plasma etching and processing are an essential component for semiconductor fabrication. Low pressure plasmas can generate high density ion fluxes for anisotropic etching of a wide array of materials. These etching systems are routinely employed in industry for fabrication of integrated circuits and microelectromechanical systems. Further, by independently controlling both the plasma density and the momentum imparted to the ions, significant improvements in achievable structures can be attained. For the work described here inductively coupled plasma reactive ion etchers, ICPRIE, are utilized for fabrication in silicon and silicon dioxide substrates. In particular, this work used 4 etching apparatus, 3 differently configured Oxford PlasmaLab System 100 ICPRIE 380’s and a PlasmaLab System 100 ICPRIE 180. This chapter will describe the basic principles of the ICPRIE, two optimized etch chemistries for silicon, and an optimized etch recipe for silicon dioxide.

Overview of Etching

Plasma etching has two basic requirements, the generation of ions and then imparting the ions with momentum to direct them at their target. Once the ions reach their target, the ions can either mechanically or chemically remove atoms from the substrate. Although this seems like a simplistic overview, careful examination of how to control these aspects of etching defines the etching system used and examination of the etching mechanisms defines the chemistry and required etch mask. First, will be a discussion of plasma generation and how to impart momentum to ions with an incorporated discussion of the mechanical system used. This chapter will then move to describe requirements to achieve anisotropic etches, etch masks typically utilized, and finally the different modes of etching.
Physical Description of Etching

To create and sustain a plasma for etching, energy input is required. Generally, this energy is transferred via coupling of an external electric field to ions located in this field. Generation of the plasma commences with the collisions of initial ions with gas molecules; the gas is injected into a vacuum system separated by an anode and cathode. The collisions are produced as ionized electrons are accelerated between the plates, and collide with the gas. These collisions impart enough energy to further ionize the gas and further generate an increasing population of ions and electrons. As the voltage increases, the creation of ions increases over the loss mechanisms until breakdown occurs. This event is known as the Townsend Discharge. The voltage, at which this breakdown occurs, $V$, is highly dependent on the pressure, $P$, and physical characteristics of the anode and cathode, known as Paschen’s Law. Here $d$ is the distance between the two plates and ‘b’ and ‘a’ are fitting parameters.

$$V = \frac{a * (Pd)}{\ln(Pd) + b}$$

Different methods exist to generate plasmas with different characteristics [1]. Most useful to reactive ion etching, RIE, are those generated by capacitive coupled plasmas, CCP, inductively coupled plasmas, ICP, or some combination thereof. In a CCP process, energy is supplied as a voltage between an anode and a cathode plate, but in a time-varying fashion. Most commonly, a radio frequency (RF) voltage is applied to the plates; the frequency of operation is a band reserved for industrial use by the Federal Communications Commission in the United State, 13.56 MHz. In this time-varying electric field, injected gas is ionized by electrons more efficiently than in a static field. The reason for efficiency improvement is due to the difference in masses between the electrons and the ions in the plasma oscillating between the anode and the cathode plates. Massive
ions are less mobile and cannot track the rapidly oscillating electric field changes. Although the ionization region is reduced, alternating electrons get multiple opportunities to scatter and further ionize the gas. Then, by placing a capacitor between the anode plate and the RF supply, negative charge accumulates on the plate (typically referred to as the table). The resulting potential difference between the charge neutral plasma and the negatively charged plate is called the self-bias $V_b$. The electric field due to $V_b$ drives the positive ions in plasma towards the negatively charged table. This is the basis for traditional RIE.

In an ICP process, the excitation is again using a time-varying RF source, but is instead delivered inductively, via a coil wrapped around the RIE plasma discharge region, resulting in a changing magnetic field. This changing magnetic field, through the Maxwell-Faraday equation, induces an electric field that tends to circulate the plasma in the plane parallel to the CCP plates. Similarly to a CCP, collisions of the rapidly moving electrons with the slowly moving ions cause further ionizations. Loss of electrons from the plasma through the grounded chamber walls tends to create a static voltage, deemed the plasma voltage $V_{\text{plasma}}$. This is distinct from the self bias $V_b$, and will be examined later. Inductive coupling is generally realized through a large 4 to 5 turn copper coil encircling the plasma chamber.

Arrangement of the ICP with the RIE creates a very powerful combination. In the typical geometry, the combination means that one is able to change ion density, and other plasma parameters, using the ICP without significantly perturbing the incident energy of the ions which is controlled by the CCP. When etching with these combined sources, generally speaking, the ICP can then control the number of ions reaching the substrate to
chemically etch whereas the CCP controls the momentum of the ions reaching the substrate to mechanically etch.

Fig I.1 Isometric (left) and cross-sectional view (right) of an Oxford Instruments ICPRIE.

The experimental results discussed here are realized on Oxford Systems Plasma Lab 100 ICPRIE 380 and 180 systems, which utilize a CCP and an ICP power source, as seen in Fig. 1. Throughout this text, CCP power will frequently be referred to as the “forward power” or Fwd power, in order to distinguish it from the ICP power and to emphasize its role in driving ions toward the substrate’s surface. This dual plasma powering affords the greatest flexibility in altering plasma characteristics such as ion density and bias voltage independently of each other. These systems have been extensively studied, particularly for silicon etching [2].

There are a few important features of ICPRIE plasmas that have an effect on etching. Most noticeable during operation is the region of glow discharge, where visible light emission occurs from a cloud of energetic ions and electrons. As the gas particles move in the plasma, collisions occur transferring energy to bound electrons. When these electrons return to their ground state, a photon may be emitted. The color of the plasma is
characteristic of the excited gas species, because the photon energy is a function of the electronic structure of the gas molecules and their interactions with surrounding molecules [3]. This can be a useful diagnostic for incorrect plasma striking conditions or other adverse changes in your plasma. For example, in a multiple gas recipe, sometimes the emission looks like only one of the gas species, instead of the average of the colors. This happens when the other species are not being ionized, and thus will cause the process to take on a completely different character from a calibrated recipe. A second plasma condition visibly recognizable is that although the CCP has generated a plasma, the ICP power might not be increasing the ion density due to large power reflections. The two conditions are distinguishable by the luminosity of the plasmas, whereas the RIE is dim and the ICPRIE is bright. This is typically due to improper impedance matching between the ICP’s power supply and the ICP’s coil.

Impedance matching refers to the optimization process of maximizing the power delivered from the RF power supply to the plasma. For maximum power transfer from the RF supply to the plasma, the impedance of the load should be the same as the supply. Furthermore, the impedance of the plasma varies with changes in the injected gas species, chamber pressure, and desired ICP and Fwd powers. The matching condition will change even as the plasma transitions from off, high impedance, to lit, low impedance. To ensure the matched impedance condition, a network of reactive elements are tuned, typically two capacitors. As an illustration of matching a simplified schematic will be detailed here for the ICP coils. Assume a plasma has started and now the capacitors are beginning to automatically tune to minimize the power reflected back to the supply. The ICP coil (and plasma) can be modeled as an inductor with a series resistance \((s L_{\text{coil}} + R_{\text{coil}})\) which is needed to be matched to a supply’s output resistance, typically 50 Ohms and
completely real ($R_{supply}$). To match the load impedance, consisting of both real and reactive terms, to a real resistance, a capacitive term is placed in parallel with the ICP coil ($s^{*}L_{coil} + R_{coil}||1/s^{*}C_1$). The capacitive element, $C_1$, is then tuned to make the real term equivalent to that of the supply. To tune the reactive part of the load, a second capacitive element is placed in series with the load, $C_2$. Typical RF supplies are tuned to be strictly 50 or 75 ohms with no reactance, leaving the series capacitor to zero out the reactive component of the load; equivalently stated as it matches the phase of the load to the power supply. Since the inductance of the ICP coil is directly proportional to the susceptibility of the space the induced magnetic field encompasses, changing the characteristics of the plasma will change the inductance. For this reason, different etch recipes will have different matching conditions and significant variations in the values of the matching capacitors can indicate deviations from the desired etch. Matching circuits are never as simple as stated here; it is commonplace to find inductive elements in the tuning circuits. However the analysis can be generalized and is still the basis of the matching circuitry. The first equation below permits solving for $C_1$. The second equation was found by setting the reactance to zero and is used to solve for $C_2$.

\begin{align*}
R_{supply} &= \frac{R_{coil}}{(1 - \omega^2 L C_1)^2 + \omega^2 R_{coil}^2 C_1^2} \\
\frac{1}{\omega C_2} &= \frac{\omega}{1 - \omega^2 L C_1} \frac{L * (1 - \omega^2 L C_1) - R_{coil}^2 C_1}{(1 - \omega^2 L C_1)^2 + \omega^2 R_{coil}^2 C_1^2}
\end{align*}

Beneath the glow discharge region is a dark space, where atoms are no longer excited into emitting photons due to the depletion of electrons. This dark space is also the part of the plasma that most directly affects the paths of incoming ions that will accomplish the etching. Neutral atoms and other ions will tend to scatter the otherwise straight path of the ions from the edge of the glow discharge to the cathode.
Fig 1.2 Illustration of the ion angular and ion energy distribution functions, with hypothetical resultant etched profile distortion. Points in IEDF correspond to different ion kinetic energies, while points in the IADF correspond to different angles of incidence.

To characterize this spread in both energy and trajectory into probability distributions, the ion angular distribution function, IADF, and the ion energy distribution function, IEDF, are used (Jansen et al., 2009). These distributions, depicted in Fig. 2, describe the likelihood that an incident ion has a given energy and trajectory. IADF strongly affects the sidewall profile, as a wider IADF corresponds to a higher flux of ions reaching the sidewalls. Similarly, the IEDF controls the types of processes the ions can be engaged in when they reach the surface, including removing passivation species, overcoming activation energies for chemical reactions, and enhancing sputtering yield. These processes determine the performance characteristics of the etch, so understanding these effects and recognizing associated faults are paramount to optimizing a recipe. Parameters controlling the IADF and IEDF include the bias voltage $V_b$, the ion density, the gas composition, and the mean free path (which also depends on the aforementioned parameters).

*Engineering the Etch*

So far, the physics and physical characteristics of the ICPRIE have been described with respect to the plasma and ion characteristics. But engineers are typically more
interested in how the etched features change with each of the parameters mentioned. Unfortunately, etch characteristics change dramatically as the gases and substrates change. A few generalizations can be made, though, and these can serve as general guidelines.

Increase in the Fwd power generally increases the bias voltage. Since the Faraday dark space changes little the static electric field will increase, thereby imparting more energy to the ions. This increases the milling aspect of an etch for both the substrate and the mask. A faster deterioration of the mask implies that one cannot etch the substrate as long. Further, if the etch rate of the substrate is not significantly increased with the increase in Fwd power, indicating that the chemical etch rate is faster than the milling rate, then the mask with etch faster for the Fwd power increase while the substrate etch rate is left relatively unaffected. Hence the selectivity of the mask is reduced. An increase in the electric field also imparts more velocity in a direction normal to the substrate. This means that collisions in the dark space will not change the direction of the ions as much, so the IADF will become narrower.

Increasing the ICP power directly increases the vertical magnetic field through the plasma. This will dramatically increase the number of electron-gas collisions in the plasma to create more ions. Since the electrons and ions remain in the charge neutral plasma, there will be an insignificant amount of bias voltage increase. Since the ion density in the plasma is increased, there will be more reactive ions being sent to the substrate increasing the chemical aspect of the etch. This leads to highlighting the most significant advantage of etching with an ICPRIE, changes in ion density and changes in ion velocity become decoupled unlike other RIE systems.
Chamber pressure is conventionally controlled using a throttle valve and by changing the flow rate of gas into the chamber. The throttle valve is situated between the chamber and the mechanical pumping systems used to modulate the vacuum during etching, typically backed by some combination of turbo, cryogenic, or direct drive vacuum pump. Automatic controls on the throttle valve will either control chamber pressure, by sensing the pressure and opening or closing the throttle valve accordingly, or by setting the valve to a given position. Gas flow rate is usually established for a given chamber size to hold a desired pressure. What is more important is the ratio of flow rates if multiple gases are utilized. Correctly setting the ratio can enable a chosen chemistry to dominate. In general, addition of more gas will alter the generation rate of ions but the effect is usually insignificant to ICP power modifications. Controlling the pressure together, the throttle valve and gas flow do have a significant effects on etched features. In general, in order to strike a plasma the pressure needs to be set for the gas based on a modified Paschen's Law, and this may or may not be the pressure at which the etch is conducted. Further, once the etch is struck, modification of the etch pressure can change the electric field. Decreasing the pressure increases the distance for Debye length of the ions in the plasma, allowing for the plasma to spread; this reduces the dark space which in turn increases the electric field driving the ions. Further, collisions in the dark space are reduced which in turn reduces the IADF. Hence a lower pressure can reduce the undercut seen on the sidewalls.

Although changing the physical parameters of the etch using power and pressure has a significant amount of control over profile, the most essential aspect of the etch is the gas chemistry used. Etch chemistries vary widely, even for the same substrate [4]. Here the focus will be on silicon and silicon dioxide; several etch chemistries will be discussed.
Etch chemistries can be generalized into two basic groups, unpassivated and passivated. Unpassivated etch chemistries are easiest to control, such as with sulfur-hexafluoride (SF$_6$) or the combination of tetrafluoromethane (CF$_4$) mixed with oxygen (O$_2$). With the SF$_6$ chemistry, the ICP controls the density of F ions in the plasma and the Fwd Power controls the momentum applied. Three basic etching mechanisms for the Si exist under this chemistry: 1) F ions reach the substrate, chemically combine with the Si to form a volatile SiF$_4$ and are pumped away (chemical etching), 2) F ions impinge on the substrate and knock away a Si ion (milling or mechanical etching), and 3) F ions impinge on the substrate, chemically bind with the Si (ion assisted etching). Using the generalities from earlier, the ICP predominately controls the chemical etch rate, the Fwd Power predominately controls the milling rate and the IADF, and the pressure controls the IADF.

Changing ratios of different gases can add another parameter to control separate from those already mentioned, such as with the combination of CF$_4$ and O$_2$. By increasing the O$_2$ for a given CF$_4$, the etch rate of silicon can be suppressed while the etch rate of silicon dioxide, slower than that of silicon for low oxygen levels, can be left unaffected. Gottlieb et al. [5] demonstrated that although the silicon etch rate peaks when the CF$_4$/O$_2$ ratio reaches 12%, by continually increasing the ratio past 23% silicon etch rate can be reduced below the etch rate of the silicon dioxide. This idea is intriguing since it adds a new parameter to control for etching. The biggest disadvantage of unpassivated silicon etches is that there does not exist any means to protect the etched sidewalls from non-vertical ions. While increasing the Fwd power and decreasing the pressure can narrow the IADF, there will always be some ions that will laterally etch the silicon sidewalls. When this lateral etching becomes an issue passivated silicon etch chemistries are utilized, such as with nanoscale etching.
Passivated silicon etches are designed to protect the etched sidewalls from this lateral etching. Just as a second gas, $O_2$, was used to modify the etch rates of silicon and silicon dioxide in the $CF_4/O_2$ etch, other gases can be used to create passivation layers. Further, the timing of when the passivation gas is used can be changed as well. This idea leads to a useful categorization of etches suggested by Jansen et al [2] and will be used here, pulsed mode and mixed mode silicon etches. Both etch schemes employ forms of etching combined with passivation that actively protect sidewalls during etching and improve anisotropy. Each has their own advantages and disadvantages which will become clear during the discussion. The pulsed mode etch, sometimes referred to as a chopping etch, uses gas “chopping” to alternately etch and deposit inhibitor on the sidewall surface. The mixed mode etch uses a gas chemistry to form passivating compounds at the sidewalls at the same time as etching.

As mentioned, the chopping etch requires two alternating plasma steps. The first step etches the silicon for a short period then rapidly shuts off the gas and plasma. The second step then initiates a plasma that deposits an inhibitor film on exposed surfaces. This alternating sequence continues as the etch progresses in depth. Inherent in the discreteness of the etching is notching on the sidewalls that occurs every step. The duty cycle between steps controls the etch angle and the total length of the combined steps controls the depth of the notching. In contrast, mixed mode etching combines the discrete etch and passivation steps into a single continuous etch. As the etching gas is driven down to the substrate, the passivation gas is also directed downward and creates a protective layer. The passivation rate is selected such that the milling rate for the vertically directed ions is enough to etch through the horizontal passivation layers and continue etching into the substrate. When the laterally directed ion etch rate, as determined by the
IADF, is less than the horizontal passivation rate, the sidewalls develop a protective layer. By balancing the ratio of etch and passivation gases for both the pulsed and mixed mode etches, not only can undercutting be reduced but the angle at which the silicon is etched can also be controlled.

In this work, multiple passivated etch chemistries are used for silicon etching. The majority of the silicon etching relies on SF$_6$ etch gas. Described earlier, the F ions and radicals interact with silicon to generate the etch product SiF$_4$. For passivation gases, O$_2$ and Octafluorocyclobutane (C$_4$F$_8$) are utilized here. The first chemistry discussed involves using SF$_6$ and O$_2$ at cryogenic temperatures, known as the Cryogenic silicon etch. For this mixed mode etch chemistry, a reduction in temperature below -85 C permits a SiO$_{x}$F$_{y}$ to grow on the sidewalls to act as a passivation layer while the F etches the silicon. A second mixed mode silicon etch described here uses a SF$_6$ etch gas while simultaneously passivation with C$_4$F$_8$ [6]. This etch is referred to here as pseudo Bosch; this name refers to the fact that the Bosch etch utilizes same gas chemistry but in pulsed mode. A passivated etch chemistry is also demonstrated here for silicon dioxide. This etch chemistry is similar to the CF$_4$/O$_2$ described earlier, but using C$_4$F$_8$/O$_2$ instead. The interesting aspect of this etch is that the same gas which creates the passivation is also the same gas that is etching the silicon dioxide.

Cryogenic Silicon Etching

The first etch discussed here is a mixed-mode silicon etch performed with substrate temperatures ranging from -85 C to -140 C. The cooler wafer temperature encourages growth reactions of silicon with oxygen to generate thin passivation layers while simultaneously etching. This section on the Cryogenic silicon etch will detail the
characteristics of the etch, etch rate control, angle control, and the notching effects seen at the top of the etched structures. Finally, techniques are demonstrated for where this etch is most useful and coupled with a discussion of the appropriateness of specific etch masks.

General Characteristics of Cryogenic Etching

The cryogenic silicon etch is a passivated etch utilizing SF$_6$ as the etch gas and O$_2$ as a catalyst for the passivation and was first demonstrated by Tachi et al [7]. As described earlier, the SF$_6$ is ionized in the plasma to create a mixture of SF$_x$ and F species; where x denotes a number between 1 and 5. The most useful ion from this splitting is the fluorine ion. When the F ion reaches the substrate, the F can remove a Si atom using one of the 3 etch mechanisms described earlier. When the ions chemically recombine with the silicon a volatile gas is created, SiF$_4$, and the etch product is pumped from the chamber. What is specifically unique about this etch is that a passivation layer can be created with O ions and the partially etch product SiF$_x$. By lowering the temperature below -85 C, recombination of Si, O, and F becomes energetically favorable and a thin SiO$_x$F$_y$ layer is created [8]. Essentially, as one or two F atoms diffuse into the Si lattice, O atoms can arrive and bond, Mellhaoui et al [9]. This thin film acts as a thin protection layer from milling ions such as SF$_5$. If the flux of milling ions is low, for example on the sidewall of the etched structure, then the passivation can reduce the chemical etching and improve the anisotropic nature of the etch. It should be noted that the passivation can be created from other means, such as ionization of the etch gas SiF$_4$. In fact, it has been demonstrated that injection of SiF$_4$ and O$_2$ can actively passivate during the etch; chopping-mode etches using this chemistry have also been demonstrated [10]. Upon bringing the wafer back up to room temperature, this passivation layer then becomes volatile and evaporates away.
This passivation scheme becomes very attractive for deep reactive ion etching, DRIE. Using the mixed-mode scheme, the plasma density and chemical etch rate can be significantly increased while protecting the sidewalls of the etched structure. Upon warming the substrate up, the etch mask evaporates. Further, the gases required for the etch are substantially cleaner and less costly than that required for chopping-Bosch etching. Since the etching and passivation are continuous, the sidewalls of the etch are significantly smoother than possible with the chopping-Bosch due to its scalloping etch characteristics [11]. Indeed, this etch chemistry has generated much interest due to all of its positive attributes. In particular, two influential papers by de Boer and Jensen et al [2,12] provide a significant amount of discussion on control over the cryogenic etch. To assist the reader with developing intuitions with regards to this etch, a qualitative description of etch control will be discussed here.

It is useful to understand how essential parameters may affect the etching rate and profile of the etched structure. As stated earlier, the advantage of using an ICPRIE is the separation of control over the chemical etch rate and milling etch rate. The cryogenic etch is predominately a chemical etch, so controlling the F ion density greatly controls the etch rate. Control mechanisms over the ion density include ICP power, SF$_6$ flow rate into the etcher, and pressure control. Increasing the ICP power essentially ionizes more of the SF$_6$ injected into the chamber. As the ICP power increases, an increase in etch rate is noted with etch rates recorded from 1 to 10 microns per minute. This increase is easily attributed to the improvement of the ionization efficiency of the gas. In the same manner, increasing the injected gas also increases the amount of ionization. Unlike increasing the ICP power, however, increasing the flow rate of the gas past a critical point for a given ICP power can lead to a decrease in etch rate, possibly due to an increase in scattering of
ions. Although increasing pressure does permit a slight increase in etch rate, significant pressure increases without increasing the SF$_6$ flow rate can lead to instabilities in the plasma and difficulty in striking the plasma.

As just stated, the cryogenic etch is predominantly a chemical etch. It was also stated that DC bias gives a measure of the amount of milling occurring and that Fwd power generally dominates the DC bias. Evidence for this fact is seen from varying the ICP and Fwd power. From the data displayed, although ICP power is varied over a range 100 times as big as the Fwd power, it only has $1/5^{th}$ the effect on DC bias. However, the data also clearly shows that the overall etch rate is dominated by the ICP power.

![Cryogenic Silicon Etch](image)

**Fig I.3**  Changes in DC bias voltage as ICP power (left) and Fwd power (right) are increased for the cryogenic silicon etch.

Increase in the Fwd power, around the 0 to 40 W range, results in almost immeasurable etch rate changes, although it does offer significant increase in DC bias voltage. Conversely, increasing the ICP power shows relatively little change in DC bias voltage but significant increase in etch rate. Clearly, the cryogenic etch is predominantly more of a chemical etch than a milling etch.
Fig I.4 Changes in etch rates as ICP power (left) and Fwd power (right) are increased for the cryogenic silicon etch.

The starting etch conditions for the measurements made here are as follows:

<table>
<thead>
<tr>
<th>SF₆</th>
<th>70 sccm</th>
<th>ICP Power</th>
<th>900 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>O₂</td>
<td>5 sccm</td>
<td>Fwd Power</td>
<td>5 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-120°C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

As seen, the cryogenic etch is usually performed under very low DC bias conditions. This demonstrates the significant advantage of low Fwd power etching; if the milling rate is low, then the etch mask can survive for much deeper etches. For this reason, the cryogenic etch has been measured to achieve etch mask selectivity values of 100:1 for photoresist etch masks, 200:1 for silicon dioxide etch masks, and more recently 3000:1 for alumina. Etch masks and mask selectivity will be discussed in more detail later. From the selectivity standpoint, one finds that lowering the Fwd power generally increases the etch mask selectivity. Some amount of milling is required, however. Injection of O₂ into the etcher provided the needed chemistry for passivation. This passivation is highly desired on the sidewalls for protection, but on the horizontal surfaces the passivation layer needs to be milled away for the silicon etching to occur. If the Fwd power is too low for a given
O₂ flow rate at a given temperature, incomplete removal of the passivation on exposed horizontal silicon surfaces can occur and black silicon can initiate. Black silicon is essentially silicon spikes that occur due to micro-masking [12]. Presumably, the name stems from the observation that these spikes appear optically absorbing, flat black. If black silicon begins for a given etch condition, increasing the Fwd power a few watts can remove the effect. There is also an aspect ratio dependence on when black silicon occurs which will be discussed later.

![Image of black silicon between silicon micropillars](image)

Fig 1.5 Black silicon beginning to form between silicon micropillars. The oxygen flow rate is too high for the given forward power creating a passivation layer on the horizontal surface.

*SiOₓFᵧ Passivation Control*

Passivation control is had using both the temperature and O₂ flow. Essentially, increasing passivation requires improvement in reaction probability; several examples are
reducing temperature, requiring more O ions to reach the silicon sidewalls, or increasing O\textsubscript{2} flow rate. Substrate temperatures are automatically controlled by throttling LN\textsubscript{2} to the plate. Typically, lowering the temperature improves the passivation with typical temperatures in the range of -110 C to -140 C. Holding temperature stable can be critical as seen from wavy etch sidewall profiles generated as the plate temperature fluctuates by 10 degrees. This effect was demonstrated by the following etch performed under these conditions:

<table>
<thead>
<tr>
<th>SF\textsubscript{6}/O\textsubscript{2}</th>
<th>70 / 4 sccm</th>
<th>ICP Power</th>
<th>900 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td>30</td>
<td>Fwd Power</td>
<td>2 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-130C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

During this 30 minute etch, the temperature dropped to -122 C then cooled back to -130 C. Qualitatively, as the etch became warmer less sidewall passivation occurred forcing the etch to become slightly reentrant. As the etch began to slowly cool back to -130 C the etching angle returned to the optimized 90 degrees. The pattern was hexagonally spaced pillars of 20 micron diameters separated by 20 microns. The mask used was AZ 5214e photoresist 1.6 microns thick.

Typically then, it is advantageous to hold the table temperature as steady as possible. To assist the LN\textsubscript{2} regulator on the Oxford machine, the LN\textsubscript{2} dewer was pressurized to 35 psi using house nitrogen and regulated. This example is useful in that it clearly shows that temperature controls passivation.
Fig I.6 Demonstration of the effect substrate temperature has on the angle of the cryogenic etch. The pattern was 20 micron diameter pillars arranged in a hexagonal array. The etch temperature varied from -130 C down to -122 C.

A second method for controlling passivation, and hence etch angle, is the Oxygen flow rate. Flow rates of O₂ typically range from 2 to 10 sccm and can change the angle of the etch around 10 degrees. The range is based on two extremes, no passivation and the beginning of black silicon. In the first case, too little oxygen implies that the SiOₓFᵧ layer will not have enough atoms to act as a protective layer. Further, controlling the flow rate in these low flow regimes becomes difficult based upon the size of the Oxygen mass flow controller, MFC. The Oxford machines used had 100 sccm Oxygen MFCs which implies that flows below 2 sccm were unstable. In the second case, so much O₂ is present that, for a given milling rate, small islands of passivation begin to form on the horizontal surfaces. These stochastically located passivation areas then begin to act as masking for the silicon and the black silicon forms. For the -120 C cryogenic etching temperatures, it
was experimentally determined that for low aspect ratio trenches the maximum O$_2$ flow rate was 7.5 sccm when Fwd power was set to 5 W.

Controlling O$_2$, then, provides a useful mechanism for controlling the angle of the silicon etch. This work has be detailed elsewhere [13] and the results will be summarized here. To determine the angle, silicon micropillars were etched with different O$_2$ flow rates. The mask used was 1.6 microns of AZ 5214e of photoresist. The pattern utilized was 5 micron circles separated by 5 microns, 10 micron circles separated by 10 microns, 20 micron circles separated by 20 microns and 50 micron circles separated by 50 microns in a hexagonal packed array all on the same substrate. Having multiple diameter pillars on the same substrate permitted aspect ratio dependence to be ascertained. Since the spacing was equal to the pillar diameter, the pattern also permitted the definition of aspect ratio to be defined by both the ratio of the pillars height to the pillars width as well as the etched trench’s ratio of height to width; the latter definition is more utilized in the etching community. The etch was performed under the following cryogenic conditions:

<table>
<thead>
<tr>
<th>SF$_6$</th>
<th>70 sccm</th>
<th>ICP Power</th>
<th>900 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td>40 min</td>
<td>Fwd Power</td>
<td>5 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-120C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

The angle, etch depth, and photoresist remaining was measured using a FEI Quanta SEM. By sweeping the O$_2$ from 3.5 to 7.5 sccm, a linear dependence was ascertained for each of the micropillar diameters. The 7.5 sccm data points were removed since black silicon was observed in the trenches. The aspect ratio dependence of the O$_2$ flow rate is
evident by the observation that for a given $O_2$ flow rate, the width of the etched trench increases the angle of the etched pillar traverses from positive taper to reentrant. This aspect ratio dependence will be discussed later in this chapter.

![Graph showing the linear correspondence between etch angle and $O_2$ flow rate for different pillar diameters.]

**Fig I.7** Angle control using $O_2$ flow rate for the cryogenic etch. A linear correspondence was established for each of the diameter pillars: 5 micron, 10 micron, 20 micron, and 50 micron.

This implies that precision flow rates are required for reproducibility. More generally, any factor which changes the bonding characteristic or probability of bonding, such as preventing the oxygen from reaching the etched sidewalls, will change the angle of the etch. It is also obvious from the low flow rates that any minor change will have drastic effects on the angle. One such effect could be a dirty chamber in which oxygen is scavenged. For this reason, it is highly recommended to begin cryogenic etching with a recently cleaned chamber. A typical cleaning includes: opening the chamber and scrubbing the sidewalls clean, immediately following is a high pressure SF$_6$/O$_2$ plasma at room temperature. Once clean, the chamber is then seasoned by running the desired
etch recipe on a blank silicon wafer. If a cleaning is not permitted, a temporary fix can be achieved by lowering the table temperature.

Aspect Ratio Dependent Etching

As the title implies, etch rates in a trench have a complicated dependence on the aspect ratio; the etched trench’s depth to width ratio. The fundamental problem is that as the aspect ratio increases, the etch rate significantly decreases [14]. This etch rate decrease is not associated with increasing substrate surface area; this particular comment leads to a slight diversion. As the exposed silicon surface increases, by either etching a trench and thereby creating more exposed surface area, or by changing the etch mask and exposing more substrate, etch rates are known to change [15]. Further, with etch chemistries such as the cryogenic etch, changing the exposed silicon also changes the etch chemistry slightly. The term for etch chemistry changing with increasing surface area is ‘microlading’. For single sample processing, a simple trick can eliminate both of these problems. By placing the masked sample on a much larger carrier wafer one can make both the effects a small perturbation to the overall surface area exposed. As an example, a 1 cm square silicon masked sample placed on a 6 inch carrier wafer becomes rather unaffected by changing mask patterns or increased surface area from the sidewalls. This technique does not solve the problem with whole wafer processing, however, and remains an open problem plaguing industry.

Aspect ratio dependent etching (ARDE) is widely seen in ICP etching. Multiple possible culprits have been suggested, summarized by Gottscho et al [16], and will be quickly reviewed here. First what is not the culprit is the conductance of etch products from the etched trenches preventing incoming etch gas from reaching the silicon. Coburn et al. studied this problem using very simple conductance arguments and ruled it as invalid...
[17]. Unfortunately, Coburn did not detail his calculation or give underlying geometry assumptions. Appendix B computes the conductance of a trench with assumptions stated and gives a formula for various geometrical configurations. The most likely 4 contributors to ARDE are Knudsen transport of neutrals, ion shadowing, neutral shadowing and differential insulating charging.

Although each of these will be described here, what first needs to be clarified is the difference between ions, neutrals, and radicals. Previously, it was explained that etching is separated into chemical etching and milling and that ions performed both. While not untrue, a deeper description can be made. When ions recombine with the many electrons, they become known as neutrals. When the neutrals have incomplete ionizations, they remain chemically active and are referred to as radicals. This recombination event can occur at anytime but as soon as it does, the atom no longer becomes influenced by the electric field but instead is dominated by diffusion. In cryogenic etching the neutrals are predominantly responsible for the chemical etching with measured radical to ion flux ratios of 1500 to 8300 [8]. Ions are still required, however, to break up the passivation layer that forms on the horizontal surfaces, milling. Ions also play a role in transport of the neutrals and an overall interacting dependence of using both the ions and the neutrals is referred to as ion-neutral synergy. Measurement of the ion density is directly performed using a Langmuir probe and measurement of the neutrals is performed using optical emission spectroscopy. Since these measurement tools are not typically found on etching machines, it becomes appropriate to use the ideas of chemical etching and ion milling. Similar to the radical to ion flux ratios, recall that etch rate variations due to chemical etching and milling variations (ICP and Fwd power changes respectively) were 1-2 microns per minute and less than 10 nm per minute respectively.
Knudsen transport of neutrals is the movement of atoms with which have long mean free paths but are travelling in a channel of dimensions significantly smaller with reflections off the sidewalls [18]. The channel dimensions are typically 10 times smaller than the mean free path. Since mean free paths are approximately 1 cm at 10 mTorr, most etched structures have some dependence on Knudsen transport. Ion shadowing refers to the principle of IADF referred to earlier. As the etched structure becomes deeper, the angle subtended from the bottom of the trench to the plasma reduces; as the angle reduces so does the possible number of ions to reach the bottom of the trench to etch. Neutral shadowing is the same fundamental effect as the ion shadowing but instead with neutrals instead of ions which move under different mechanisms. Finally, if the etched substrate cannot conduct the positive charge, as is the case when etching the top silicon layer of silicon on insulator (SOI), then the positive charge can begin to repel the incoming ions. This reduction is referred to as differential insulating charging.

As stated earlier, differentiation and measurement between these contributors in etching systems is difficult. Instead a different approach is to model ARDE as a perturbation from aspect ratio independent etching. Using this method, a set of differential equations can be established.

\[ \frac{dD}{dt} = E - b \frac{D}{W} \]

Where D is the etch depth, E is the etch rate for an aspect ratio of zero, b is a coefficient to be fitted describing the etch rate reduction due to aspect ratio, and W is the width of the minimum etched spacing between the pillars. This model is intended as an approximation for etching rates and should closely approximate the rates seen for etching trenches of similar aspect ratios. The assumption made for this model is that the ARDE
rate scales linearly, the simplest possible model describing the aspect ratio effects. Solution to this ODE yields the following equation.

\[
D = \frac{E \cdot w}{b} \cdot (1 - e^{-\frac{b \cdot t}{w}})
\]

E was determined to be 1.15 microns per minute and b was 0.04099 microns per minute by curve fitting the width normalized data, D/w and t/w, resulting in an R-square fit of 0.9972.

Fig I.8 Cryogenic etch data for various aspect ratios of silicon micropillars. The data was width normalized to solve for the E and b coefficients.
Fig I.9 Cryogenic etch depth dependence on time for silicon micropillars. The curves are generated from the solutions to the generalized etching rate equation with E coefficient set to 1.15 microns per minute and b coefficient set to 0.041.

Although this model predicts etch height accurately, it does have several drawbacks. This first is that it is a non-physical model; it is not modeled on the underlying physics of etching. So if the etch is dramatically changed, the model would require etch data for determination of the etch coefficients. Second, it does not offer any understanding as to how ARDE might be eliminated. What this model does offer, however, is a rapid characterization method. One etch of the multi-diameter pillar mask offers 4 data points to solve for two coefficients and yields an accurate and predictive tool. As an example, a 10 micron diameter pillar (actual spacing between pillars was 9.5 microns) was etched for 80 minutes. Not accounting for ARDE, one would predict the etched height to 92 microns based on the 1.14 etch rate. Using the rate equation model, an etch height of 77.8 microns was predicted. The actual height, measured in an SEM was 76.5 microns; 1.7% error from predicted etched depth.
Control over the etch depth is only part of what is needed for control over the total etched profile. The other needed control is over the angle, which was previously discussed. It was seen that a first approximation to the oxygen dependence on angle was a linear fit and permitted over 6 degrees of angle control. One can begin to exercise more control over the structure now by creating a similar rate equation for trench width control. This begins by creating a differential equation for relating the width of the trench to the depth of the trench based on a geometrical argument. A small deviation of width with respect to a small deviation in height is related by the tangent of an angle. If the etch is perfectly vertical, then this angle is zero. Then recognizing that a factor of 2 is needed to account for the fact that both sides of the trench is etching, the following differential
equations can be created. Similar to solving for the b and Eo coefficients in the etch depth dependence, $\beta$ and $\varepsilon$ are coefficients to be similarly solved for. Results can be quite dramatic. As a demonstration of this effect several sets of micron sized pillars were etched. Qualitatively, the outside of the pillar has an aspect ratio of zero; hence the b coefficient should be 0. From the angle dependence on the oxygen graph, interpolating the angle for a very large width, it is clear that the angle would be a negative value. Hence, the outside of the pillars which see an effective aspect ratio of 0, the pillars should taper inward. For a spacing of 5 microns between pillars, the oxygen dependence yields an etch angle of approximately 4 degrees. This means that the spacing between the two pillars should close faster than for an etch depth of 35 microns. Note that as the pillars close, the aspect ratio increases which increases the angle due to the oxygen dependence. This positive feedback mechanism will force the spacing to close faster than expected. For this reason, it is clear that more analysis should be performed on the aspect ratio dependence of angle to permit accounting of this feature.

$$\frac{dW}{dt} = 2\tan(\beta \cdot [O_2] + \varepsilon) \cdot \left( E_o - b \frac{D}{W} \right)$$

$$\frac{dD}{dt} = (E_o - b \frac{D}{W})$$

Fundamentally, the ARDE problem is one of getting etching ions and neutrals to the base of the trench; in this case it is fluorine atoms. It stands to reason if the fluorine flux is restricted, so should the oxygen flux. Further, if Knudsen transport relies on reflection off the sidewalls, then if the oxygen has a different binding probability than that of the fluorine the aspect ratio dependence might strongly differ. It was previously shown how the etch angle is dependent on the oxygen flow rate, so any change in flow rate due to aspect ratio should be manifest on the angle.
Fig I.11 SEMs of a cryogenic etch of multiple diameter silicon micropillars, etched approximately 55 microns (left) and 25 microns (right). The outside of the pillars were predicted to taper inward and a 5 micron gap was expected to close before the etch depth of 35 microns was achieved.

Fig I.12 Cryogenic etch angle dependence on aspect ratio for silicon micropillars.
Pseudo Bosch Silicon Etching

The second etch described in this thesis is the SF$_6$/C$_4$F$_8$ silicon etch dubbed pseudo Bosch etch here. This etch is a mixed-mode passivated etch which etches slower than the cryogenic etch making it indispensible for nanoscale etching. Unlike the cryogenic etch, the passivation gas and the etch gas injected for ionization are different. This leads to the etching rate equation and the passivation rate equation to be completely decoupled making control over the etch profile significantly easier. Although this etch has been widely used in the semiconductor industry, details on this etch are scarce; due to the nature of the industry. To illuminate this subject, this section is dedicated to understanding this etch more.

General Characteristics of Pseudo Bosch Etching

As stated, this etch uses the same chemistry as the Bosch etch. SF$_6$ is injected and ionized in the chamber to provide fluorine ions and radicals to etch silicon; the etch product is SiF$_4$. C$_4$F$_8$ is injected and ionized to create a polymer chain of CF$_2$ which is deposited on the substrate. This polymer protects the surface of the silicon from chemical etching. However, the milling generated by the acceleration of SF$_x$ and F$_y$ ions in the DC bias electric field can remove the passivation layer on the horizontal surfaces faster than the polymer can redeposit. Overall, the effect is a sidewall coated in polymer with the horizontal surfaces free to etch. The Sisyphean task of removing the horizontal polymer deposition prior to etching silicon is the reason why this etch rate is an order of magnitude slower than chopping Bosch etching. But unlike Bosch etching, the continuous passivation and etching prevents scalloping inherent in the Bosch etch. The slower etch rate and smoother sidewalls makes this etch ideal for nanoscale structures.
Due to the high popularity of Bosch etching in industry, C₄F₈ has been widely studied. Although it is widely used, there is active research in replacing the gas with other mixtures of carbon and fluorine since the gas is a perfluorocarbon which is considered a greenhouse gas. The C₄F₈ gas is a molecule in which each of the carbon atoms are connected together with a single C-C bond. Two fluorine atoms are then bound to each of the carbon atoms. When the gas ionizes, the C-C and C-F bonds are broken up. Using optical emission spectra, Rhee et al., the predominant ion species have been determined to be CF₂, C₂, and C₃. Ideally, the CF₂ form long polymer chains that cross link, deposit, and protect etched sidewalls on the silicon surface. The fluorocarbon film is typically characterized by measuring the fluorine to carbon ratio; the higher the less strong the cross linking.

![Ball and stick models of C₄F₈ (left) and CF₄ (right) molecules. When the C₄F₈ molecule ionizes in a plasma, it primarily forms a protective CF₂ polymer chain. Introduction of F ions from an SF₆ plasma can neutralize the CF₂ into CF₄. Reproduced from www.wikipedia.org.](image)

The SF₆ is then simultaneously injected into the chamber and ionizes into mixtures of SFₓ and Fᵧ for use in etching. However, the fluorine ions can scavenge the CF₂ molecules
to create CF$_4$ molecule [2]. If the gas is pumped away, the overall effect is a reduction in passivation and etching. This recombination also acts to slow the etch rate as compared to the chopping Bosch. Another interesting aspect of the fluorocarbon polymer is the deposition rate, approximately 20 to 30 nanometers per minute. This is important because it describes the minimum milling rate required for silicon etching to occur. When thinking about a hypothetical etch rate equation, additions from chemical etching and milling are reduced due to the polymer deposition rate. From the cryogenic etch it was seen that chemical etching was significantly dominant over the milling and hence the etch was considered chemical. With the pseudo Bosch etch, a significant amount of milling must occur to remove the much thicker passivation layer for silicon etching to occur. For this reason, the pseudo Bosch etch is considered more of a milling silicon etch than a chemical etch.

To understand the general characteristics of this etch, several experiments were performed. First is parameter sweeps to understand what occurs with DC bias voltages. Similar to the cryogenic etch, the DC bias increases linearly as Fwd power is increased and decreases as ICP power is increased for the same reasons described previously. A major difference is that the cryogenic etch was operated around 35 V where as this etch is typically closer to 100 V attesting to the milling required by this etch.
Fig I.14  Changes in DC bias voltage as ICP power (left) and Fwd power (right) are increased for the pseudo Bosch silicon etch.

Fig I.15  Etch depth for various etch times for the pseudo Bosch silicon etch. A linear least squares fit to the curve yields an etch rate of 284 nm per minute.

The conditions for the pseudo Bosch etch are as follows:

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<thead>
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</thead>
<tbody>
<tr>
<td>SF₆</td>
<td>33 sccm</td>
<td>ICP Power</td>
<td>1200 W</td>
</tr>
<tr>
<td>C₄F₈</td>
<td>55 sccm</td>
<td>Fwd Power</td>
<td>20 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>15 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>
As a further comparison to the cryogenic etch, it was seen that the passivation gas flow rate, oxygen, was small when comparing the etch gas flow rate. When the ICP power increased, the cryogenic etch rate increased since the passivation amount changed very little. Unlike the cryogenic etch, the pseudo Bosch etch behaves significantly different. Since the passivation gas flow rate is almost twice that of the etch gas, increasing the ICP power creates more passivation ions than fluorine ions. Instead of increasing the chemical etch rate, increasing the ICP power of a pseudo Bosch etch actually slows the etch down, significantly! Doubling the ICP power from the standard 1200 W to 2400 W cuts the etching rate in half, down to 150 nm per minute. This data set was measured by etching silicon masked with PMMA and patterned using a Leica EBPG. The etches were conducted using the parameters mentioned earlier and the patterned trench widths were greater than 20 microns to eliminate any aspect ratio dependent etching. Each etch was performed for 3 minutes to average out the effect of the strike step.

![Fig I.16](image_url)  
**Fig I.16** Etch rate variation for various ICP powers for the pseudo Bosch silicon etch. The etches were conducted for 3 minutes and the etch depth averaged over the sample.
In a similar methodology, the etch rate was also measured for varying the Fwd power. The most important aspect of the curve is the dramatic decrease in etch rate as Fwd power lowers below 10 W. It is at this point, the milling is becoming comparable to polymer deposition rate.

![Fig I.17 Etch rate variation for various Fwd powers for the pseudo Bosch silicon etch. The etches were conducted for 3 minutes and the etch depth averaged over the sample.](image)

A dramatic difference between the pseudo Bosch etch and the cryogenic etch is the selectivity of silicon to photoresist. Where the cryogenic demonstrated a 100:1 selectivity, pseudo Bosch shows, at best, a 5:1 selectivity. As a specific example, a 55 nm thick PMMA resist was patterned with ridges with widths starting at 1 micron and increasing; this ensured that aspect ratio would not be a factor. The etch was performed for 1.3 minutes with a trench depth of 257 nm. Although all of the resist was etched away, the depth of the trench demonstrated exactly how deep the etch was able to perform before the mask completely failed. Once the mask failed, the top of the ridge was etched at the same rate as the bottom preserving the relative height between the top and bottom of the trench. This yields a selectivity of 4.7:1 for electron beam resist and silicon. Although,
PMMA is useful for patterning nanoscale features, such low selectivity implies that mask erosion is the primary concern when using it as an etch mask.

**Silicon Dioxide Etching**

The silicon dioxide etch employed here is the easiest to understand. Unlike the two silicon etches described earlier, this etch is mostly from a single gas etch. Injection of C$_4$F$_8$ into the chamber is ionized and accelerated to the silicon dioxide surface for etching. Although this etch is modeled after a classic CF$_4$ etch, some subtle differences arise and will be discussed. A fabrication sequence will also be described for using this etch to define metal structures in quartz wafers.

*General Characteristics of the Silicon Dioxide Etch*

The chemical basis of this etch is relatively simple. C$_4$F$_8$ injected into the ICP and ionized to create a mixture of fluorine and carbon ions [5]. These ions are then accelerated down to the SiO$_2$ substrate where the fluorine combine with the silicon and the carbon combine with the oxygen. The volatile etch products, SiF$_4$ and CO$_2$, are then pumped away leaving the etched structure. Stoichiometrically, for every SiO$_2$ molecule needed to be removed, 1 carbon and 4 fluorine atoms are required. This leaves a few extra carbons in the chamber which have the potential to redeposit on the substrate and act as a potential micro-mask. Notice that there is a lack of radicals in the plasma which have the ability to etch a carbon atom from the substrate. For this reason, a small amount of oxygen is injected.

For this etch, there is no dedicated passivation gas being injected. However, this does not imply that sidewall passivation is not occurring. From looking at the chopping Bosch etch in which an entire step, similar to this one, is dedicated to passivate the silicon
sidewalls, it should in fact be expected that a CF$_2$ polymer is being deposited [19]. So this etch is similar to the pseudo Bosch etch in which the substrate is being simultaneously etched and passivated creating a very high anisotropic etch. The etching conditions utilized here are as follows:

<p>| | | | |</p>
<table>
<thead>
<tr>
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<th></th>
<th></th>
<th></th>
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</thead>
<tbody>
<tr>
<td>O$_2$</td>
<td>2 sccm</td>
<td>ICP Power</td>
<td>2100 W</td>
</tr>
<tr>
<td>C$_4$F$_8$</td>
<td>45 sccm</td>
<td>Fwd Power</td>
<td>200 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>20 C</td>
<td>Pressure</td>
<td>7 mt</td>
</tr>
</tbody>
</table>

Again the etch rate was determined experimentally by etching multiple substrates for multiple times and linear least squares fitting the data; etch rate was determined to be 388 nm per minute. This etch was performed on a 2.4 micron thick thermally oxidized silicon wafer using chrome as an etch mask. Chromium etch masks are common since they offer good etch selectivity; here approximately 300 nm of chrome was thermally evaporated with approximately 50 nm consumed during 4 minute long etches. This gives a selectivity of better than 32:1. Resist masks, 1.6 microns thick, were simultaneously used to mask silicon wafers during the oxide etches. Only 230 nm of resist remained for the 4 minute etches yielding a selectivity of 1.1:1.
Fig I.18  Etch depth for various etch times for the silicon dioxide etch. A linear least squares fit to the curve yields an etch rate of 388 nm per minute.

Increasing the ICP power increases the density of radicals. Some of these radicals are being used for etching the silicon dioxide and some are being utilized as a passivation. Looking at the pseudo Bosch etch, increasing the ICP actually increased the passivation rate over the chemical etch rate for the combined effect of reducing the silicon etch rate. For the silicon dioxide etch, increasing the ICP power increases the etch rate. This implies that the etch gas formation is greater than passivation. This data was generated by etching the 2.4 microns of thermal oxide on silicon using a chrome mask for 4 minutes then measuring the etch height.
Fig I.19  Etch rate variation for various ICP powers for the silicon dioxide etch. These etches were conducted for 4 minutes and the etch depth averaged over the sample.

A second useful piece of data observed while increasing the ICP power was that the sidewalls did not significantly undercut as power increased. With non-passivated etches increasing the ICP generally increases the undercut of the mask since the etch is becoming more isotropic (chemical). As stated earlier, this lack of undercutting is due to the sidewall passivation being simultaneously deposited. Using high Fwd power milling rates, the horizontal passivation can be milled leaving the sidewall passivation intact. It is noted that ICP power cannot be indefinitely increased and expect to have the etch rate increase continuously. Although the exact culprit for this lack of curvature is unknown, it is possible that this phenomenon is linked to two possible explanations. First, and most likely, is that for a given gas flow rate the ionization rate is becoming limited due to a reduction in possible ionization targets (the effective ionization cross section is being reduced). A second possible explanation is that the stoichiometry of the plasma is shifting from etch product heavy to passivation product heavy (more CF$_2$). An easy experiment to
verify the first explanation would be to repeat the same ICP power sweep as but using different $C_4F_8$ gas flow rates. The author leaves this as an exercise to the reader.

Fig I.20 Two silicon dioxide etches etched under similar conditions except ICP was 3100 W (left) as compared to 1100 W (right) with no significant change in undercut. This aspect demonstrates the protective nature of the polymer sidewall passivation.

It should be noted that only 4% of the total gas injected is oxygen. It was stated that oxygen is critical for scrubbing any carbons that might redeposit on the substrate. To determine if too much oxygen would prevent the passivation from occurring, etches were performed varying the oxygen flow rate while simultaneously etching similarly patterned silicon. Two aspects were looked at. First would the lower passivation allow for the silicon dioxide sidewalls to undercut? Second, would a reduction of carbon permit more fluorine to etch the silicon and/or retard the oxide etch rate? By varying the oxygen gas percentage to values of 0, 4.4%, 22.2%, and 44.4% the overwhelming answer to both questions was no. There was no relative undercut seen in any of the structures. The oxide and silicon etch rates were almost constant. What was seen, however, was the effect of micro masking. The 0% sample was very contaminated with oxide grass, to the level that finding a 5 micron area where no grass was present was very difficult.
Etch rates for silicon dioxide and silicon etched using the silicon dioxide etch while varying the oxygen flow rate. Note that no significant change was noticed but there was an observation of a large amount of oxide grass present when oxygen was missing.

As noted earlier, this etch closely resembles that of a CF₄ silicon dioxide etch. One of the biggest advantages is that this etch should demonstrate a higher silicon dioxide etch rate over that of silicon. To improve this selectivity it has been understood that if one can remove fluorine from the plasma, a higher selectivity between the oxide and silicon etch rates could be achieved. As a good solution to this problem, H₂ gas was injected to bond with the fluorine to create HF. This prospect seems applicable for C₄F₈ as well. However, work has been performed by Li et al. [5] showing that this selectivity can also be achieved by injection of Ar into the reactor achieving an increased oxide to silicon selectivity of 5:1.

Etch Applications
The silicon dioxide etch was utilized for several applications. First this etch was used to create nanoimprint molds. Specifically this oxide etch was first optimized and established to create circular grating distributed feedback dye lasers, Yan et al [20]. Using
a chrome etch mask, patterned using electron beam lithography, this oxide etch was used to etch into a silicon dioxide substrate 600 nm (approximately 100 seconds of etch time). The etch created circular ridges over a 200 micron area for use as a Bragg grating. The grating period was set to 410 nm with 282 nm wide ridges to match the 2\textsuperscript{nd} order Bragg reflection condition. The silicon dioxide mold was then used to nanoimprint into polydimethylsiloxane (PDMS). Silicon dioxide was needed since it offers high rigidity and stiffness required for the pressures seen during the imprinting process. This application is interesting in that it offers a method for creation of nanoimprint molds.

A second application for this silicon dioxide etch was for use as a decapitation step for selectively removing the oxide layer off of the top of a vertical silicon nanowires. The fabrication sequence and etches used to create said silicon nanowires will be detailed later in this thesis. Beginning with an array of vertical single crystal P\textsuperscript{+} silicon nanowires, etched 1234 nm high, oxygen plasma cleaning was performed to ensure the sample was free of resist and particles. After the cleaning, a dry thermal oxidation was performed at 1000 C for approximately 10 minutes to create an approximately 8-10 nm thick oxide. The range of pillar diameters was set from 40 nm up to several hundred nanometers. Upon
completion of the oxidation, a 20 second oxide etch was performed. This etch removed
the oxide layer off of the top of the pillar and the surface of the substrate leaving the pillar
sides with the oxide layer. The sidewall layer of oxide was required for use as an electrical
passivation layer in an attempt to improve the electrical conductivity of silicon nanowires.
From the aspect of etching, this fabrication sequence is interesting because it develops a
method for creating lateral oxidation layers potentially interesting for making a vertical FET
or gate all around FET.

![Cross sectional SEMs of the silicon nanowires etched 1.2 microns tall with a 10 nm thermal oxide around the side of the pillars. The silicon dioxide etch was used to remove the oxide layer from the top of the pillar (the darker circle on top) and the substrate surface. The left pillar is 100 nm in diameter and the right pillar is 300 nm in diameter.](image)

As a third application, this oxide etch was used to embed copper into etched quartz
wafers for fabrication of a planar copper microcoil. The interesting aspect of this
fabrication sequence is that realignment of a photoresist mask for metallization liftoff is
easily achieved. Beginning with a chrome patterned quartz wafer adhered to a silicon
carrier wafer using Fomblin, a silicon dioxide etch is performed. Due to the large ICP
power and the large thermal resistivity of the wafer, etch times should remain less than 15
minutes with 15 minute cooling down times before recommencing the etching. Etch times
much larger can result in large thermal stresses across the quartz and shatter the wafer
inside the ICP chamber. Approximately 200 nm of chrome mask will be consumed for every 15 minutes of etching and a remaining mask optically opaque is required for the subsequent steps, so planning ahead for the mask consumption is required. Upon achieving the desired etch depth, the wafer is removed from the chamber and cleaned in isopropyl alcohol. Photoresist is then spun on the top of the chrome and prebaked. The sample is then turned over, and a UV flood exposure is performed on the backside. This allows for the light to travel through the quartz and any resist behind the chrome etch mask is protected whereas as the resist that reached the etched trenches is exposed. Finally, the exposed wafer is developed and thermal evaporation is performed. Although metallization typically requires a liftoff mask 3 times thicker than the metal layer being deposited, in this instance metal layer many times thicker can actually be deposited. After liftoff has been performed, the etch mask is removed in chrome etchant. As a demonstration of this technique, a microcoil pattern was etched approximately 7.5 microns deep into a quartz wafer. Following the same fabrication sequence approximately 5.8 microns of copper was then thermally evaporated into the etched trenches.

Fig I.24  Cross sectional SEMs of planar copper microcoils embedded into an etch quartz wafer. The silicon dioxide etch was performed for 7.5 microns masked with chrome.
**Silicon Etch masks**

From the previous chapter, it was seen how the silicon etches mostly a chemical etch with very little milling action. What made the silicon etches so successful was the highly reactive binding between the fluorine and the silicon combined with the nonreactive passivation layers of SiOxFy and CF2. Much attention has been brought to calibrating the etch chemistries. However, all of this attention has overlooked one of the most key aspects of an etch, the etch mask itself. This chapter will describe several etch mask solutions beginning with what is commonly used and progressing to the several new etch masks.

**Etch Mask Requirements**

*The Etch Mask Problem*

For an etch mask to be successful, several basic requirements must be met [15]. First, the etch mask must have a removal technique that is orthogonal to the substrate. With resist and silicon as an example, this condition is met as Acetone can remove the etch mask yet not chemically attack silicon. This requirement is based on the idea that once a precision etch has been performed, using a chemical which alters the etched profile as it removes the etch mask severely limits the resolution of the patterning. Second, the etch mask must be resilient to the chemical etching performed in the ICPRIE. This fact derives from several aspects. Primarily, if the mask is has low selectivity, the ratio of the etch rate of the mask to the etch rate of the substrate, then a thicker mask must be used to achieve higher aspect ratio structures. Besides being more complex wet chemistry, thicker masks limit the resolution of the patterned structure. As an example, it is easier to pattern a 30 nm etch mask using a 30 nm thick layer than it is using a 1 micron
thick layer. This example is exactly why resists are sold with chemistry variations to allow for thinner layers for a given spin speed. Secondarily, if the etch mask is chemically etched, then the edge of the mask can be laterally etched inwards as the substrate is etched down and reduce pattern fidelity.

A third requirement for a good etch mask is resilience to milling. This idea is similar to chemical resilience but is separated for clarification. As seen in cryogenic etching, the chemical etch rate far surpasses the milling etch rate. For this reason, the selectivity of photoresist is dominated by the milling rate of the etch. While this is acceptable when a thick mask is available, it severely limits the etch depth of nanoscale structures when thin electron beam resists are used. A fourth requirement is that the etch mask should not interfere with the DC electric field established between the plasma and the table. For photoresist or silicon dioxide etch masks, this requirement is met. However, for metal etch masks, this requirement is not met.

Resists are often a good compromise of all the requirements with the biggest advantage being the ease of preparation. For the micron scale, photolithography using Clarion AZ 5214e can achieve structure size down to approximately 1 micron. For the nanoscale polymethylmethacrylate (PMMA) A2 was typically used for the work described in this thesis for patterning down to 20 nm. Recipes for fabrication using each of these are found in Appendix A.

Since the cryogenic etch is more appropriate for micron scale etching, the photoresist is used. However, cryogenic etching places further restrictions on the photoresist; it cannot be much more than 1.6 microns thick. In fact, a 1.6 micron thick resist on a fully coated 3” silicon wafer is the maximum thickness achievable when etching at -120 C.
Thermal stresses induced over a large surface area will place large cracks across the resist significantly reducing the fidelity of the pattern transfer. Oxford Instruments recommends only using resist thicknesses less than 1 micron. Thicker resists can be used but must have smaller surface areas; for example a wafer patterned with circles is less susceptible to cracking as compared to a wafer patterned with holes. The thickness limitation then sets a maximum achievable etch depth for a given forward power. Typical photoresist selectivity is around 100:1 which implies a maximum etch depth of around 100 um. It was stated earlier than the mask is chemically etched and milled and that the two effects are separable. Increasing the Fwd power increases the milling. In this case, increasing the oxygen flow increases the chemical etch. For the same range of oxygen variations, 2 to 8 sccm, a reduction of etch mask selectivity is seen from 130:1 to 80:1. Chemical etching is assumed since Fwd power, and DC bias, was constant. Further, since SF$_6$ flow rate and ICP power was held constant, the chemical etching was attributed to oxygen.

Fig II.1 Loss of photoresist selectivity for the cryogenic etch as oxygen is varied. The etch conditions were SF$_6$-70sccm, ICP-900W, Fwd-5W, temperature-(-120)C, and pressure of 10 milliTorr.
Etching on the nanoscale requires both the pseudo Bosch etch and nanoscale patterning. To achieve the patterning, electron beam lithography and PMMA is used. Unfortunately achievable selectivity is approximately 3:1 for low Fwd power etch conditions. Under higher Fwd power conditions this selectivity can drop to lower than 1:1. With such low selectivity, the most predominant etch problem becomes mask erosion. As the etch progresses deeper, the thinnest section of the mask begins to deteriorate; this region is the edge of the pattern. When the mask is etched away, the silicon beneath it is no longer protected and begins to etch. For this reason, the sidewalls on the nanoscale begin to develop an uncontrolled taper.

![Fig II.2 Cross sectional SEM of a pseudo Bosch etch of 30 nm (left) and 100 nm (right) silicon ridges masked using approximately 55 nm of PMMA. This etch was terminated before the onset of mask erosion at 256 nm.](image)

Another standard etch mask is silicon dioxide. This mask offers significantly higher selectivity for cryogenic etching, around 200:1, but with added complexity and specific problems. Silicon dioxide can be thermally grown on a silicon substrate or deposited by chemical vapor deposition (CVD). The difficulty lies in creation of thick etch masks, masks greater than 1 micron needed to achieve 200 micron deep silicon etches.
Furthermore, patterning such deep etch masks become difficult. Wet etching of silicon dioxide using hydrofluoric acid (HF) induces as much lateral undercut as it does vertical and dry etching requires a second patterning step using chrome etch mask. The advantage of using silicon dioxide is that removal and wet etching techniques do not chemically etch the silicon. Although dry etching is preferential to etching silicon dioxide over that of silicon, it does etch silicon at rates comparable to pseudo Bosch. For this reason, silicon dioxide etch masks are infrequently used.

**Undercutting with Metal Masks**

Metal etch masks are used since metals can be very chemically resilient, very hard to withstand milling, and very easy to pattern since only thin layers are needed. Further, metal etch masks can be removed using wet chemistry which will not affect the substrate; achieving the orthogonality requirement. A very good example of a metal used is chrome. Very thin layers are easily deposited using thermal evaporation or sputtering and can offer selectivity of 50:1 for silicon dioxide etches. Where metal fails to meet etch requirements is on the low Fwd power silicon etches. Metal etch masks protect the vertical sidewalls well but have a severe problem of undercutting. The exact nature of this undercut is unclear but a very good demonstration is as follows.

![Fig II.3](image)

Cross sectional SEM of a cryogenic etch of 10 (left), 20 (middle), and 50 (right) micron diameter silicon micropillars. The etched height was 30 microns and was
A chrome etch mask was thermally evaporated on silicon and patterned using photoresist and chrome etch. The pattern was the hexagonal pillar pattern, described earlier. Upon completion of a 30 micron deep cryogenic etch, the chrome mask was completely undercut. The 10 and 20 micron diameter pillars had their mask completely undercut and falling off and the 50 micron diameter had an undercut of approximately 15 microns radially. What is most surprising is that the silicon etch was very vertical and smooth. A second experiment with metal etch masks was performed using thermally evaporated copper patterned similarly to the chrome mask experiment. The difference between the two metals is that copper is about 10 times less resistive than that of chrome, 16.78 nano-Ohm-m and 125 nano-Ohm-m respectively. The copper masked silicon was etched 37 microns deep under similar etching conditions. Although the amount of lateral undercutting was comparable, the copper masked structure was hollowed out from the inside and left resembling a chalice as seen from the 20 and 50 micron diameter pillars.

Fig II.4  Cross sectional SEM of a cryogenic etch of 50 (left) and 20 (right) micron diameter silicon micropillars. The etched height was 37 microns and was masked with chrome. This etch demonstrates a failure of metal etch masks not seen with dielectric etch masks.
copper. This etch demonstrates a failure of metal etch masks not seen with dielectric etch masks.

The fact that dielectric masks such as silicon dioxide and photoresist do not undercut suggests that this problem could be attributed to electric field perturbation effects. Further, it is interesting to note that as the conductivity of the metal increases, so does the effect of the undercut. As previously stated, insertion of a metal plate into a DC and AC electric field can alter the boundary conditions. What is clear is that a mask undercut will occur using the cryogenic etch and the pseudo Bosch etch with metal masks, so an alternative is needed.

**Alumina Etch Mask**

Achieving high aspect ratio silicon nanostructures is rapidly becoming necessary [21]. In order to meet Moore’s Law, fabricating at the nanoscale is critical. Deviations in the etch much more than a nanometer can result in process failure. It is the author’s vision that predicts that silicon will be required to be built vertical to maintain the current drive to higher transistor count per wafer [22]. Bottom-up processing already has the ability to grow long silicon nanowires with smooth sidewalls. Where this technology is challenged is that precision placement is difficult. This is not acceptable in current CMOS fabrication facilities. Top-down processing will need to create silicon structures similar to that achieved by bottom-up but using tools and material currently integrated in industrial facilities. It would be interesting to ask a Fab manager if gold could be introduced into a CMOS Fab line in order to grow silicon nanowires.

Novel nanoscale etching has been very close to achieving the needed nanostructures. With the invention of passivated silicon etching, such as the cryogenic or pseudo Bosch etch, smooth vertical sidewalls are achievable [23]. Using extreme UV lithography or
electron beam lithography nanoscale patterning is also achievable [24]. What has been missing is an etch mask which meets all four of the requirements needed: orthogonal mask etching chemistry from that of the silicon, chemical resilience to fluorinated silicon etches, milling resilience, and electrically insulating [25].

For these reasons, the aluminum oxide (alumina) etch mask was invented. It was hypothesized that since alumina is non-conductive, electric field effects would not be present unlike metal masks. Since alumina is hard, it was expected that it should be resilient to milling. Further, if fluorine were to bond it would create a nonvolatile AlₓFᵧ or AlFₓOᵧ compound which would remain; essentially it would be resilient to fluorine chemical etch. Finally, since alumina is more glass like than metal, it was predicted that patterning and liftoff would be easier than with metal. On all these points alumina was successful. What was unexpected was the alumina mask removal chemistry. After etching alumina was discovered to be removed using Buffered HF, albeit at a very slow rate. But what was advantageous was that BHF does not etch silicon [26]. So the idea of orthogonality between etch chemistry of silicon and alumina was realized with this as an etch mask.

Since the ammonium in BHF was what etched the alumina, it was quickly realized that ammonium hydroxide and hydrogen peroxide would much more efficiently etch the alumina. This combination is referred to in industry as RCA 1 clean and is used for cleaning silicon during wafer fabrication. In one discovery, alumina enabled high aspect ratio silicon nanostructures to become compatible with mainline semiconductor fabrication lines.

This section of the chapter will detail fabrication processes of the alumina etch mask for microscale and nanoscale silicon structures. It will detail the patterning, etching, and
removal process and describe the results of using the mask with the cryogenic etch and the pseudo Bosch silicon etch.

**Mask Fabrication Sequence**

As stated earlier, both photoresist and cryogenic etching are most suitable for the microscale. The alumina etch mask integrates well with these two processes. To demonstrate a possible fabrication sequence, micropillars and micro-holes, identical to the hexagonal pillar pattern described previously, were fabricated. Using the AZ 5214e resist, a 1.6 micron thick patterning of holes and circles with diameters 5, 10, 20, and 50 microns were defined on both P and N type <100> silicon wafers. Patterning using this resist is detailed in Appendix A. For the nanoscale, it was more appropriate to use PMMA electron beam resist and pseudo Bosch etching. Nanoscale patterning was performed in 75 nm thick resist. The patterns consisted of hexagonally packed arrays with pillar separation double the diameter and square array rows of pillars with decreasing diameters. The square arrays were marked with 5 to 20 micron diameter pillars at the corners of the arrays. The patterns were defined using a Leica EBPG with a 100kV electron beam. Again, both P an N <100> silicon was used.

Alumina was then sputtered on the patterned resist. Sputtering of alumina offers the advantage of low temperature deposition with the disadvantage that step coverage is very good. Sputtering was performed using a TES 1800 DC magnetron sputter system, using a 99.995% aluminum target and a 5:1 mixture of argon to oxygen as the process gas. This ratio of gases allows for the aluminum to be sputtered without poisoning the target while still deposits a stoichiometric aluminum oxide. Specifically, the sputtering parameters are as follows: 100 sccm of Ar, 20 sccm of O₂, pressure of 10 to 15 mTorr, and 400 W of DC power. Lower sputtering power can be used but reduces the sputter rate of approximately
10 nm per minute. An aluminum target was used for multiple reasons. Primarily, the heat generated on the target does not crack an aluminum target like an alumina target; this is due to the increased thermal conductivity of aluminum over alumina. Secondary is that aluminum targets are significantly less expensive than alumina targets.

Liftoff is then conducted using Acetone. Placing the sample in a beaker, liftoff is achieved on timescales of minutes. Adhesion between the silicon and alumina is very good and permits light scrubbing using Q-tips or cotton swabs. At this point, all that remains on the silicon substrate is the patterned alumina. If further cleaning is needed, a low milling oxygen plasma can be implemented to clean the structure. The patterned sample is now ready for silicon etching.

Fig II.5  SEM of 5 micron diameter alumina etch mask on silicon after liftoff.

Micropillar and Nanopillar Etching

Micropillars were etched using a cryogenic etch modified slightly to achieve high aspect ratio structures. The adjustments are as follows:
Using this chemistry DC bias was 91 V, $E_0=0.9843$, and $b=0.02808$ with the two coefficients calculated with an R-square value of 0.9946. Comparing this set of parameters with previously stated, it should be noted that $E_0$ decreased as well as $b$. Fundamentally, by increasing the oxygen and temperature the passivation increased which overall slowed the etch rate down 1.14 microns per minute to 0.98 microns per minute. Interpretation of $b$ as the slowing of the etch rate due to aspect ratio, and measuring the aspect ratio dependence as a ratio of $b$ to $E_0$, shows the change of 3.6% to 2.85%. The dependence reduction is attributed to the increased Fwd power.

Fig II.6 Cryogenic etch data for various aspect ratios of silicon micropillars. The data was width normalized to solve for the $E$ and $b$ coefficients.
The alumina etch mask used was 110 nm thick and the highest pillar etch was 143.7 microns tall for a 50 micron diameter pillar. With some resist mask remaining this yielded a minimum selectivity of 1306:1. The milling rate on the alumina mask was approximated to less than 0.75 nm per minute given an etch time of 140 minutes. Measurements were taken in a FEI tools Quanta SEM. Trench aspect ratios of the 5, 10 and 20 micron diameter pillars were 25.3, 12.0, and 7.4 respectively. It should be noted that the edges of the mask began to fail as evident by the etched marks at the top of the pillars. The next etch in this sequence for 160 minutes resulted in complete mask erosion. It should also be noted that very little re-deposition of the alumina mask occurs since very little black silicon is present.

Fig II.7 Cross sectional SEM of a cryogenic etch of 5 micron diameter silicon micropillars. The etched height was 83 microns. The alumina mask was approximately 110 nm thick.
Fig II.8 Cross sectional SEM of a cryogenic etch of 10 (left) and 20 (right) micron diameter silicon micropillars. The etched height was 103 and 126 microns respectively. The alumina mask was approximately 110 nm thick.

Fig II.9 Cross sectional SEM of a cryogenic etch of 20 micron diameter silicon micropillars. The etched height was 30 microns. The alumina mask was approximately 30 nm thick for a selectivity of 1000:1.

By reversal of the same resist from positive to negative, holes in an identical pattern as that of the pillars was also etched. Etch conditions were again slightly altered with a
decrease in Fwd power to 10 W and etched for 1 hour. The alumina etch mask was deposited for 2 minutes for an approximately 20 nm thick mask. The 5 micron diameter holes were etched 41 microns deep and the 20 nm holes were etched 64 nm deep. This yields a selectivity of approximately 3200:1. The hourglass like shape at the top of the 5 micron holes is attributed to cleaving the holes off center.

Fig II.10 Cross sectional SEM of a cryogenic etch of 5 (left) and 20 (right) micron diameter silicon holes. The etched height was 41 and 64 microns respectively. The alumina mask was approximately 20 nm thick.

To create the silicon nanopillars, the pseudo Bosch etch was employed since the etch rate was significantly slower and more controlled. The etch used is as follows:

<table>
<thead>
<tr>
<th>SF₆</th>
<th>33 sccm</th>
<th>ICP Power</th>
<th>1200 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>C₄F₈</td>
<td>57 sccm</td>
<td>Fwd Power</td>
<td>20 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>15 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

Using this etch, silicon nanopillars and nanowires were fabricated down to 20 nm diameters and pillar aspect ratios over 60:1. The etch rate for these etch conditions
yielded an etch rate of approximately 300 nm per minute. Error bars indicate the range of etch heights over all the trench aspect ratios over the etch. Changes in the fwd power do have dramatic changes in the etch rate, however, so caution should be taken when varying conditions.

![Etch Rate Graph](image)

Fig II.11  Pseudo Bosch etch data averaged over all the aspect ratios of silicon nanopillars.

As a first example of the quality achievable with the mask, rows of 40 and 65 nm pillars were etched 3 minutes to 780 nm heights. The pillars were hexagonally packed and spaced at twice the diameter. As a second example to demonstrate the improvement of alumina etch masks over masks such as nickel, an experiment was performed using both etch masks under identical etch conditions described above. Approximately 80 nm diameter pillars arranged in a hexagonal packed array were etched to similar heights. What should be noticed is that the tops of the pillars are dramatically different. The nickel etch masked pillars have sharp point and severe undercutting where as the alumina etch masked pillars have flat smooth tops with little to no undercutting.
Fig II.12  Cross sectional SEM of a pseudo Bosch etch of silicon nanopillars. The pillar diameters alternated between 40 and 65 nm and were etched 780 nm tall. The alumina etch mask used was 30 nanometers thick.

Fig II.13  Demonstration of the difference between a nickel etch mask (left) and alumina etch mask (right). Cross sectional image of approximately 80 nm diameter pillars etched to 970 nm (left) and 780 nm (right). The etch conditions were identical. Note the mask undercut problems of the nickel mask are not present on the alumina etch mask.

To measure the surface roughness of the etched sidewalls, bright field reflection electron microscopy was performed on the nanopillars. By mounting the silicon nanopillars sideways in a FEI TEM, the sample could be imaged without removing it from
the substrate. The images taken display notching of less than 5 nm and with the peak surface roughness approximately a few nanometers.

Fig II.14 Bright field reflection microscopy of a 100 nm diameter pillar taken in a FEI transmission electron microscope. The pillar was etched using the pseudo Bosch silicon etch and masked using alumina. Not the image is rotated approximately 60 degrees.

Although the previous pillar pattern was useful in characterizing the etch mask and etch, separation of the pillars was desired for mechanical and electrical characterization. For characterization, the pillars were separated by 5 micron with rows which descended in sizes from approximately 420 nm diameters down to 20 nm in diameter in 40 nm increments and back up to 180 nm diameters in 20 nm increments with 14 pillars in each row. The arrays had 20 micron diameter pillars located on the edges of the array to serve as markers. Using this array, silicon nanowires with aspect ratios greater than 60:1 and with diameters down to 20 nm were fabricated using this top-down method. As an example, a 57 nm nanowire was etched 2.54 microns high with a positive taper of 90.6 degrees and an aspect ratio of 45:1. This patterning permitted testing of pillars with identical heights but varying diameters; for example a sample with 52 nm, 114 nm, 152 nm, and 206 nm diameter pillars etched 2.1 microns in length.
Fig II.15  SEM of alumina masked nanopillar array etched 2.75 microns tall. The diameters in the array started at approximately 420 nm and cascaded down to 20 nm and then back up to 180 nm. The pillars were etched for 10 minutes and had 30 nm thick alumina etch mask.

Fig II.16  SEM of alumina masked nanowire etched 2.54 microns tall and is 57 nm in diameter; the etch angle is approximately 90.6 degrees. SEM of alumina masked silicon nanopillars, with diameters of approximately 50, 110, 150, 200 nm, etched 2.1 microns tall.

Alumina Mask Evaluation

To verify that the film deposited was not aluminum but rather alumina, several tests were performed. First, DC resistance measurements were performed and demonstrated very high resistivity; counter to what is expected from the conductive aluminum. Second,
stoichiometry of the sputtered alumina was determined using energy dispersive X-ray spectroscopy (EDX). Analysis of the spectrum indicates that the etch mask is within 0.6% of stoichiometric alumina with a ratio of oxygen to aluminum very nearly 3:2. Although it is not a qualitative test, comparison between the nickel and alumina etch mask demonstrated that the alumina mask does not seem to be as conductive as the nickel.

Fig II.17  EDAX measurement of the sputtered alumina film. The peaks are centered around Oxygen, Aluminum, and Silicon with a ratio of nearly 3:2 of Oxygen to Aluminum; the same as stoichiometric alumina.

The most significant advantage of using this mask for fluorinated silicon etch chemistries is the achievable selectivity. For the cryogenic etch a 20 nm thick alumina mask is used to etch more than 64 microns into the silicon wafer before mask erosion begins. From this etch a lower bound on the alumina to silicon selectivity of over 3200:1. As a further demonstration of the resiliency of the etch mask, 300 nm of alumina is used to etch 50 micron diameter holes through a 350 micron wafer. A 110 nm thick alumina mask
began to erode after 160 minutes of cryogenic etching using 20 Watts of Fwd power; the 50 micron diameter pillar final etch height was 126 microns. This selectivity is a significant improvement over photo resist’s selectivity of approximately 100:1; a factor of 32 improvement.

For the Pseudo Bosch etch chemistry, typical values of selectivity for PMMA are 5:1. Using an alumina etch mask of 30 nm, nanoscale pillars were etched to heights of 2.75 microns yielding a selectivity of better than 91:1. This is a factor of 18 in improvement.

**Focused Ion Beam Implanted Gallium Etch Masks**

Creating top-down fabricated nanoscale structures has predominantly required electron beam lithography patterning of resist to define the structure. This method requires a planar surface so that the resist may be planarized by spinning. Once the pattern is spun it is patterned using an electron beam, either from a modified SEM or an EBPG. After writing, the resist is chemically developed in a solution that removes the cross linked resist leaving a patterned substrate. Upon completion of the fabrication sequence, such as ICP etching, the etch mask needs to be removed by either oxygen plasma or wet chemistry. This fabrication sequence is troublesome for multiple reasons. First the requirement of a planar surface severely restricts when this step may occur. For example, re-patterning of etched silicon is extremely difficult and time consuming. Second, this patterning technique requires the use of wet chemistry which always leaves a chemical residue and can limit the structures achievable. As an example of this, wet chemistry involving nanowires typically leaves the wires sticking together due to surface forces. Furthermore, wet chemistry inevitably requires more chemical waste; a current ecological problem.
When fluorine or oxygen chemically bonds to gallium, it forms a nonvolatile GaFₓ or GaOₓ respectively. This property enables the Ga implantation to act as a fluorine or oxygen etch mask. This aspect has been explored for wet etching of silicon using potassium hydroxide (KOH) and HF; the mask demonstrated chemical etch resistance. This etch resistance was explored for use as an ICP etch mask. To pattern the Ga mask, a Focused Ion Beam was used to implant the Ga with resolution to better than 30 nm. This chapter describes the implantation and etches viable using this concept enabling a dry lithography.

Admittedly, this technique produces extreme damage to silicon. However a significant amount of work and time has been spent understanding the damage and methods to repair. Although this work is outside of the scope of this thesis, a very good list of references can be found from the SRIM and TRIM website. Finally, it should be emphasized that the technique of implanting ions as an etch mask is not limited to Ga and Si. This method can be extended to SiO₂, diamond, graphite, carbon nanotube, etc. The critical idea is that the implanted ion and the etching ions need to form a nonvolatile compound under ICP etch conditions which favor chemical etching over milling.

*Ga Implantation using a FIB*

One alternative has been a combination of patterning and etching using a Focused Ion Beam, FIB. A FIB draws atoms from either a precursor gas or liquid, ionized the gas, accelerates the ion using a voltage potential, and then collimates the beam of ions. Deflection of the beam using either magnetic or electrostatic lenses permits precision control over beams. The achievable beam waists and control over the beams trajectory have been reduced down to a few nanometers. The method of accelerating and control of these ion beams is akin to electron beam control used in SEMs or EBPGs. By changing
the dwell time or the beam current the amount of ions driven to a sample can be modified. Many FIB’s utilize an ion beam of Gallium, Ga, electrostatically pulled from a liquid metal source. When this beam is applied to substrates such as silicon, silicon dioxide, silicon dioxide or metal, the impact of the Ga ion can remove substrate atoms. This is referred to as milling. If the energy of the impact, or number or impacts, is not enough to remove the substrate the ion is said to have been implanted in the substrate. Implantation is similar to a meteor crashing into earth, if the size and velocity of the meteor is small enough, the meteor will continue to bury itself in the earth until it comes to a stop. The trajectory path is filled with damaged and disarray. This is analogous to what occurs with silicon. The Ga atom can travel into the silicon substrate, leaving amorphous silicon in its wake, and come to rest at a given location in the silicon. By controlling where these impacts occur, the energy of the impacts, and the number of impacts occurring, a Ga layer in the silicon can be defined. This patterned Ga layer can then be used to protect the silicon below it from other impacting ions of lesser energy and from chemical reactions. This is the basis of the implanted Ga etch mask.

Patterning of the Ga etch mask was accomplished using the dual beam Nova FIB/SEM by FEI. A cleaned silicon sample is placed at the eucentric height and rotated such that the ion beam strikes perpendicular to the substrate surface. For a selected beam current, the Ga⁺ beam is focused at the edge of the substrate. Automated write programs specifying the pattern and dwell times are then executed to raster the ion beam. In a manner analogous to a scanning electron microscope, the FIB accelerates the Ga⁺ ions to the surface of the silicon substrate using various accelerating beam voltages. The magnitude of the beam voltage controls both the implantation depth and the thickness of the Ga layer.
Fig II.18 Ga⁺ implantation depth for varying FIB beam voltages as simulated using TRIM. The etch mask thickness is approximated by 2 times the straggle length.

To estimate the effect of the beam voltage on the thickness of the implantation layer and implantation depth, simulations using Stopping and Range of Ions in Matter (SRIM/TRIM) were performed for implanting Ga⁺ ions into silicon [27]. The results are summarized above; the vertical straggle length of the implantation is used to approximate the thickness of the Ga-implanted layer for the purpose of effective selectivity calculations. For the implantation patterning performed, a 30 kV beam voltage was used. From the implantation simulations of 30 kV beams, an approximation can be made that the implantation damage was to the top 15 nm of silicon, creating amorphous silicon, and the next 20 nm below as a Ga rich amorphous silicon layer, consistent with TEM measurements [28].

To investigate patterning over the entire nanometer length scale, three sets of patterns were generated. To measure the nanometer range, patterned squares were used starting
at 500 nm and ending at 50 nm stepped in 50 nm increments. The dose columns began at $5.3 \times 10^{15}$ cm$^{-2}$ and ended in $1.96 \times 10^{17}$ cm$^{-2}$ with the dose stepped in approximately $1 \times 10^{16}$ cm$^{-2}$ increments. To determine sub 200 nm resolution, patterned squares were again used starting at 200 nm and ending at 20 nm stepped in 20 nm increments. The third pattern arrays were circles starting at 100 nm in diameter and ending at 10 nm in diameter stepped in 10 nm increments. Both the second and third pattern arrays, the dose column began with $1.25 \times 10^{16}$ cm$^{-2}$ and ended in $1.25 \times 10^{17}$ cm$^{-2}$ with the dose stepped in approximately $1.25 \times 10^{16}$ cm$^{-2}$ increments using a measured 6.87 pA beam.

For the micron scaled structures we created dose arrays of 5 micron by 5 micron squares separated by approximately 10 microns. Each square dose was varied by incrementing the write time 2 second. With the beam current at 100 pA, this provided a dose step of $5 \times 10^{16}$ cm$^{-2}$. The dose array began at $1 \times 10^{16}$ cm$^{-2}$ and stopped at $5 \times 10^{16}$ cm$^{-2}$. After implantation, verification of the patterning can be seen using a scanning electron microscope (SEM).

**Silicon Etching**

**Pseudo Bosch Silicon Etching**

Investigation into the potential for nanoscale patterning utilized the pseudo Bosch etch for reasons mentioned earlier. As a verification that the type and amount of doping in silicon wafers was unimportant, several different Si samples were used, N-doped <100> rho=1-10 Ohm-cm and P-doped <100> rho=0.005 Ohm-cm. Patterned samples were placed on a 6 inch silicon carrier wafer using Fomblin oil as an adhesive and thermal conductor. The first dose array was etched under the following conditions:
<p>| | | | |</p>
<table>
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<tr>
<td>SF$_6$</td>
<td>33 sccm</td>
<td>ICP Power</td>
<td>1200 W</td>
</tr>
<tr>
<td>C$_4$F$_8$</td>
<td>50 sccm</td>
<td>Fwd Power</td>
<td>10 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>15 C</td>
<td>Pressure</td>
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This etch chemistry had a measured forward bias of 54 volts. The second and third dose arrays were etched under identical etching conditions as before, except Fwd power was increased to 15 W and the C$_4$F$_8$ gas was increased to 68 sccm; this modification improved pattern fidelity for sub 100 nm structures. Upon completion of etching, the Fomblin was removed using IPA and the sample imaged using either the FEI Nova 600 or a FEI Sirion SEM.

Fig II.19 Scanning electron micrograph of a dose array for nanoscale SF$_6$/C$_4$F$_8$ etch. Etch depth was 460 nm with the squares ranging from 500 nm down to 50 nm in 50 nm increments. Inset is a scanning electron micrograph of Ga implanted nanoscale dose array in silicon. The large square was where the ion beam was focused and used as a visual marker.
Dose arrays of 50nm to 500nm squares were etched for different times so that etch rate, minimum dose for a required depth, the critical dose, and minimum structure size could be ascertained. Samples were inspected in SEM to determine the time and height of each structure. The results of these measurements were compiled into the critical dose array. Two features of this graph are important to notice. First, no measurable masking occurs below a particular dose, termed here as the threshold dose. Next, the height of failure displays an approximately linear relationship with the areal dose.

Motivated by this apparent structure, the data was fit with the following equation:

Fig II.20 Ga dose array; the dose required for a given etch depth for the Pseudo Bosch silicon etch. The diagonal line describes the minimum dose required for achieving a desired etch depth. Area to the right of the diagonal line, the dosed structures were successfully masked. Etch mask selectivity is determined by dividing the etch depth by the Ga mask thickness of 20 nm.
\[ h_{\text{critical}} = \frac{k_{\text{etch}}}{k_{\text{erosion}}} \ast (d_{\text{critical}} - d_{\text{threshold}}) \]

Where \( h_{\text{critical}} \) is the height of the etched structure at failure, \( k_{\text{etch}} \) is the experimentally measured etch rate, \( d_{\text{critical}} \) is the measured dose from FIB implantation of the failed structure, and \( k_{\text{erosion}} \) and \( d_{\text{threshold}} \) are the effective erosion rate of the mask and the threshold dose treated as free parameters to be determined by a least squares fit to the data. The etch rate, \( k_{\text{etch}} \) was determined to be 186 nm/min for the P-doped silicon samples. For the pseudo Bosch data, the fit yields the following fit parameters:

\[ h_{\text{critical}} = \frac{0.186 \text{[um/min]}}{2.45 \times 10^{16} \text{[ions \cdot cm^{-2} \cdot min^{-1}]} \ast (d_{\text{critical}} - 1.85 \times 10^{16} \text{[ions \cdot cm^{-2}]})) \]

Since the implantation thickness was approximated as 20 nm, the selectivity of the mask improves as the areal dose increases (increasing the density of the Ga mask) and is also described using equation 1 by dividing the etch height by the mask thickness of 20 nm. Although the etch damage is approximated to be the 15 nanometers of amorphous silicon on the top of the etch mask, it should be noted that surface remains notably smooth. The first dose array demonstrates that this masking technique can create, at the minimum write pattern of 50 nm, a 72 nm diameter nanopillars and 800 nm tall with sidewall and roughness of less than 5 nm. Although the patterned size was originally 50 nm, the increase in size to 72 nm is consistent to SEM resolution and SRIM calculations of having a lateral straggle length of 7.2 nm. Other contributions to the mask size increase can be attributed to several factors including approximation of the beam as Gaussian and the ion beam being slightly defocused. The lateral straggle was determined as being the
most significant of all the contributions at this beam voltage. Resolution and
categorization of the Ga beam width will be discussed later [29][30][31][32].

Fig II.21  Scanning electron micrograph of a silicon nanopillar, 72 nm in diameter and 800 nm
tall.

To investigate the minimum structure size, the second and third dose array was
employed. The second dose array consisted of squares etched 448 nm tall. The
minimum pattern etched was a 43 nm square with an aspect ratio of 10:1. Although a 20
nm square was implanted, the SEM shows only a mound where the pattern began to etch
but ultimately failed, possibly due to a lower Ga\(^+\) concentration caused by imperfect
focusing. It is also clear that the minimum dose of \(1.25\times10^{16} \text{ cm}^{-2}\) was not sufficient to
protect the silicon much greater than 70 nm.
Fig II.22 Scanning electron micrograph of second dose array for nanoscale SF$_6$/C$_4$F$_8$ etch. Etch depth was 448 nm with the squares ranging from 200 nm down to 20 nm in 20 nm increments.

The third dose array patterns were circles for vertical silicon nanowire fabrication and were etched simultaneously with the second dose array pattern. The minimum pattern etched was the 31 nm diameter pillar. The etch was reentrant at 89.15 degrees causing the base of the pillar to be at an 18 nm diameter. Although it is clear that significant masking occurred for the 20 nm pattern, the reentrant angle did not permit the structure to withstand the etch. Important to note is the higher fidelity of this patterning as compared to previous demonstrations.
Fig II.23  Scanning electron micrograph of third dose array for nanoscale SF$_6$/C$_4$F$_8$ etch. Etch depth was 448 nm with the pillars ranging from 100 nm down to 10 nm diameters in 10 nm increments.

This etch attained a very high selectivity with no oxygen in the etch chemistry. This is contrary to the masking mechanism of GaO$_x$ forming at the surface proposed elsewhere [33]. Formation of a GaO$_x$ layer during sample exposure to ambient is also excluded due to the 28nm implantation depth. This leads us to hypothesize another masking mechanism. Fluorine can bond with the Ga to create an involatile GaFx mask, which may also contribute to further physical sputtering resistance. This is consistent with previous results using reactive ion etching with SF$_6$ which relies on F$^+$ ions for etching [33,34,35].

*Cryogenic Silicon Etching*

Using the same etching system and mounting techniques as the nanoscale etch, micron sized features were also etched to determine the etch rate and threshold dose for a required depth. The cryogenic etch was employed for this scale. The etch conditions used are as follows:

| SF$_6$ | 70 sccm | ICP Power | 900 W |
This etch chemistry had a measured DC bias of 54 volts. The cryogenic dose array, described earlier, was etched for etch times of 1, 3, 10, 20 and 40 minutes with a measured etch rate, $k_{\text{etch}}$, of 1.03 microns per minute; the results compiled in the cryogenic critical dose array.

![Critical Dose for Ga Implantation and Cryogenic Etch](image)

**Fig II.24** Ga dose array; the dose required for a given etch depth for the Cryogenic silicon etch. The diagonal line describes the minimum dose required for achieving a desired etch depth. Area to the right of the diagonal line, the dosed structures were successfully masked. Etch mask selectivity is determined by dividing the etch depth by the Ga mask thickness of 20 nm.

The Fwd power, and subsequently the bias voltage, was intentionally set to match that of the pseudo Bosch etch with the other etching parameters set to optimize the etch. Although the ICP and gas chemistry changes the plasma density, matching the bias...
voltages allows for the milling aspect of the two etch chemistries to be more closely compared.

$$h_{critical} = \frac{1.03 \left[ \frac{\mu m}{min} \right]}{0.06736 \cdot 10^{16} \left[ \frac{ions \cdot cm^{-2}}{min} \right]} \cdot (d_{critical} - 2.2 \cdot 10^{16} [ions \cdot cm^{-2}])$$

Interestingly, $d_{threshold}$ is nearly the same for both etch chemistries ($2.2 \cdot 10^{16}$ ions*cm$^{-2}$ as compared to $1.85 \cdot 10^{16}$ ions*cm$^{-2}$), while $k_{erosion}$ for the cryogenic etch is nearly two orders of magnitude lower than for pseudo Bosch. This threshold dose, etched with 10 W of Fwd power, is consistent to that reported by Chekurov et al. [34] whom etched with 2-3 W of Fwd power and with an etch rate approximately double of that reported here.

Fig II.25 Scanning electron micrograph of a dose array the cryogenic etch. Etch depth was 10.1 μm with 5 μm squares. The dose was varied in this array from $1 \times 10^{16}$ cm$^{-2}$ to $5 \times 10^{16}$ cm$^{-2}$ in $0.5 \times 10^{16}$ cm$^{-2}$ increments.
To compare the fidelity of the pseudo Bosch etch to that of the cryogenic, a smaller feature size pseudo Bosch dose array pattern was cryogenically etched for 1 minute (approximately 1 micron). The minimum resolvable feature was a 350 nm square mask with the pillar body 200 nm at its widest spot.

Fig II.26 Scanning Electron Micrograph of Ga masked silicon squares, cryogenically etched 1 micron tall, to quantify the mask undercut associated with cryogenic etching. The pattern etched is identical to that used for the pseudo Bosch dose array.

To investigate if the FIB beam accelerating voltage affected the threshold dose, a 6 by 4 array of Ga implanted 5 μm by 10 μm rectangles was patterned. The beam voltages sampled were 5, 10, 20, and 30 kV written with beam currents of 120 pA, 50 pA, 81 pA, and 100 pA respectively. Beam currents were selected to match implantation rates to as close as allowed by the FIB’s settings. Each dose array started approximately at $0.375 \times 10^{16} \text{ cm}^{-2}$ with the next higher dose value doubling that of the previous up to approximately $13 \times 10^{16} \text{ cm}^{-2}$. Two samples were then etched to etch heights of 10.2 μm.
and 20.1 μm under the same conditions as before but with a reduced Fwd power of 3 W. Reduction of the Fwd power increased the slope of the dose array, maximizing etch mask selectivity, to amplify any etch height changes due to beam voltage. A failure of the etch mask during cryogenic etching rapidly destroys the structure, so for this experiment a loss of etch mask denoted a failure. For the 10.2 μm etch, the 5, 10, 20 and 30 kV structures required a minimum dose of $2.1 \times 10^{16}$ cm$^{-2}$, $1.6 \times 10^{16}$ cm$^{-2}$, $1.6 \times 10^{16}$ cm$^{-2}$ and $0.75 \times 10^{16}$ cm$^{-2}$ respectively. For the 20.1 μm etch, the 5, 10, 20 and 30 kV structures required a minimum dose of $2.1 \times 10^{16}$ cm$^{-2}$, $1.6 \times 10^{16}$ cm$^{-2}$, $0.8 \times 10^{16}$ cm$^{-2}$ and $1.6 \times 10^{16}$ cm$^{-2}$ respectively. There is a possible trend of slightly improved masking ability for higher beam voltages. Different accelerating voltages do result in different ion straggles and thus different effective Ga layer thicknesses, an etch mask thickness increase due to beam voltage increase. Although this experiment requires more data for clarification of how the masking mechanism depends on the implantation voltage, from this we concluded that if beam voltage did affect the critical dose, it would be by an acceptable value of less than $1.35 \times 10^{16}$ cm$^{-2}$ for a 5 to 30 kV beam voltage shift with a previously determined threshold dose of $2.2 \times 10^{16}$ cm$^{-2}$.

**Multilevel and Grayscale Lithography**

One of the most significant advantages of using Ga implanted etch masks is that unlike photolithography, which requires a planar surface for effective spin coating and exposure, the FIB can pattern non-planar structures. A second advantage of Ga masking is the linear relationship of etch depth to dose beyond the threshold dose. Utilizing these two advantages, we demonstrate the feasibility of three dimensional structures in silicon using multiexposure and grayscale etch masking.
Since the Ga beam does not require a polymer resist in which to define a pattern, one may perform multiple implantations for etch masking regardless of sample surface topography. Experimentally, this fabrication procedure proceeds as follows: implant initial mask, etch the silicon, implant second pattern, and etch the silicon. This repeating sequence can continue for as long at the Ga etch mask remains. Re-implantation of previous structures can also extend the critical height for these structures.

This technique was demonstrated using a mixture of both the pseudo Bosch and the cryogenic etch to create a suspended silicon nanowire connected to two pads. First, two 10 micron diameter circles separated by 10 microns were Ga implanted at a dose of $2 \times 10^{17} \text{ cm}^{-2}$. The structure was then etched to a height of 0.5 microns using the pseudo Bosch etch. A Ga mask was then implanted in the shape of a rectangle connecting the two pillars with the same dose as the circles. A mask undercutting cryogenic etch was then performed for an etch height of 5 microns; this step utilized the undercut to remove all unmasked silicon below the rectangle. The resulting structure was an 80 nm by 20 nm silicon nanowire suspended between two 10 μm diameter pillars etched 5 μm tall with the nanowire connected half a micron below the pillar tops. This technique utilized the advantages of each etch, the high pattern fidelity of the pseudo Bosch etch and the inherent undercutting and high selectivity of the cryogenic etch.
A second applicable technique is the creation of graded structures which utilizes the observation of the etch depth's linear dependence on the critical dose. Here, the structures are dosed to different critical doses and etched to the desired height. At the heights corresponding to their critical dose the structures will then start to etch at the same rate as the substrate, in a manner similar in principle to grayscale lithography [32,36]. These implanted structures can then be etched to create sloped features such as blazed gratings and optical lenses. This idea was demonstrated using nine 5 micron squares arranged in a row. Each square’s dose was increased approximately 2.5*10^{16} cm^{-2} more than it neighbor square for a dose ranging from 2.5 - 22.5 *10^{16} cm^{-2} and etched using the pseudo Bosch etch. This created a stair step set of platforms.
Fig II.28 Scanning electron micrograph 5 μm squares with varied doses. When the etch depth increases over the critical dose depth, the structure begins to etch but maintains its relative height to its neighbor.

Resolution limitations and masking mechanism

The theoretical limit to the highest resolution structures is highly dependent on the beam spot size and the accelerating beam voltage. These two parameters define the effective implantation masking area, as the spot size establishes the kernel to be convolved with the desired dose profile and the accelerating voltage determines the further spread of ions after interacting with the silicon. For the FIBs at Caltech, a theoretical resolution limit can be estimated by summing these dimensions in quadrature [30]:

$$d_{\text{system}}^2 = d_{\text{spot}}^2 + d_{\text{ion}}^2$$

For the minimum spot size $d_{\text{spot}}=5$ nm and lateral ion spread at 5 kV $d_{\text{ion}}=3.2$ nm $+1.8$ nm (1 sigma straggle), resulting is $d_{\text{system}} = 7.07$ nm. For these experiments at 30 kV, $d_{\text{ion}}=9.9+5.6$ nm, resulting in $d_{\text{system}} = 16.2$ nm, as compared to the minimum realized...
structure of 43 nm. This analysis does not take into account any excess resolution loss from deflection error, exposure scheme (amount of overlap between shots was 50%), defocus, or other experimental parameters which may account for the measured minimum [29,37].

To achieve the greatest etch depths, and hence highest selectivity, the amount of Ga present in the top layer should be maximized. However, further exposure of the beam past a certain dwell time leads to a steady state where the influx of Ga\(^+\) is balanced by the sputtered Ga. The amount of Ga present in the silicon sample, areal dose, as a function of total ion flux for a 30kV beam is seen below. This is approximated from the total flux of Ga atoms minus the sputtered Ga atoms, using the composition-dependent sputter yield computed by Monte Carlo simulation [38].

![Image of graph showing implanted dose as a function of incident dose]

Fig II.29  Plot of implanted dose as a function of incident dose, with limiting value is 3*10\(^{17}\) Ga atoms-cm\(^{-2}\).

As expected, for low doses the areal dose implanted is linear with total flux, as the sputtered material has a relatively low concentration of Ga relative to the amount
implanted. However, as the sputtered depth approaches the mean implantation depth of 27 nm, the total concentration of Ga in the sputtered material increases. By 28.4 nm, the areal concentration is $10^{17}$ Ga atoms-cm$^{-2}$, which is lower than total incident flux by 16%. The Ga sputter yield rapidly increases from this point, requiring an enormous amount of incident flux to increase the implanted concentration. As an example, doubling the concentration from $10^{17}$ to $2\times10^{17}$ Ga atoms-cm$^{-2}$ requires more than five times the incident flux leading to a mask 144 nm below the surrounding substrate. The maximum implanted value at steady state, calculated to be $3\times10^{17}$ Ga atoms-cm$^{-2}$, is dependent on the ratio of the mean implantation depth and the sputter yield. For the two silicon etch chemistries described, this leads to a theoretical maximum etch depth of 3406 nm for the pseudo Bosch chemistry and 425 μm for the cryogenic etch chemistry and a maximum effective selectivity of 85 and 10625 respectively assuming a 40 nm mask layer. However, practically achievable figures will be lower, as determined by fidelity requirement and the point of diminishing returns in implantation, where the selectivity increase is less than the amount milled by the Ga beam.

Based on SRIM simulations, the 1-sigma average density of Ga assuming no phase segregation or preferential removal of silicon is approximately 14% of the density of a pure Ga layer. However, silicon’s low solubility in Ga is well known [39], so the assumption of complete segregation of the implanted Ga combined with measured Ga lattice constants leads to a figure of 5.11 - 8.66 equivalent monolayers of Ga present at the threshold dose. This leads the authors to speculate that the etch masking mechanism is the formation of a contiguous Ga layer that forms involatile compounds in fluorine-based chemistries and fails once the layer is breached via physical sputtering of the mask.
Nanometer Scaled Devices
Etching silicon nanostructures using top-down fabrication techniques enabled creating precisely patterned arrays for investigation of nanoscale properties. Moreover, control over nanowire lengths for nanowire diameters down to 20 nm is significantly more repeatable compared to bottom-up growth. On the same sample it is possible to prepare identical or different diameter nanowires of precisely the same length in any given pattern. Given this advantage, nanowire arrays for electrical probing of individual pillars became possible using a probe station mounted in a Quanta SEM.

Although precision in situ electrical measurements of the vertical nanowires have proven difficult, observations made during probing has spun off many interesting avenues. This chapter will detail characterization of electrical probing of the silicon nanowires using this new method and its advantages for vertical devices. Rapid fabrication of lateral silicon beams using the Ga implantation will also be discussed along with some measurements to describe their properties.

Vertical Silicon Nanowires
Alumina Etch Masked Nanowires
Establishing etch control for the silicon nanowires was interesting, but as soon as they were fabricated it was pondered if they could be used for devices such as vertical silicon transistors. Before the transistors could be designed however, an understanding of the conduction and contact properties was needed. Nanoscale conduction is not the same as it is on the micron scale. It has been observed for lateral devices that as the surface to volume ratio decreases, surface states become more significant. As the nanoscale
regime is reached, the unpassivated surface states have the theoretical potential to completely stop conduction. This section will describe how the nanowires fabricated using the alumina etch mask were measured, some of the surprising results observed, and possible routes forward for improving the silicon nanowires.

Fabrication of the silicon nanowires follows that described in the alumina etch mask section. All of the vertical nanowires and nanopillars described in this section utilized P⁺ silicon with resistivities of 5 to 20 mΩ-cm. Upon completion of etching, the alumina etch mask was removed using a RCA-1 and BHF clean cycle, detailed in Appendix A [40]. Upon completion of the clean, gold was thermally evaporated on the backside of the silicon at a rate of 5 Angstroms per second. The thickness of the metal was until a glass cover slide was no longer optically transparent, approximately 50-100 nm. Layout of the pillars was arranged such that each pillar diameter would be repeated 8-10 times in the ‘x’ direction. The pillars were also arranged in ‘y’ to start at a 400 nm diameter and decrease in approximately 40 nm steps down to 20 nm diameter. The samples then increased in 20 nm increments up to 200 nm. Since each pillar was etched simultaneously, the array provided a range of pillar diameters with identical lengths. Spacing between rows of pillars was set to 5 microns and spacing of pillars in the row was set to 2 microns.
The high doping of the silicon offers two useful advantages. The first advantage is that since the silicon has increased in its surface to volume ratio and surface states become important, a large acceptor density would encourage a smaller effect from the surface states. To clarify this idea, consider a perfectly contacted Ohmic vertical silicon nanowire of radius ‘r’. Ideally the resistance would be as follows:

$$R = \frac{\rho L}{\pi r^2}$$

Here, $R$ is the resistance of the nanowire, $L$ is the length, $\rho$ is the resistivity, and $r$ is the radius. However, if surface states are present at the surface of the silicon, a depletion region will form radially. This depletion region will extend until charge neutrality in the semiconductor exists. This can be expressed by integrating the number of surface states over the surface and equating it to the charge in the depletion region:

$$\int \int N_s dA = \int \int N_a dV \rightarrow 2 \pi r LN_s = \pi LN_a(r^2 - a^2) \rightarrow a^2 = r^2 \cdot \left(1 - \frac{2N_s}{rN_A}\right)$$
The last equation describe the actual radius of the pillar not depleted, \( a \). Correcting the ideal resistance term yields:

\[
R = \frac{\rho L}{\pi r^2 \cdot (1 - \frac{2N_s}{rN_A})}
\]

Hence, as the doping level increases, both the resistivity decreases and the effect of surface states decrease. A second advantage of using P\(^+\) silicon is that creating an Ohmic tunnel contact becomes increasingly easier. This enables for the backside contact to become relatively unimportant.

After sample preparation was complete, the samples were mounted in a FEI Quanta SEM. A 90 degree mount was used and the sample was adhered using conductive copper tape. The stage was set to approximately 10mm, the focal length for this particular SEM. A four point probe stage was then mounted around the sample. Although the stage has the capability of a 4 point measurement, the size of the pillars prevents making one. A tungsten probe tip is bent 90 degrees with about a ¾ inch lead. This probe tip is then mounted such that the side of the probe makes contact along the backside metal. This helps to maximize the tungsten-gold surface contact. The second tungsten probe is also bent but with only a 1 cm lead. One of the two electrical feed-throughs is then grounded using a coax ground connector. This connector shorts the outside of the coax, SEM chassis ground, to the backside tungsten probe tip. It should also be noted that the sample mount is also connected to SEM ground. The second feed-through is connected to an Agilent Semiconductor Parameter Analyzer 4155 C. The coax ground connects the SEM chassis ground to the instrument’s ground and connects the tungsten probe, making the top contact, to the positive channel of the instrument. By placing the nanopillar at 90
degrees relative to the SEM beam, it allows for the probe tip to contact the top of the pillar without image obstruction.

With the mounting described, here are several notes of caution when conducting electrical probing of silicon devices in the SEM. The Quanta SEM is outfitted with an IR imaging system which allows the user to have a constant view of the chamber. Unfortunately, this imaging system induces photo-current in the devices. This extra current can significantly confound the electrical measurements being made, especially since the nanowires and nanopillars typically have very large resistances and have very small currents on order that are generated by the IR photons. However, stage movements should only be made with the IR camera on to prevent collisions with the SEM’s pole piece. Secondly, although the SEM can image the sample while probing, doing so also generates current. This is the basis of the electron induced beam current imaging (EBIC) technique. Moreover amplification is proportional to the beam voltage, so it is very easy to get a several thousand amplification of beam current in the device if current is allowed to flow through it. For these reasons, all electrical measurements detailed here were made with the electron beam blanked.
Fig III.2  Scanning electron micrograph of a 45 nm diameter silicon nanowire, etched 2.5 microns tall, is being electrically probed by a tungsten probe tip and electrically measured. An interesting observation is the amount of flexing of the nanowire.

Fig III.3  Scanning electron micrograph of a 60, 80, and 100 nm diameter silicon nanowires, etched 1.5 microns tall spatially arranged to allow access for electrical probing.

Three distinctive curves were observed during I-V measurements. The first type of curve was exponential behavior in quadrant 3 with relatively little current in quadrant 1.
Chapter 4 will explain this curve type in more detail; essentially the tungsten probe tip interacting with the P⁺ silicon creates a Schottky diode which is reverse biased when a positive voltage is applied to the top of the silicon nanowire. The low current levels seen in quadrant 1 can be described as leakage current with a voltage dependence due to barrier height lowering from image charges. The second behavior observed was approximately the linear behavior expected of a resistor. This behavior was rarely seen. Instead, the most common behavior was a cubic shaped ‘s’ function, type 3. As another subdivision of behavior type 3, the curves were subdivided into symmetric and non-symmetric; definition of this symmetry was only approximate and was based on the relative current magnitude between each side.

Fig III.4 Current vs. Voltage measurements of silicon nanopillars; sizes vary from 240 nm to 50 nm in diameter and the lengths are 2.5 microns long. These curves demonstrate ‘s’ curves with symmetric and non-symmetric behavior.

The majority of curves measured predominately show ‘s’ shaped behavior. What should be noted is the extremely small currents measured. Ideally, if these devices were
treated as resistors, their values would vary in range from 1 kΩ to 200 kΩ; this would imply hundreds of microamps. Other experiments conducted, similar to these, yielded similar results, with currents ranging from hundreds of picoamps to nanoamps. Before conducting a detailed analysis on the device physics of the nanoscale, it was obvious that this contacting problem required correction. Contacting a 400 nm diameter highly doped silicon pillar should have a very low resistance. Aside from the physics, which modified the shape of the curve from the ideal Ohmic to ‘s’ shaped, being the possible culprit for low conduction, three other potential contributions were considered. First, if the tungsten to silicon connection was actually a Schottky diode, vice an Ohmic tunnel contact, then as the resistances of the pillars increased it would adversely affect the conduction. When a diode is placed in series with a large resistor, increasing voltage causes an increase in current from the diode. This current increase also causes an increase in voltage dropped by the resistor. The result is that the voltage increase across the resistor reduces the voltage across the diode; a negative feedback which shuts the diode off. Second, parallel conduction paths or incorrect wiring from outside the Agilent SPA to inside the SEM would cause an erroneous measurement (which could be compounded with the Schottky diode). To eliminate this possibility, probe tip to probe tip measurements were made inside the SEM to ensure low series resistances; typical values were under 50 Ω. Further, open circuit measurements were performed to ensure there were no parallel conduction paths as well as to measure the resolution of the instrument which was in the tens of GΩ; essentially, the smallest current measurable was approximately 10 pA. Third, the physical contact between the tungsten probe and silicon is imperfect. Even with a perfectly clean silicon sample, where surface oxide is removed, and a clean tungsten probe tip, the contact area would be reduced due to surface roughness of the tungsten. This option was
very probable. In fact, from measurement to measurement of the same nanowire, I-V curves were observed to vary greatly. This indicated that contact resistance was the probable cause.

In an attempt to reduce the Schottky contact and improve the contact resistance, several modifications to the probing procedure was done. First, gold was evaporated on the tungsten probe tip. This assisted in reducing the contact barrier height between the silicon and probe tip. Since the evaporated gold was soft, driving the probe tip down onto the nanowire pushed the wire into the gold slightly. Ideally, this maneuver would improve the contact resistance. Also, immediately before the silicon sample was placed in the SEM, the sample was dipped in BHF for 1 minute to remove any native oxide and hydrogen terminate the surface states. Using these modifications yielded significantly improved results for the same sample. However, typical currents were still nA. Improvement in contact resistance was required for more accurate measurements of sub 100 nm diameters.

Fig III.5 Current vs. Voltage measurements of silicon nanopillars; sizes vary from 422 nm to 215 nm in diameter and the lengths were 1.5 microns long. Note, the 371 diameter is reduced by a factor of 0.005 for plotting purposes. These curves demonstrate type 3 curves with symmetric and non-symmetric behavior.
Vertical Ga-Silicon Nanopillars

The advantage of using implanted Ga mask is that this rapid fabrication technique creates nanopillars and nanoscale beams in just a few minutes with dimensions as small as 30 nm. Further, the fabrication is a completely dry fabrication, meaning that liquids such as developer or HF are not required; this is a significant advantage. The engineering trade off for rapid prototyping is that the silicon surface is turned amorphous and implanted gallium is left interstitial instead of becoming bonded as a dopant. In this section, several techniques are described for fabrication of the Ga-Si nanowires and electrical measurements are made to characterize their electrical properties. This section also details how the a-Si Ga mixture provides an optimal interface for electrical probing of vertical nanopillars using a tungsten probe tip.

In Chapter 2, the writing and etching using the Ga mask was described. Most importantly, the required dose to achieve a given etch depth was detailed for the fabrication of vertical nanowires. Patterns of decreasing size and dose were
simultaneously etched to develop a description of the masking effect. One such example of the patterns used is square silicon pillars whose size began at 200 nm and decreased in 20 nm increments down to 40 nm. Etch depths varied from 100 nm up to over a micron. One very noticeable aspect of these pillars, when imaging in the SEM, is the very bright, thin etch masks. This very thin region is the amorphous silicon and gallium which served as the etch mask. Although the alumina masked silicon nanowires were cleaned and free of oxide, they demonstrated a strong Schottky contact when a tungsten probe tip was used. It was hypothesized that this Ga rich layer might offer a more conductive transition between metal and the silicon. For this experiment three sets of pillar arrays were formed identical to those which established the dose arrays. A set of square pillars beginning at 500 nm and stepped down in 50 nm increments were made as well as 2 sets of pillars beginning at 200 nm diameters and stepped down in 20 nm increments and a set beginning at 100 nm diameters and stepped down in 10 nm increments. Note that beam spread and straggle slightly widen the actual size of the pillar. Where applicable, the average measured widening will be stated.

Fig III.7 Scanning electron micrograph of Ga implanted Si nanowires etched 707 nm tall. The array sizes began at 200 nm and were decreased in 20 nm increments down to 40 nm. The areal dose applied increases from right to left.
Using the same probe station in the Quanta SEM, one of the etched dose arrays was mounted and electrically probed in a manner identical to that of the alumina masked silicon nanowires. The 2 point probe measurement was made using an Agilent Semiconductor Parameter Analyzer 4155 C. The measurements were performed by lowering the tungsten probe tip down to the vertical pillars and gently placed on the tops. Care was taken to ensure that the probe tip did not penetrate through or remove the Ga mask layer. The measurement was made several times to ensure repeatability.

Fig III.8 Scanning electron micrograph of Ga implanted Si nanopillars. A tungsten probe tip makes electrical contact to the top of a 70 nm diameter pillar etched 660 nm tall.

From the I-V curves of the squares, it was observed that the a-Si Ga mixture improved conduction as compared to that seen previously. All of the square pillars from 500 nm down to 150 nm were conducting 1 mA before 2 volts was reached implying that the pillar resistances were all less than 2 kΩ. From a geometrical viewpoint and given an etch depth of 616 nm, the lowest resistance seen should have been 123 Ω and the highest
1370 Ω. The implication is that this new contacting scheme is a significantly lower contact resistance than before when using only a tungsten or gold plated tungsten probe tip.

Qualitatively, the data demonstrated I-V curves both linear and symmetric ‘s’ shaped. All of the pillars I-V curves were numerically curve fit to one of two functions. The first was a linear function where the inverse of the slope determined the resistance. The second function was a summation of two exponential curves of the form, \( I = I_a \cdot \exp^{(b \cdot V)} + I_c \cdot \exp^{(d \cdot V)} \).

Four of the nine pillars in the 500 nm to 150 nm array were best described by a linear function and their respective resistances determined and compared to their geometric ideal resistance; the values agreed closely. The other 5 pillars were better fit using the exponential function. The fitting coefficients demonstrated a common trend for 4 out of the 5 pillars. Specifically, the \( I_a \) and \( I_c \) coefficients were the same except opposite in sign and the \( b \) and \( d \) coefficients were the same but also opposite in sign. This implication was that the curves were highly symmetric. The 5\textsuperscript{th} pillar described by the exponential function demonstrated the non-symmetric bending where the coefficients did not match. There was a slight trend with pillar diameter, in that the curves generally were more horizontal as area decreased. However, this trend was not strictly observed. A likely explanation for this effect is that although the doping is \( 10^{19} \) cm\(^{-3} \), the imperfect contact still offers a large contact resistance; approximate that of the pillar resistance. From this, several conclusions can be made. First, the Ga etch mask provides a better contact surface than using only a tungsten probe tip. Second, the exponential behavior is likely due to an imperfect contacting between the tungsten and mask, increasing the barrier height of the contact. A possible explanation for the curve shape will be discussed later.
Fig III.9 Current vs. Voltage measurements of silicon nanopillar squares masked using the implanted Ga from the FIB. Sizes were 500 nm stepped down in 50 nm increments to 150 nm; with the length of 0.615 microns tall. The high currents seen here demonstrate the improvement the a-Si Ga layer provides for contacting.

For a better resolution of changes which might be diameter dependent, the second pattern was measured on the same sample. This dose array, previously seen in Chapter 2, began with 200 nm diameter pillars and decreased in 20 nm increments down to 40 nm diameters. A typical increase in diameter was about 18 nm. To remove the areal dependence from current, current densities were plotted. This allows for the interesting size dependence to be obvious. The J-V curves again displayed the ‘s’ curvature. Further, the maximum current density again decreased as diameter decreased. As the diameter decreased below 100 nm, a second effect occurred, the quadrant III curvature became more pronounced while the quadrant I curvature reduced until there was no conduction for the smallest of diameters.
Fig III.10  Current density vs. Voltage data from the implanted Ga masked nanopillars. The pillar heights were 620 nm and the diameters ranged from 220 nm down to 140 nm. Note that the 159 nm and 139 nm current densities are multiplied by 100 for scaling.

Fig III.11  Current density vs. Voltage data from the implanted Ga masked nanopillars. The pillar heights were 620 nm and the diameters ranged from 180 nm down to 58 nm. As the diameter decreased, the quadrant I exponential decreased to very small conduction.
Finally, the last array measured consisted of 100 nm diameter pillars down to 40 nm diameters, and were decreased in 10 nm increments. The current densities measured were approximately double that of what was measured in the 200 nm array. The curvature was still the ‘s’ shaped symmetric exponential curves which became more non-symmetric as the diameters decreased. The pillar diameters were also about 5-7 nm larger in diameter than that written. Since the SEM resolution was not as high of quality as that when using less magnification, an approximate error bar for the diameters would be 10 nm in diameter.

![Ga-Si Nanopillar I-V Measurements](image)

Fig III.12  Current density vs. Voltage data from the implanted Ga masked nanopillars. The pillar heights were 620 nm and the diameters ranged from 110 nm down to 44 nm. As the diameter decreased, the quadrant I exponential decreased to very small conduction.
Electrical Properties of Vertical Nanopillars

Electrical conduction of semiconductors under reduced dimensions is becoming more interesting and more important yearly as industry drives the transistor node downwards. Current investigations in the nanoscale are displaying semiconductor physics that is much different than what is seen on the micron scale. Importantly, conduction through long (approximately 1 micron) and thin nanowires are of great concern as the semiconductor electronics industry begins to launch fabrication lines at these scales. By looking at conduction properties of both the alumina and the Ga masked silicon nanowires, this section will detail observations and some conclusions made from \textit{in situ} measurements characterizing these devices by this relatively new method of measuring.

As was noted in previous sections, although several I-V and J-V curve shapes were observed, two major classifications were devised. The first is a linear, or purely a resistive, curve. This was more typically seen in the structures with areas bigger than $4 \times 10^{-14}$ m$^2$. As the sizes reduced, a more general ‘s’ shaped curvature was seen. This regime was further subdivided into symmetric and non-symmetric. Throughout this work, I-V curves were typically displayed since their curvature includes the effect their area has on current conduction. Larger areas typically display higher current magnitudes than smaller values. For this reason, J-V curves are used to visually remove the magnitude effect in the plots caused by the area. However, simply taking out the area from the saturation current does not completely eliminate this effect. Evidence of this fact is obvious since the J-V curves do not lie on top of each other. Since the nanopillars are small, typically only 2-probe measurements are available for vertical pillars. The consequences of this measurement restriction imply that the voltage driving the nanopillar is now distributed across the
contacting junction, the nanopillar, and the substrate/contact. Although the substrate can be typically ignored, separation of the contact resistance and pillar resistance become difficult. Even under the best of circumstances, the series resistance from the pillar can act as a negative feedback on the contacting junction. Numerically separating this effect becomes difficult, as the equation is transcendental, and plotting tends to require lots of data manipulation beforehand.

A second effect involving area is that surface states are understood to create a depletion region between the surface and bulk. This effect was introduced at the beginning of this chapter and several publications made on this topic within the last few years. Inclusion of this effect must be taken with care, however, since a simple modification of saturation current (or current density) does not completely describe this effect. Decreasing the diameter also increases the contact resistance. Further, although the pillar becomes depleted of carriers, space-charge-limited current (SCLI) can dominate conduction complicating standard assumptions of conduction in the depletion region.

Most measurements made to detail these types of measurements rely on knocking the nanopillars over, lithographically constructing large metal contacts, and making 4 probe measurements to eliminate these surface effects. The work performed for this thesis was to explore the feasibility of in situ measurements. So the measurements here are burdened with a 2-probe regime. Under the most difficult conditions, here a 40 nm diameter pillar, it is possible to have the majority of the voltage applied, dropped across the contact. This implies that measurements are describing junction effects instead of the assumed pillar effects. As an example consider the best contacting situation, a highly
conductive tunnel contact. Then the measurement is actually a voltage divider between the contact and the pillar resistance is as follows:

\[ V_{\text{junction}} = V_{\text{measured}} \frac{R_{\text{Contact}}}{R_{\text{Contact}} + R_{\text{Pillar}}} = \frac{R_{C} R_{P}}{R_{C} \left( \frac{2N_{S}}{\gamma N_{S}} \right)} \]

Here, \( R_c \) is the specific contact resistance in Ohm-m\(^2\). Notice that device area is not a factor here. For a reasonable barrier height and high doping, where tunneling is dominant, one can expect a \( 10^{-3} \) Ohm-cm\(^2\) specific contact resistance. Given a 0.05 Ohm-cm resistivity and 1 micron pillar height, the majority of the voltage is across the contact. However, since contact resistance is only determined around zero volts, this is not always the case. As the bias is increased, the device current increases exponentially and the contact can rapidly become less resistive. However, measuring the slope of an I-V curve around zero can provide insight on the behavior of the contacting junction.

Fig III.13 Contact resistance for pillars contacted directly by the tungsten probe tip and for pillars with an a-Si Ga interface between the silicon and tungsten probe. The black line shows thermionic field emission theory for a 0.7 V barrier height.
By measuring both types of nanopillars in the manner described, the behavior of the contact around zero was extracted. From the graph, measurements of the alumina masked pillars (note the alumina was removed) and the Ga masked pillars display two different behaviors. Since the alumina masked pillars effectively had the probe tip making contact directly with the silicon, and the silicon was highly doped, it was expected that the contact should be described by a thermionic-tunneling Schottky contact. Qualitatively, although the barrier height is determined by the difference between the work function of the metal and the work function of the silicon, the depletion width is controlled by the doping levels. Using a $2 \times 10^{19}$ cm$^{-3}$ doping establishes a very thin depletion region, less than 6 nm. At this thickness, tunneling can occur as described by Padovani et al [41]. However, the thermal energy is still a significant contribution to majority carrier conduction over the barrier. For this reason, thermionic-field emission was used to describe the barrier; this is the solid line in the figure.

\[
R_C = \frac{V_{th} \cdot \sqrt{V_{oo}} \cdot \cosh \left[ \frac{V_{oo}}{V_{th}} \right] \cdot \text{Cot h} \left[ \frac{V_{oo}}{V_{th}} \right]}{A^{**}T^2 \pi \left( \phi_{BP} - \phi_p \right)} \cdot \text{Exp} \left[ \frac{\phi_{BP} - \phi_p}{V_{oo} \cdot \text{Coth} \left[ \frac{V_{oo}}{V_{th}} \right]} \right] \cdot \frac{\phi_p}{V_{th}}
\]

where $V_{oo} = \frac{h}{2} \sqrt{\frac{N_A}{m^* \epsilon_{sl}}}$

Here, $V_{th}$ is the thermal voltage of 0.02582 V, $\phi_{BP}$ and $\phi_p$ are the barrier height and the difference between Fermi level and valence band respectively, $V_{oo}$ is approximated at 22.6 mV, $A^{**}$ is the Richardson constant, and $T$ is the temperature. The barrier height is approximated at 0.7 V for a p-type silicon and tungsten contact.

A striking difference was observed for the W/a-Si Ga/Si contact. Large areas show a significantly reduced barrier potential. This was commented on previously when micro-
Amps were measurable on the square pillars vice the tungsten contacted pillars showing pA. Even more striking is the transition from the low contact resistance to that of where a contact barrier of 0.7 V is seen. The 100 – 40 nm Ga pillar array shows a high contact barrier. The 500 – 150 nm Ga pillar array shows a very low contact barrier. The 200 – 40 nm barriers shows the transition range with satisfactory overlap between the two barriers.

The reduced contact resistance in the 500-200 nm range can be explained by approximating the effect as a graded junction. It is likely that with the a-Si Ga interface acting as a highly doped, thin silicon region a reduced barrier height is achieved [42].

![Fig III.14 Illustration of a possible method for the reduction of the contact barrier when using implanted Ga etch masks. It was observed that the implantation reduces contact barrier height from 0.7 V to 0.26 V.](image)

\[ \Delta \phi_{BP} \sim \frac{q}{\varepsilon_{si}} \sqrt{\frac{N_{Ga} t_{Ga}}{4\pi}} \]

Here, \( t_{Ga} \) is the remaining thickness of the mask and \( N_{Ga} \) is approximated doping. By making very modest assumptions of doping of the Ga mask at \( 5 \times 10^{19} \text{ cm}^{-3} \) with a thickness of 20 nm, a theoretical barrier height reduction of 0.44 V occurs. By reducing the barrier height to 0.2 V, thermionic tunnel theory predicts a significant resistance reduction. This
effect is striking since anneals are typically required to activate the implantation; although it is known that implantation does activate some of the ions due to heating.

Fig III.15 Contact resistance for pillars contacted directly by the tungsten probe tip and for pillars with a-Si Ga interface between the silicon and tungsten probe. The lines shows thermionic field emission theory for a 0.7 V barrier height (dotted) and 0.26 V reduced barrier height (solid).

The 200 – 40 nm nanopillar range provides a striking transition from the low barrier height to the expected Schottky barrier height. Although what is physically happening during the transition is enigmatic, it is clear that the effective barrier height ($\phi_{\text{Bp}} - \Delta \phi_{\text{Bp}} - \phi_p$) term is responsible. With the W Si nanopillars below 100 nm diameter, the contact resistance is only slightly greater than that expected from the larger pillars. Since the barrier height reduction is not applicable, the ($\phi_{\text{Bp}} - \phi_p$) difference is what is responsible for this slight increase. Feasible increases in this effective barrier height of 0.1 – 0.2 V numerically describe the data. The a-Si Ga nanopillars demonstrate a diameter dependent increase in barrier height with a rate of approximately 0.6 V per 100 nm. This dependence stops around 100 nm where the barrier height returns to the 0.7 V regime. It is likely that surface states, either from the sides of the pillar or between the metal silicon
interface, drive the overall barrier to greater values making tunneling and thermionic current more difficult. Based on the overlap of the independent data sets, and repeatability of the results, it is unlikely that this transition is due to contacting problems of the probe tip.

Understanding the consequences of barrier height on the overall 2-probe measurement requires looking again at the J-V curves. It was previously noted that the curves took on a ‘s’ shape and that this ‘s’ shape was modeled by an exponential behavior for both the forward and reversed biased directions. This exponential behavior is described well using the combination of thermionic emission and tunneling. In the forward biased regime:

\[
J_{Fwd} = \frac{A^* T^2 \sqrt{\pi \cdot V_{oo} \left( \phi_{BP} - \phi_p - V \right)}}{V_{th} \cdot \cosh \left[ \frac{V_{oo}}{V_{th}} \right]} \cdot \exp \left[ \frac{\phi_{BP} - \phi_p}{V_{oo} \coth \left[ \frac{V_{oo}}{V_{th}} \right]} - \frac{\phi_p}{V_{th}} \right] \cdot \exp \left[ \frac{V}{V_{oo} \coth \left[ \frac{V_{oo}}{V_{th}} \right]} \right] \\
J_{Fwd} \sim J_a \cdot \exp[bV]
\]

In the reversed bias regime:

\[
J_{Rvd} = \frac{A^* T^2 \sqrt{\pi \cdot V_{oo} \left( V + \frac{\phi_{BP}}{\cosh \left[ \frac{V_{oo}}{V_{th}} \right]} \right)}}{V_{th}} \cdot \exp \left[ -\frac{\phi_{BP}}{V_{oo} \coth \left[ \frac{V_{oo}}{V_{th}} \right]} \right] \cdot \exp \left[ \frac{V}{V_{oo} - \tanh \left[ \frac{V_{oo}}{V_{th}} \right]} \right] \\
J_{Rvd} \sim J_c \cdot \exp[dV]
\]

An interesting aspect seen plotting the saturation current densities, \(J_a\) and \(J_c\), is that as barrier height changes a decreasing saturation current results. Hence, as the diameter decreases, one should expect the saturation current density to actually decrease. Further, exponential behavior of the nanopillars and effects due to diameter, are best described by
the contact vice the nanowire itself. This conclusion explains a fair amount of the
results seen across the scientific community. Similar effects were seen from both the W Si
contacts and the W a-Si/Ga Si contacts. To demonstrate this point, the curve fitted
parameters from the 200 – 40 a-Si/Ga nanopillars was tabulated for all the coefficients and
$R^2$ values. It is interesting to note that there is a slight difference in $J_a$ and $J_c$ values.

![Graph](image)

**Fig III.16**  Theoretical saturation current densities, $J_a$ and $J_c$, reducing as barrier height
increases, as predicted from thermionic field emission theory. The values used are
the same as stated earlier in this section. The forward bias, $J_a$, is constantly a
smaller than $J_b$ for the same barrier.

<table>
<thead>
<tr>
<th>Pillar Diameter (nm)</th>
<th>$J_a$</th>
<th>$b$</th>
<th>$J_c$</th>
<th>$c$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>1.84E+09</td>
<td>1.039</td>
<td>-1.78E+09</td>
<td>-1.388</td>
<td>0.9988</td>
</tr>
<tr>
<td>180</td>
<td>3.29E+09</td>
<td>1.512</td>
<td>-3.33E+09</td>
<td>-1.655</td>
<td>0.9993</td>
</tr>
<tr>
<td>160</td>
<td>-</td>
<td>-</td>
<td>-1.60E+08</td>
<td>-3.372</td>
<td>0.9675</td>
</tr>
<tr>
<td>140</td>
<td>6.77E+05</td>
<td>2.014</td>
<td>-7.23E+05</td>
<td>-2.086</td>
<td>0.9985</td>
</tr>
<tr>
<td>120</td>
<td>1.45E+04</td>
<td>3.347</td>
<td>-1.46E+04</td>
<td>-3.494</td>
<td>0.9930</td>
</tr>
<tr>
<td>100</td>
<td>4.67E+03</td>
<td>1.681</td>
<td>-6.34E+03</td>
<td>-1.734</td>
<td>0.9976</td>
</tr>
<tr>
<td>80</td>
<td>2.49E+03</td>
<td>1.883</td>
<td>-8.09E+03</td>
<td>-1.632</td>
<td>0.9969</td>
</tr>
<tr>
<td>60</td>
<td>2.83E+03</td>
<td>2.154</td>
<td>-2.20E+03</td>
<td>-2.668</td>
<td>0.9903</td>
</tr>
<tr>
<td>40</td>
<td>-</td>
<td>-</td>
<td>-4.87E+03</td>
<td>-2.477</td>
<td>0.9776</td>
</tr>
</tbody>
</table>

**Fig III.17**
Hence, thermionic field emission in both the forward and reversed biased regimes gives a good description of the presented nanowires. The nanowires were seen to have exponential current behavior in quadrant 1 and 3 which can be closely modeled by \( I = I_a \cdot \exp(b \cdot V) + I_c \cdot \exp(d \cdot V) \). Using the amorphous silicon with implanted Ga yields a highly conductive interface which acts as a gradient doped silicon – metal interface. This interface, on the hundreds of nanometer scales, yields a reduced barrier potential allowing for a significantly reduced contact resistance. As the diameter decreases from 200 to 100 nm, a transition was observed. It is likely that this transition, described as an increasing barrier potential, is due to a depletion of charge carriers or potentially from surface states. Using a 2-probe measurement system also was shown to describe more of the physics of the interface, or contact resistance, rather than the pillar itself. In order to efficiently use the nanopillars for sensors, contact resistance will need to be reduced to below that of the pillar resistance. Although further investigation of the contact resistance transition is needed, implanted Ga in silicon seems to offer an advantageous method for probing silicon nanowires.

*Lateral Ga-Silicon Nanowires / Nanobeams*

Vertical silicon nanowires and silicon nanopillars offer the ability to expand silicon technology out of the classic lateral plane. However, there are still technologies which utilize silicon nanowires laterally. Such technologies are lateral electrical wire runs and lateral mechanical beams. It was demonstrated that lateral wires could be fabricated using the implanted gallium mask and that this technology could even be multiplanar; demonstrated by placing the wire 1 micron below the surface. This technology was expanded to two extremes; the fabrication of nanoscale reduced dimensions and wide lateral beams.
Although two different etch chemistries were previously used in Chapter 2, creation of the lateral nanowires does not require both etches. The fundamental requirement to create the suspended structures relies on the undercutting seen when using the cryogenic etch. This undercut is similar to that seen when using a metal mask. Instead of using two etches, a pattern of two circles with a rectangle between the two can be used to generate suspended nanowires. Using low doped N-type silicon, multiple geometries were tested. As an example, two 10 micron diameter circles were made with a separation of 10 microns. A set of 75, 50, and 25 nm width rectangles were patterned between different sets of circles; effectively creating a spoke configuration. For the patterning, a 30 kV, 300 pA Ga beam was unblanked for 0.375, 0.25, 0.125 seconds, respectively. A cryogenic etch was then performed using previously stated conditions for 3 minutes. The result was suspended nanowires 87.5, 65.7, and a 40.5 nm in diameter, 10 microns long and approximately 3 microns above the substrate. The increase in actual width from patterned width is consistent with the 7.2 nm straggle previously determined. An interesting side effect of the undercut was the rounding of the wire; presumably due to the Gaussian beam’s spread combined with the cryogenic’s isotropic like undercutting.
Fig III.18 Scanning electron micrograph of Ga implanted Si nanowires 10 microns long and suspended 3 microns high. The nanowire diameters intended were 75, 50, and 25 nm. Top left shows a 87.5 nm wire, top right and bottom left show a 65.7 nm wire, and bottom right shows a 40.5 nm wire.

Fig III.19 Scanning electron micrograph of Ga implanted Si nanowires 40 nm in diameter and 16 microns long.
In a second experiment, a 25 nm by 16 micron rectangle situated between two 3 micron diameter circles was Ga patterned and etched yielding a 40 nm diameter beam 16 microns long. Although these devices demonstrate the wide application of the implanted Ga etch masking, an important feature of this technique should be reiterated. These silicon nanowires are actually amorphous silicon with some Ga bonded, probably activated during the implantation, and some Ga left interstitially. Reflection electron microscopy in the TEM, similar to that performed on the nanopillars, was performed on these lateral nanowires. This verified that the nanowires were amorphous and the body of the micron post remained crystalline. Since the pillars were wide and the resistance to the substrate very small, it presented a technical difficulty in measuring the electrical resistance of the nanowires.

Fig III.20  Transmission electron micrograph of Ga implanted Si nanowires 40 nm in diameter and 10 microns long.
To address the multiple electrical conduction paths, much larger scale devices were fabricated on SOI (silicon on insulator). The top layer of silicon was N-type 37.5-62.5 ohm-cm silicon 1 micron thick on 1.5 micron thick silicon dioxide. The low resistivity of the top silicon layer implies a very low doping of $10^{14}$ cm$^{-3}$. By etching the structure in the top silicon layer, down to the oxide layer, conductivity could be ensured to be through the lateral wire. For this experiment, much thicker silicon beams were designed. The patterned beams were originally 50, 75, and 100 nm wide and 10 microns long, situated between 10 micron diameter pillars. Implantation in the FEI Nova 200 was performed using a 30kV and 290 pA beam. The areal doses of the beams were $1.45 \times 10^{17}$ cm$^{-2}$, $1.21 \times 10^{17}$ cm$^{-2}$, and $1.45 \times 10^{17}$ cm$^{-2}$ for the 50, 75, and 100 nm beams respectively. The silicon was cryogenically etched in the ICP-380 machine for 80 seconds under the following conditions:

<table>
<thead>
<tr>
<th>SF$_6$</th>
<th>70 sccm</th>
<th>ICP Power</th>
<th>900 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>O$_2$</td>
<td>4 sccm</td>
<td>Fwd Power</td>
<td>3 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-130 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

The etch was tuned to undercut less than 1 micron; this permitted the silicon micropillar to remain mostly vertical but allowed for the beam to be completely undercut and freed. Since the Fwd power was tuned down and a cryogenic etch used, the selectivity of the Ga etch mask significantly increased the width of the beam. This etch tuning combined with the beam being slightly defocused resulted in final beam dimensions of 142 nm, 194 nm, and 252 nm widths. The length was measured to 10 microns and the thickness of the beams approximated to 25 nm based on the implantation straggle. For this experiment, each set of 3 beams was written 3 times to make a total of 9 beams. This redundancy was used to verify resistance measurements taken. The total write time for a
set of beams was approximately 4.5 minutes three beams and the etch time was 1.3 minutes. Including sample loading and unloading from vacuum chambers, the total time to fabricate silicon nanobeams was under 20 minutes and did not require wet chemicals at any stage.

Fig III.21 SEM of 2 tungsten probe tips contacting one of three lateral Ga-Si beams 10 microns long. The I-V measurements of these beam indicates a resistivity improvement from 40 to ~1 Ω-cm.

With the fabrication completed, the samples were loaded onto the probe stage in the Quanta SEM. Two tungsten probe tips were brought down to make contact on the two 10 micron diameter pads. Several preliminary measurements were made to verify that there were no alternate conduction paths other than going through the beam: both probes contacting the substrate measured as an open circuit, and one pillar on a pad and the other left dangling measured an open circuit. Given the dimensions of the beams and the lowest resistivity of the crystalline silicon, expected resistances should be 1.056 GΩ, 773
MΩ, and 595 MΩ respectively. Actual measurements yielded resistances around 100 MΩ and down to 14 MΩ. Given the physical dimensions of the beams, an upward bound of the resistivity of the beams were measured to 0.2-4.5 Ohm-cm. The measurements were repeated over each of the three groups and then performed again on an identically fabricated second sample. All of the measurements were within the range reported here. Although the exact nature of the conductivity is not understood in detail, qualitatively the interstitial Ga mixed with amorphous silicon creates a type of binary phase material. It is likely that the conduction of this sludge-like layer is mostly due to the conduction through the Ga.

Fig III.22  Current vs. Voltage measurements of implanted Ga masked lateral silicon nanobeams. From the geometry, resistivity of less than 5 Ohm-cm was inferred. The red curves was for a ~150 nm wide beam, the green curve was for a ~200 nm wide beam, and the blue curve for a ~250 nm wide beam.

Several observations were made during the probing of the beams. First, the SEMs denote a clear differentiation of the Ga implanted silicon and the crystalline silicon. This is seen from changes in SEM signal intensity of the 10 micron pad. The images are seen as bright discs atop of a darker etched structure. The undercut of the disc also denotes this transition. Second, in many of the high areal dosed Ga implanted regions, there are dots of brighter intensity. This feature is notable, for example, in the 40 nm diameter nanowires...
and in the 10 micron contact pads. TRIM calculations indicate that an aerial dose of $1 \times 10^{17} \text{ cm}^{-2}$ results in a maximum Ga density of $4 \times 10^{22} \text{ cm}^{-3}$; this is exceeding the solid solubility of Ga in silicon at room temperature [43]. It is likely that these dots are locations where the Ga segregate and coalesce from the amorphous silicon [44]. This segregation was not seen for the lower dose, such as with the critical dose array described in Chapter 2. Some future experiments might include TEMs of the dose array to determine when the segregation begins. Since the lower areal dose limit is based on the selectivity from the etch, this segregation dynamics might act as the upper limit for areal doses instead of the milling limit.

Fig III.23  SEM of a lateral implanted Ga masked silicon nanobeam. The beam was constructed on SOI with a 1 micron thick silicon layer. Note the bright regions on both the beam and the pad which is interpreted as Ga segregating out of the etch mask due to a high areal dose.

A third observation made was that during the probing of the pads, the amorphous silicon – gallium layer was able to be physically moved about using the tungsten probe tip.
Further, if the probe tip was pushed down too far, the tungsten could make contact with the low doped silicon and greatly increase the resistance measured. This layer is likened to mud, where it the combination of sand and water creates a dual phase system. In this case, the Ga would act as the liquid state and the amorphous silicon as the solid state. From this idea, it was hypothesized that annealing could recrystallize the silicon while activating the Ga (placing the Ga in the diamond lattice structure of the silicon). As a first attempt, a 12 hour \( N_2 \) anneal at 1000 C was performed on the samples. Resulting from the temperature changes, all of the beams were fractured; the appearance of the broken beams indicates that they were under tensile stress. Most importantly, sections of the contact pad could be fractured off and all of the observed Ga segregations were no longer present. From many sessions probing these implanted structures, fracturing of unannealed sections has not been observed. These observations are encouraging and future work might include optimizing anneal for these nanobeams; possibly to independently control Ga activation and recrystallization. It was also hypothesized that a Rapid Thermal Anneal before etching could heal the silicon and activate the Ga. For this experiment, the RTA was performed at 800C for 2 minutes. Optically, it was observed that the Ga segregations remained, indicating that a significant amount of Ga diffusion did not occur. However, under identical etching conditions to that which fabricated the nanobeams described earlier, there was no masking effect on the silicon except where the Ga segregations were observed. Although not conclusive, it is likely that some of the implanted Ga did activate, leaving little interstitial Ga. This might have prevented the bonding of F or O to the Ga to act as an etch mask.
Fig III.24  SEM of a lateral implanted Ga masked silicon nanobeam after a 12 hour thermal anneal at 1000 C. All of the beams broke under tensile stress (right). From the chipped region on the pad (left), it is hypothesized that recrystallization of the silicon occurred and the lack of segregated Ga indicates that activation occurred.

From the SEMs, a downward or upward bending in the lateral nanobeams can be observed. Since the beams are approximately 10 times wider than they are thick it is expected that this bending is mostly in a direction normal to the substrate. When the sample is imaged at 85 degrees, a maximum deflection of 340 nm is measured. Using a triangular argument, the beam was expanded by approximately 10 nm. Annealing of the same set of beams at 580 C for 50 minutes in a N2 purged atmosphere, shows the beams returning back to horizontal. Further, it is observed that a material was leached out of the silicon to the surface. It is likely that the material is Ga and that the anneal pushed the excess Ga out. The removal of the excess material reduced the length of the beam. This experiment provides incentive to understand the annealing process for silicon as a method to control beam tension.
Fig III.25 SEMs of a lateral implanted Ga masked silicon nanobeam before (left) and after (right) a 50 minute thermal anneal at 580 C. Comparison of the two SEMs indicate that the beam was laterally extended by 10 nm and upon annealing, the material forcing the extension is pushed to the surface returning the beam to horizontal.
Micrometer Scaled Devices
This chapter details applications of the etching and fabrication developed for micron length scales. There are two major applications of this work in silicon and they will be discussed separately. The first application was the push to develop portable nuclear magnetic resonance (NMR) integrated into silicon. For this application, several devices were created: a 1 Tesla magnetic field created using NdFeB permanent magnets, and planar microcoils in silicon. The magnetic field was shimmed by fabrication of high susceptibility iron shims in silicon and placed on the surface of the permanent magnet. The planar microcoils were also fabricated in silicon for use as RF magnetic field pulsing to a sample volume and then for detection of the oscillating magnetic fields. Although the NMR apparatus was not completed, a detailed description of the devices as well as experimental evaluation will be discussed here. The second major application of the micron scale work was fabrication of the silicon micropillars described earlier. Besides their specific use in calibration and exploration of the cryogenic etch, these pillars were used for photovoltaic experiments and electrical measurements of Schottky point diodes. The purpose of the diode measurements was to provide understanding critical for the nanowires and will be described in this chapter for completeness. In all of these projects, the cryogenic etching of silicon was the enabling technology to achieve both the planar iron shims and the planar microcoils.

Components of a Portable NMR Apparatus
1 Tesla Magnetic Field and Shimming
This section will detail the generation of the 1 Tesla (T) field using permanent neodymium-iron-boron (NdFeB) magnets. Creation of the magnetic field began with the
design of the inhomogeneous magnetic field. The standard method of generating the magnetic fields for NMR is to use cooled superconductive electromagnets. Fields generated in this manner can exceed more than 20 T for volumes of several cubic centimeters. Although the sensitivity of NMR is proportional to the square of the field, the cost of these can be upwards of several hundred thousand dollars and occupy a very large physical space. As an alternative, there has been interest in utilizing low field permanent magnets due to their low cost and physical size [45,46,47]. The objective of the design described here is to create a low cost, 1 T magnetic field, and using NdFeB magnets in a portable setting so it does not consume any electrical power. Once the magnetic field is established, the second goal was to make a homogenous magnetic field over as large a volume as possible using passive shims [48]. Shims are usually a highly susceptible magnetic material used to alter magnetic fields similar to how lenses can bend light based on the material’s index of refraction [49,50]. To precisely fabricate the passive shims, a design for iron deposited in lithographically patterned silicon was engineered.

To generate the 1 T field a simple magnetic circuit was designed. The geometry of the design was set to minimize the inherent inhomogeneity while maximizing the magnitude of magnetic field attainable [51]. An attractive geometry was chosen such that two of the NdFeB magnets, separated by an air gap, were connected using magnetic steel; the so called ‘C’ configuration. Due to the hysteresis of permanent magnets, the length and the area of the air gap separating the magnets alters the strength of the magnetic field. To determine the strength of the field, the magnetic field flux and magneto-motive force are simultaneously solved [52]. The resulting magnet’s magnetic field dependence on the auxiliary magnetic field, H, is then plotted on the magnet’s demagnetization curve to find the air gap’s magnetic field. To begin, note that the magnetic field flux leaving the
magnet’s face is equal to the field flux entering the gap. Then calculate the magnetomotive force over the steel loop, air gap and magnets. Substitution using the two equations yields an equation for a straight line.

\[ B_{\text{gap}} \cdot A_{\text{gap}} = B_{\text{mag}} \cdot A_{\text{mag}} \]

\[ \int H \cdot dl = 0 = H_{\text{gap}} \cdot l_{\text{gap}} + 2 \cdot H_{\text{mag}} \cdot l_{\text{mag}} + H_{\text{steel}} \cdot l_{\text{steel}} \]

\[ B_{\text{mag}} = H_{\text{mag}} \cdot \left( \frac{-2\mu_{\text{a}}}{l_{\text{gap}} A_{\text{mag}}} \frac{l_{\text{mag}} A_{\text{gap}}}{A_{\text{mag}}} \right) \left( 1 + \frac{l_{\text{steel}} A_{\text{gap}}}{\mu_{\text{r-steel}} l_{\text{gap}} A_{\text{steel}}} \right) \]

Assuming the gap area and magnet area are matched, a numerical solution for a 2 inch diameter magnet yields a slope of \(-5.083/|l_{\text{gap}}|\) in units of T/kOe; this assumes a very large relative permeability of the steel. Placing this line, in red, in the demagnetization curve for a N42 or N52 magnet allows for the determination of the magnetic field in the air gap from the intersection of the two lines. Note that the demagnetization of the magnet depends upon temperature. Further, multiple correction factors should be added to account for non-idealities losses. However, once the slope is calculated for a given system and a correction factor determined, it should be constant for any strength magnet of similar dimensions. This calculation is most useful for considerations of magnet holder geometry.
Fig IV.1  Demagnetization curves for *KJ Magnetics* NdFeB magnets of N42 and N52. The red line is the theoretical demagnetization line; the intersection of the two lines indicate the magnetic field in the air gap.

Using the calculation described above, a holder was designed for 2 inch diameter, 1 inch thick NdFeB magnets. A Garolite fiberglass was constructed to maintain a magnet separation, or air gap, of close to 6 mm. The Garolite holder was constructed of 4 pieces so two magnets could be controllably brought together and placed in the steel loop.

Fig IV.2  Model of the NdFeB magnetic circuit. The blue represents the steel loop and the brown represents the Garolite holders.
Precise control over the magnet was incredibly important because of magnet’s strength. Placing two magnets in contact would require 232 lbs-force for N42 and 278 lbs-force for N52 to separate them again. To safely construct the magnetic circuit the following sequence would need to be performed: 1) lock a single magnet between two holders, 2) slowing bring a vertical steel bar into contact with the backside of the magnet, 3) repeat steps 1 and 2 on the second magnet, 4) slowly bring the two magnets together until the Garolite holders make contact with each other, 5) slowly bring the horizontal steel bar into contact with the two vertical steel bars. Once completely assembled, the magnet is held together with the majority of the magnetic field trapped in the steel loops and magnets or in the air gap. Typical measurements of the field just outside of the gap were approximately 5 Gauss (ten times the Earth’s magnetic field).

Using Comsol and FEMM (both are a finite element magnetic solvers) the magnetic fields were simulated. Simulations were performed in 2-D utilizing symmetry of the system in both cylindrical and Cartesian coordinates. The cylindrical simulations placed the $r=0$
axis along the center line of the magnets and the z axis along the direction of the magnetic field. This assumes symmetry along the theta axis which is not completely valid; this simulated configuration would have the iron loop completely encasing the Garolite holder. To correct for this, simulations in a Cartesian coordinate system were used. In fact the magnetic field across the center of the gap demonstrated a slight perturbation due to the fact that the iron holder was present. This perturbation will be discussed later. To model the magnets, several different terms were required, the relative permeability ($\mu_r$), the electrical conductivity ($\sigma$), the residual flux density ($B_r$), and the coercive force ($H_c$). The conductivity was 0.667 MS/m. The residual flux density and coercive force for the N42 was 1.32 T and 875,820 A/m and for the N52 was 1.48 T and 891,744 A/m. These values were suggested by the manufacturer, KJ Magnetics (www.kjmagnetics.com).

![Fig IV.4 Comsol simulation for determination of the magnetic field. The pink sections contain the magnetic flux, the steel loop and the magnets. The white field is simulated as free space.](image-url)
Running simulations of the magnetic field allowed for the field homogeneity to be determined. Typically, plots of the $B_z$ field plotted both radial at $z=0$ (center of the air gap) and azimuthally at $r=0$ (along the center of the magnet) were used for characterization of the homogeneity defined here as $(B_{z_{\text{max}}}-B_{z_{\text{min}}})/(B_{z_{\text{max}}})$ over a specified radial or azimuthal distance. Unshimmed, the magnetic homogeneity was simulated in Comsol as 5273 ppm over a 1 cm diameter radially and 3568 ppm over the 6 mm azimuthal gap. Simulation of FEMM in radial coordinates yields a radial homogeneity of 4661 ppm and an azimuthal homogeneity of 2777 ppm. This level of inhomogeneity is unacceptable for conducting proton NMR experiments and requires shimming [48,53].

To verify the calculations and simulations, the magnetic field was measured using a LakeShore Model 455 single axis Gauss meter. The Hall probe was mounted on a 3 stage micrometer and zeroed. Placement of the micrometer was measured using a caliper to be approximately square and the setup was measured on a wooden table (glued together) to minimize field distortions due to metal ferromagnetic objects. To ensure the probe’s surface was normal to the magnetic field, the probe was rotated to reach a
maximum field reading. Centering of the micrometer was an iterative process where the radial maxima was first determined in two directions (radial) then the minima was located azimuthally. This process would repeat 3 to 4 times until variations of the peak field were smaller than 10 $\mu$T. The micrometer was moved in 500 (250 for azimuthal) micron increments noting the temperature of the probe. Typical measurements were conducted slowly, taking approximately 10 minutes, to prevent temperature fluctuations of the Hall probe. Using Matlab’s curve fitting toolbox, the measured data was numerically fitted to solve for two components: coefficient for a parabolic curvature, and lateral offset of the field maxima. The maximum magnetic field was set at the highest value experimentally recorded. Due to the cylindrical symmetry of the magnetic field, a negative parabolic function was assumed. From the curve fitting, a lateral offset from zero of approximately 900 microns was seen with a 3558 ppm radial homogeneity over a 1 cm diameter.

![Graph](image)

**Fig IV.6** Gaussmeter measurement of the magnetic field homogeneity. The top graph depicts the magnetic field, $B_z$, plotted radially at the center of the air gap. The bottom graph shows $B_z$ plotted azimuthally along $r=0$. Data points are marked with an ‘x’.

A second experiment was performed to determine the magnetic field’s dependence on the air gap length. For this experiment, the magnets were separated in measured 1 mm increments. Upon separation, the magnetic field’s center was again determined using the
Gaussmeter mounted on the micrometers to determine the azimuthal minima and radial maxima. As a second check of the length, the azimuthal micrometer was used to verify that the minima shifted only 0.5 mm. The data was plotted along with the FEMM simulated data and fitted to 1/(1+x) curves. The basis for using this function derives from using the air gap equation and approximating the demagnetization curve as linear.

\[
B_{\text{magnet}} = \mu_o (1 + \chi) H_{\text{magnet}} + B_r \quad \text{and} \quad B_{\text{gap}} = -2\mu_o \frac{l_m}{l_{\text{gap}}} H
\]

Where \(B_r\) is the residual magnetic field of the magnet, typically quoted by the vendors, \(l_m\) is the length of the magnet, \(l_{\text{gap}}\) is the length of the air gap and \(\chi\) is the susceptibility of the magnet. The intersection of these two equations on the demagnetization curve occurs when the H fields are matched. This yields the following dependence on the air gap length:

\[
B_{\text{gap}} = \frac{B_r}{(1 + \mu_o \frac{l_m}{2 l_{\text{gap}}})}
\]

Under the assumption that the magnet’s length is 25.4 mm, the measured residual magnetic field was determined to be 1.363 T and the magnets relative permeability of 1.911 to an r-square value of 0.9975. Note that magnetic losses are typically represented by a factor multiplied by the ratio of the lengths. Unfortunately, this factor and the permeability term are inseparable; so the 1.911 was really a composite of the terms and should not be thought of as the actual permeability. The determination of the residual magnetic field, allowed for more precise simulations by using this value when describing the simulated magnets. Although adjusting the simulated magnets’ residual magnetic field helped, comparison of the new simulated results with experiments still shows that that the simulated field decreases slightly faster as the air gap is increased.
Fig IV.7 Simulation (blue circles) and measurement (red x) of Bz field as the air gap was increased. The measurement was made using a LakeShore 455 Gaussmeter with the Hall probe mounted on a micrometer. The arrows show the change in simulations results as the magnets are adjusted from supplier’s characteristics to the measured $B_r$.

The large inhomogeneity demonstrated is unacceptable for proton NMR experiments. Magnetic field broadening decreases the NMR’s peak signal intensity by spreading the number of signal generators out over a wider frequency range. Field homogeneity should be as uniform as possible over as large a volume as possible. To perturb the field towards more homogeneity, devices referred to as shims are utilized. Shims can either be (and typically are) active electromagnets or passive ferromagnetic structures. Since this work is designed for portable applications, active shims were not considered since they would draw a large amount of current continuously. Instead, this work details the design and fabrication of passive shims attempting to make use of lithographic fabrication for precision patterning.

To correct the field distortions, two ferromagnetic shims have been designed. The first shim is simply a thin sheet of ferromagnetic material formed into a 1 inch diameter disc.
This disc acts as a collimating magnetic lens to pull the magnetic flux away from the edges of the magnet and back to the center. This is needed since magnetic field lines in the center are repelled from each and are pushed to the outer edge of the magnet. As a second magnetic lens, rings of different diameters and different widths are positioned to assist in flattening the magnetic field to a greater level. Although the second lens performs similar to that of the collimating lens, it is very dependent upon the collimating lens. Essentially, the more the collimator pulls the magnetic field in, the easier it becomes for the shaping lens to achieve higher homogeneity. Hence, it is most logical to design the collimating lens first then fit the second, tuning, lens.

Design of the collimating shim is similar to that of the classic electromagnetic problem of finding the correct coil diameters for a given separation of Helmholtz coils. The difference is that the passive shims are ferromagnetic and hence suffer from a nonlinear B-H curve. As the magnetic field passes through the normal of the shim, a magnet current is established along the perimeter of the ferromagnetic material, \( K_b = M \times n \). The surface current around a disk is then similar to a loop of electric current. By placing a disc in the center of each magnet, a Helmholtz like configuration is established. Instead of a current \( I \), a magnetic current of \( M \times h \) is seen, where \( M \) is the magnetization of the disc and \( h \) is the thickness. Since the magnetization is proportional to \( \chi \), to change the magnetization current one can either use thicker passive shims or a higher susceptibility.

Using this concept, finite element simulations were performed to optimize the field homogeneity by placing a passive ferromagnetic shim in the center of the magnet. This shim was simulated to have a \( \chi \) of 5000 and the disk thickness was set to 7 microns [54]. Although addition of a shim changes width of the air gap, and hence the magnetic field's
strength, changes in the gap by tens of microns are relatively unnoticeable. The first
optimized parameter was the diameter of the shim. By changing the diameter, the amount
of flux being collimated as compared to the amount of flux leaving the magnet is varied.
Looking at the two extremes suggests that an optimum diameter exists. If the shim is the
same diameter of the magnet, no collimation occurs and the homogeneity is that of the
magnet. If the shim is very small it will channel a high amount of flux and create a very
strong field in the center. Running simulations indicated that an optimal shim diameter is
located around 18 mm. It is clear that if the shim is smaller by $\delta$, then a much greater
higher homogeneity will be seen than if the shim was larger by the same $\delta$. For this
reason, the majority of the shims designed were set to diameters of 25.4 mm.

Fig IV.8  Simulation of $B_z$ field radial homogeneity as the passive shim diameter is increased.
The susceptibility used was 5000, approximate to that of iron, and the thickness was
7 microns.

The field bending effect of the shim is proportional to both the susceptibility and the
thickness. So doubling the susceptibility permits a reduction in thickness by half. With this
idea, the optimum susceptibility-thickness ($\chi$-t) product was then varied to determine the
maximum homogeneity. As expected, the stronger the $\chi$-t product, the more significant improvement in the homogeneity. For clarity, to achieve the homogeneity of better than 500 ppm a $\chi$-t product of approximately 0.18 is needed. For example, if $\chi$ were 5000, a thickness of 36 microns would be required; if $\chi$ were 20,000, only 9 microns is needed.

![Graph](image)

**Fig IV.9** Simulation of $B_z$ field radial homogeneity as the passive shim's susceptibility-thickness product is increased. The shim diameter used is 25.4 mm or 1 inch.

The second lens was a series of ferromagnetic rings. The physics behind this design is similar to magnetic field alteration using Helmholtz electromagnetic coils. As a magnetic field passes through the iron, a magnetic surface current is induced on the sides of the rings. The outside of the ring acts to increase the magnetic field whereas the inside ring generates a magnetic current opposite to that of the outside and acts to decrease the magnetic field. Combination of the two currents can act together to provide local additions to the magnetic field. The location of the addition is determined by the average radius of the ring whereas the amplitude of the field addition is determined by the width.
To describe this effect, assume two electromagnetic rings centered at radius \( r \) and separated by a radius of \( \delta \). Further, place the ring a distance of \( a \) away from the origin. Have the outer ring conduct a positive current and the inner ring a negative current of equal magnitude. Then using elliptical integrals, the closed form solution can be written.

\[
\frac{B_z(\rho, z = 0)}{I} = \frac{\mu}{2\pi} \left\{ \frac{1}{\sqrt{(R - \delta + \rho)^2 + a^2}} \times \left[ K(k^2) + \frac{(R - \delta)^2 - \rho^2 - a^2}{(R - \delta - \rho)^2 + a^2} E(k^2) \right] - \frac{1}{\sqrt{(R + \delta + \rho)^2 + a^2}} \times \left[ K(k^2) + \frac{(R + \delta)^2 - \rho^2 - a^2}{(R + \delta - \rho)^2 + a^2} E(k^2) \right] \right\}
\]

Here, \( K \) and \( E \) are the elliptical integrals of the first and second kind respectively. If a ferromagnetic material is used vice the electromagnetic loops, one can replace the currents \( I \) with \( M^*h \); this assumes that the ring has a uniform height.

![Graph](image_url)

**Fig IV.10** Effect of two current loops with equal but opposite currents, separated by a distance \( d = 100 \mu m \). The plot shows the addition to the magnetic field for average radii of 1 mm, 5 mm, and 10 mm.
Fig IV.11  Effect of two current loops with equal but opposite currents, separated by a distance $d=100\mu m$. The plot shows the addition to the magnetic field for average radii of 1 mm, 5 mm, and 10 mm.

A second method to increase the effect of the shim would be to increase the susceptibility of the ferromagnetic material or increase the thickness. The magnitude of the effect is useful because with 1 amp, the inhomogeneity can be shimmed past that achievable from the first magnetic lens. Using these design rules, and the assumption of a first magnetic lens with a thickness of 20 microns, diameter of 1 inch, and susceptibility of 5000, a set of 5 rings were designed to improve the field homogeneity. The rings were assumed to have a thickness of 10 microns and susceptibility of 5000. The average radii and widths of the rings are as follows: 1. 2.025 mm, 50 $\mu m$, 2. 3.05mm, 100 $\mu m$, 3. 3.55 mm, 100 $\mu m$, 4. 4.35 mm, 150 $\mu m$, and 5. 5.25 mm, 500 $\mu m$. These rings were designed using the finite element simulator previously described. With the design parameters stated, the magnetic field could be shimmed to less than 50 ppm. This value is approximately that of the Earth's magnetic field which would limit the ultimate resolution if not shielded.
Fig IV.12 Effect of combination of 5 shims. The locations and widths were designed to counter the magnetic field inhomogeneity.

Fig IV.13 Effect of adding the shim rings to the collimating lens. The combined effect is a 6 mm diameter range with homogeneity of 50 ppm. These curves were generated using a finite element magnetics simulator.

With the design of both the collimator lens and shim rings complete, fabrication problems would need to be solved for both structures. Since the shim rings require precision structures and placement on the micron scale, silicon fabrication was implemented instead of traditional machining. One of the greatest advantages of the cryogenic silicon etch is the high selectivity of the etch rate of photoresist over that of silicon. This advantage can be utilized for improving metallization lift-off on silicon.
Typically when lifting off a metallization layer using photoresist, care must be taken in obtaining resist sidewalls that are vertical or even slightly reentrant, and the photoresist has to be substantially thicker than the deposited metal layer. The fabrication approach described here transfers the difficult liftoff profile requirements from the photoresist to the cryogenic silicon etch. As we demonstrated with the silicon pillars, the sidewall profile is very easy to control and reproducible by optimizing the cryogenic etch parameters. The high selectivity improves the relative height between the top of the photoresist to the silicon surface being metalized thereby permitting thicker metal layers to be deposited. This enables creation of passive magnetic shims and electromagnetic coils by deposition of thick layers of iron into silicon. To the authors knowledge, this is the first time using the etch mask as also the metallization lift-off mask for deposition of thick metal layers on silicon.

To fabricate the iron rings, two inch p-type silicon wafer were cryogenically etched simultaneously to approximately 20 microns in depth to define the ring patterns with the various radii and width describe earlier. Etch conditions were identical to those describe previously and in Appendix A. With over 1 micron of photoresist remaining, iron was then thermally evaporated at a rate of 8 A/sec to a final thickness of approximately 6.5 microns. To reduce stresses from magnetic anisotropy, a 1 inch NdFeB N42 magnet was placed behind the wafer during evaporation [55]. Following metallization, liftoff was then performed in acetone. Thicker depositions typically failed due to the film stresses in the iron layer. It was typical to see layers peel up under what optically appeared to be tensile stress; this observation is consistent with the thermal coefficients of expansion for iron as compared to silicon.
To reduce the stresses at the expense of a more granular iron film, the wafer was cooled during evaporation. This cooling was achieved by placing a 4 inch diameter copper disc, ½ inch thick, behind the substrate. Immediately before evaporation, the copper was cooled in a LN2 bath, transferred to the evaporation chamber, and the chamber immediately pumped down. The copper then acted as a heat sink to remove the heat from the evaporated iron. This allowed for 3-5 microns of evaporation to be performed several times to achieve the desired film thickness of 10 microns. In addition to temperature, the trenches were broken up into segments which retained the ring structure. The basis behind this was to reduce the volumetric stress of a deposited layer.
Fig IV.15 SEM of iron shim rings embedded in a silicon substrate. By cryogenically cooling the substrate during evaporation, more than 10 microns of iron were deposited into the etched silicon.

Before the ring structure could be magnetically tested, a collimating lens was required to improve the homogeneity to closer to a 1000 ppm. Since the metallization layer to achieve 10 microns already proved a challenge from stresses, deposition of a 1 inch diameter 20 micron thick iron layer was not attempted. As an alternate route, highly ferromagnetic metallic glass was used from the Metglas Corporation. Metallic glass is a metal alloy in which its amorphous state is locked in during cooling; essentially there is no long range crystalline order. Typically this is done by rapid cooling of the metal from a liquid state. Metglas 2605s3a was selected for several of its properties. The quoted as cast susceptibility was > 20,000, the thickness was 0.7 mils (17.8 microns), and the saturation induction was 1.4 T. The technical specifications of this material can be found at http://www.metglas.com/downloads/2605s3a.pdf.
Initial testing at the time of this writing has shown mixed results. Although the Metglas proved to be highly ferromagnetic from observation in the magnetic field, measurements using the Hall Probe indicated otherwise. When the Metglas was placed in the field, a very strong attraction was noted between the magnet and the shim. Moreover, centering the shim resulted in curling of the edges of the shim to normal with respect to the magnet. This indicates that the shim is forcing the field to push field lines closer together. It could be interpreted that this implies a more homogeneous state. This most certainly is not a conclusive observation since the curling of the shim should also indicate that the field is reducing the reluctance across the gap by having a ferromagnetic material traversing it.

Magnetic field measurements indicated that the Metglas did have some effect. One layer, although theoretically should have flattened the field, actually made the field less homogeneous. But two layers appeared to make the field more homogeneous. Measurements over many shims under different mounting conditions had the same enigmatic results. Some configurations resulted in field flattening and some improved the field.

Fig IV.16  Magnetic field measurements using a Hall Probe mounted on a micrometer stage. Three conditions were tested, an unshimmed field (black), using one 1 inch diameter
Metglas 2605s3a shim (blue), and using two 1 inch diameter Metglas 2605s3a
shims (red).

It is quite likely that difficulty in measuring the homogeneity could be due to the
measurement device itself or part of the holder design [56]. Although the probe is rated to
measure 1 Gauss in a 3 Tesla field, it is not clear whether having the probe in the field
actually perturbs the field homogeneity. It is known that when shimming NMR machines
most operators use the measurement of the NMR spectra as the determining factor for the
true field homogeneity. Unfortunately, it is impossible to test the second lens before the
first lens is in place. The main reason is that the purpose of the second lens was to take a
known field and shim it to homogeneity. Placing the second lens in the magnetic field and
expecting it to operate correctly is akin to using a telescope objective without the main
telescope mirror. It is possible the field is homogeneous enough over a large enough
sample volume that it would be possible to measure spectra and use this to determine the
effects of shim additions. Indeed, it was noted that over a 1.5 mm, a sub 100 ppm field
homogeneity exists. Setting up a method to accurately measure the magnetic field to high
homogeneity is the next logical step for this project.

Copper Planar Microcoils

As a second major component of the portable NMR system, transmission and
detection coils were fabricated on silicon [57]. By creating the microcoils in silicon vice
winding copper coils from wire, the fabrication process can reduce the cost and increase
the repeatability of the microcoil [58,59,60,61,62,63]. This microcoil is designed to also act
as a resonator whose resonance is placed according to the gyromagnetic ratio of the
nuclei being detected. This section will detail the design of the microcoils both as an
electrical component in a circuit as well as the electromagnetic field generation. A fabrication sequence will detail how to create these microcoils in silicon using a single lithographic step. Finally, the electrical characteristics, both DC and AC, as well as the electromagnetic field are measured and described for the coils. It should be emphasized that this planar microcoil is designed for NMR applications but should not be limited to such. For example, this design is CMOS compatible so an ideal use might be increasing the inductance for use in an integrated switcher or for a microfluidic susceptibility detector [64].

The basis of the microcoil design was to optimize their signal to noise ratio (SNR) for use in NMR experiments [53,61,65]. In NMR experiments, changing the nuclei that are observed or changing the strength of the polarizing magnetic field also changes the Larmor frequency at which the signal is observed. Further, the signal to noise ratio of the experiment is proportional to the field produced by the coil, the noise generated by the Johnson resistance of the coil, and the number of nuclei being observed or volume of the sample. Hence, the design of the geometry of a NMR coil is initially based on maximizing the SNR for a chosen frequency, which then determined the required inductance and resistance of the coil.

\[ SNR = \frac{\gamma^3 h^2 * B^2 * \beta * I (I + 1) * N_{sample} * \int \frac{B_1}{current} dV}{3 * \sqrt{\frac{4 * \text{Resistance} * \Delta f}{\beta}}} \]

Here \( \gamma \) is the gyromagnetic ratio (\( \gamma = 42.58 \text{ MHz/T} \) for protons), h-bar is Planck’s constant, \( B \) is the polarizing magnetic field created by the permanent magnet setup, \( I \) is the spin (1/2 for proton), \( N_{sample} \) is the number of spins generating a signal per unit volume, Resistance is the total resistance of the coil, \( \beta \) is Boltzmann’s constant times the
temperature, \( \Delta f \) is the bandwidth of the circuit used, and the integral describes the magnetic field generated by the planar microcoil (\( B_1 \)) over the sample volume per Amp.

To achieve the highest SNR, geometrically, the optimization of the microcoil involves the resistance, and the integrated terms. To some extent the bandwidth is also modified, but an external matching circuit was utilized to further reduce the bandwidth. To numerically model the microcoils, the classic NMR SNR equation is recast into a more transparent form.

\[
SNR = \frac{\omega \cdot M_o}{\sqrt{4 \cdot \text{Resistance} \cdot \Delta f \cdot \beta}} \int B_1 \cdot \text{current} \cdot dV
\]

\[
M_o = \frac{N \gamma^2 h^2 (1 + 1) B_0}{3 K_B T} \approx 0.0032021 \text{ Amp m}^{-1}
\]

To accurately model the electromagnetic field of the coil, FEMM was employed to simulate the microcoil around the frequency of interest. The simulations were performed for an increasing number of coil turns to determine the optimal number. This simulation permits coupling of the coil's turns and accounts for skin depth in the copper conductor (approximately 9.5 microns at 50 MHz) and assumed a 1.15 T polarizing field (\( \omega = \gamma B_o \approx 50 \text{ MHz} \)). Four starting radii were selected to test the silicon based microcoil detection; 980 micron, 730 micron, 480 micron and 230 micron radii. All of the coils had wire widths of 40 microns at 70 micron center-to-center spacing based on what was achievable from the fabrication process. The sample volume of all the simulations incorporated a volume of diameter equal to that of the first turn of the microcoil and a height determined by a radius to height ratio of 0.08. From the simulations, several parameters were retrieved, most importantly the integral over the volume, the resistance at high frequency, the magnetic
field the microcoil can generate from 1 Amp of current, and approximation of the signal size to be detected.

**Fig IV.17** Simulation of B$_z$ field for a 500 micron radius planar microcoil. The simulation was run at 50 MHz for a 2 turn microcoil. These FEMM simulations allowed for the signal to noise ratio to be optimized.

**Fig IV.18** Simulation of the signal to noise ratio for the various microcoils. These FEMM simulations allowed for the signal to noise ratio to be optimized.
Using the simulations it was determined that for the 1000, 750, and 500 micron radius coils, 2 turns would be used and only 1 turn for the 250 micron radius coil. As a verification of the simulations, an analytical solution was numerically calculated in Mathematica for the 2 turn coils. To calculate the magnetic field, the full solution to a planar coil was used [66].

\[
B_z(\rho, z) = \sum_{n=0}^{1} \mu \frac{\rho}{\sqrt{((R + \delta n)^2 + z^2)} \cdot (EllipticK \left[ \frac{4 \cdot (R + \delta n) \cdot \rho}{\sqrt{((R + \delta n)^2 + z^2)} \right] + \frac{((R + \delta n - \rho)^2 - z^2)}{((R + \delta n - \rho)^2 + z^2)}}
\]

The summation was used to account for each of the coil’s turns but did not include the inductive coupling from one turn to another. A similar summation was used to calculate resistance with the width of the wire limited to 2 times the skin depth for copper (9.4 microns). A final assumption was that the substrate has no conductivity which would otherwise degrade the inductance. Although these three assumptions assist in making the calculations tractable, they do not accurately model the coils. In fact the skin depth adds considerably more resistance at 50 MHz than modeled and reduction of the inductance due to coupling and the substrate will be seen to dramatically decrease the ‘Q’ of the inductor [67]. However, the calculation does serve as a validity check for the simulations. The results from the calculations, found in the Appendix, are seen in the following table:
Using the optimum coil radii, the fabrication sequence was designed. The fabrication sequence began as a standard lithography and plasma etching sequence. On P⁺ silicon 3 inch <100> wafer, a 1.6 micron thick AZ 5214e photoresist is patterned in accordance with the fabrication recipe given in the Appendix. The pattern consisted of two sets of the 4 different diameter coils on a soda-lime glass and chrome photo mask; the mask was generated using a Heidelberg Laser Mask writer with approximately 1 micron resolution. Using this photo mask, the resist on the silicon was optically patterned. Immediately following the patterning, a cryogenic etch was performed to achieve approximately 25 microns in depth. Since the cryogenic etch has such a very high selectivity, most of the photoresist remained.
Fig IV.19 Cross sectional SEM of a microcoil ridge separating two trenches where copper was to be deposited. The cryogenic silicon etch was masked with 1.6 microns of resist. Following the etch, an insulating 1.6 micron thick silicon dioxide layer was PECVD deposited.

At this point, one of two techniques of low temperature chemical vapor deposition (CVD) were used to deposit an insulating layer of silicon dioxide. This insulating layer prevented the current from leaving the copper wire runs and going to the substrate. This layer also created a parasitic capacitance which will be discussed later. The first technique utilized an ICPRIE fitted with a gas ring around the table. This unique gas ring configuration permits the injection of 5% Silane diluted with nitrogen, 5%-SiH₄/N₂, into the chamber for creation of a plasma. When nitrous oxide, N₂O, is injected into the plasma the result is a recombination of the silicon atom and the oxygen atom to create a silicon dioxide deposition. This technique is referred to as ICP-CVD. This method of deposition is advantageous since no Fwd power is required and the table temperature is approximately 90 C. The low temperature prevents the resist from cross-linking or burning. A very dense layer of silicon dioxide deposits at a rate of approximately 18 nm per minute and
typical deposition times were 2 to 8 minutes; 8 minutes results in approximately 140 nm. To improve the adhesion of metal to the silicon dioxide layer, a 2 min deposition of amorphous silicon was deposited; the recipe is the same as the silicon dioxide but the nitrous oxide flow was stopped.

<table>
<thead>
<tr>
<th>SiH₄/N₂</th>
<th>100 sccm</th>
<th>ICP Power</th>
<th>2000 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>N₂O</td>
<td>15 sccm</td>
<td>Fwd Power</td>
<td>0</td>
</tr>
<tr>
<td>Temperature</td>
<td>90 C</td>
<td>Pressure</td>
<td>5 mT</td>
</tr>
</tbody>
</table>

A second technique for silicon dioxide deposition was using plasma enhanced chemical vapor deposition (PECVD). This instrument was also an Oxford Instruments Plasmalab System 100 but is physically different from an ICPRIE in that it does not have an ICP coil. Instead, the machine uses a CCP with both a 13.56 MHz RF power supply and a low frequency power supply. The low frequency supply has an output low pass filter which limits the output frequency to less than 100 KHz. The addition of the lower frequency power supply permits stress built up during the deposition to be controlled. Since the plasma is not as dense as the ICPRIE, the table temperature is required to be much hotter to achieve a similar density in the layers when compared to the ICP-CVD; standard temperatures are 350 C to 400 C. Since photoresist was used in this process, the temperature was limited to less than 150 C, reducing the quality of the layer. Typical deposition rates using this machine were 65 nm per minute and were typically run for 20 seconds. Again to achieve better adhesion between the metal and oxide, by stopping the nitrous oxide gas flow a thin layer of amorphous silicon was deposited.
Fig IV.20 Deposition rate of low temperature PECVD of Silicon Dioxide. Data was fitted to a linear deposition rate of 42 nm per minute with an offset of 207 nm. This data is untested for less than 20 minute deposition times.

Upon completion of the silicon dioxide insulating layer, one final step was needed before deposition of the copper. This step was exposing clean silicon substrate at the end of the innermost wire run. Having clean, highly doped P-type silicon and copper come into contact, an Ohmic tunnel-junction could be made. An Ohmic contact is made by one of 2 methods: matching the metal and semiconductor work functions to lower the barrier height
or by making a very thin depletion region where the current can tunnel through [42].

For this device, since copper was used to reduce the expense, the junction width was instead reduced by using highly doped silicon. The barrier width was approximated as an ideal Schottky diode using a $P^+$ silicon doping of 1019 cm$^{-3}$, a copper work function of 5.10 V and a silicon work function of 4.72 V.

$$W_d \sim \frac{2 * \varepsilon_{si}}{q * N_A} \left( E_g - \left( \phi_{cu} - \chi_{si} \right) \right) \sim 9.8 \text{nm}$$

This contact permitted the current travelling through the coil to be shunted to the substrate and picked up on the backside of the wafer eliminating the need for a bridging contact from the center of the coil to the outside of the coil. This idea created a truly planar silicon microcoil where microfluidics or another silicon wafer could be bonded to the surface. By etching a pillar at the end of the innermost wire, a diamond scribe could be brought in to fracture off the pillar, thereby exposing clean silicon.

Fig IV.21 SEM of the center contact after being mechanically cleaved off and copper thermally evaporated over the clean $P^+$ silicon. This contact established an Ohmic tunnel-contact from the copper microcoil to the substrate eliminating the need for a bridging wire and the required additional fabrication steps.
Immediately following the removal of the contact pillar, a thermal evaporation of copper was performed. The thermal evaporator used was pumped down to approximately $5 \times 10^{-6}$ Torr. The boats used were R.D. Mathis RDM-WBAO-3 alumina coated tungsten boats allowing for approximately fifteen 50 g copper slugs to be evaporated at the same time. This permitted approximately 5 microns per run to be deposited. Evaporation rates were approximately 20 – 40 Angstroms per second with a plate temperature set at 41 C. Upon completion of the evaporation, the sample was allowed to cool for two hours before vacuum was broken. To perform liftoff, the sample was immersed in acetone where the metal on top of the resist would peel off, usually in one single foil sheet leaving the copper in the etched trenches. To create the backside contact, the wafer was floated in BHF (floating denotes that the wafer was placed on top of the HF solution and would float on the top of the fluid so only the back side of the wafer made contact with the solution). The backside silicon was cleaned for 1 minute, rinsed with DI, dried with N2, and placed in the evaporator where 100-300 nm of copper was then evaporated.
At this point the wafer could be cleaved to make separate the planar microcoils for testing. A couple of points about the fabrication sequence should be highlighted. First, this fabrication sequence is significantly less complicated than any other sequence currently used to produce microcoils in silicon. This permits a high level of repeatability and reduces the fabrication costs per wafer. Second, by shunting the current to substrate, the need for multiple realignments or lithography steps is eliminated since the bridging contact is not needed. This also permits wafer bonding or PDMS bonding to be achieved. Finally, although only 1.6 microns of photoresist was used, up to 15 microns of thermally evaporated copper could be lifted off. Typically, if metallization is to occur, a thick photoresist layer is required which is approximately 3 times thicker than the desired metal thickness.
To confirm the fabrication work, the microcoils are first electrically tested under DC conditions. The first test uses an Agilent Semiconductor Parameter Analyzer 4155 to sweep biasing voltage negative to positive while measuring the current. Although this is a two probe measurement and has the problem of introducing series resistance in the measurement from the leads, it allows for the verification that the copper silicon contacts are indeed Ohmic vice a Schottky rectifying diode. This measurement does not provide an accurate measurement of contact or coil resistance. One aspect to note is that a current compliance was implemented in the measurement, so once this current is met any increase in voltage will not increase the current further. This is seen in the graphs as a diagonal line. The spike at zero is due to a numerical divide by zero calculation and a short circuit measurement of approximately 3.98 Ohms was made. The most important aspect of this measurement is that the copper-silicon junction is Ohmic to under 0.1 Ohms.
Since a 50 MHz AC signal is used for the NMR experiments, any rectification of the signal will introduce errors in the detection.

![Resistance Measurements for Planar Silicon Microcoils](image)

**Fig IV.24** Resistance of a 2 probe measurement of planar microcoils taken using an Agilent Semiconductor Parameter Analyzer. Measured lead resistance was 1.9 Ohms (from probe tip to probe tip). The diagonal line is when the machine enters current compliance and will not permit the current to increase. The flat resistance denotes that the copper silicon contact is Ohmic to under 50 mΩ.

To more accurately measure the DC resistance, a 4 point probe measurement was made using a Keithley 2400 source-meter. This type of measurement, also referred to as a Kelvin measurement, injects current into the device while using two other probes to measure the voltage across different components. Since the voltage measurement draws little to zero current, probing the device yields a more accurate measurement. The devices tested had an approximately 7 micron thick copper layer, half as thick as the calculations. The measured results are displayed with simulated results under DC conditions for a 15 micron thick layer. Comparison between the two resistances shows very good agreement upon a multiplier of 2 due to the thickness difference.
<table>
<thead>
<tr>
<th>Microcoil Radius (µm)</th>
<th>Measured Coil and Lead Resistance (Ω) ~ 7 micron thick copper</th>
<th>Simulated Coil and Lead Resistance (Ω) – 15 micron thick copper</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000 / 2 turn</td>
<td>0.716</td>
<td>0.375</td>
</tr>
<tr>
<td>750 / 2 turn</td>
<td>0.624</td>
<td>0.284</td>
</tr>
<tr>
<td>500 / 2 turn</td>
<td>0.326</td>
<td>0.194</td>
</tr>
</tbody>
</table>

To ensure the magnetic field generated was close to simulations, a Hall probe and LakeShore 455 Gauss meter was used to measure the $B_z$ field at the center of coil along the axis. Using the Keithley 2400 multimeter to supply 1 amp to the coils, the magnetic field was measured using the Hall probe on a 3 stage micrometer. First the center of the coil was determined in the 'x' and 'y' directions by finding the maxima. The Hall probe was then moved as close to the substrate as possible, the current turned off and the Gauss meter zeroed. This measurement was also normal to the Earth’s 50 µT magnetic field which eliminated this variable from the measurement. The current was then turned back on, and the probe lifted in 50 micron increments. This measurement permits the complicated magnetic field measurement to be simplified.

$$B_z(z) = \frac{n\mu l}{2} \times \left( \frac{R^2}{(R^2 + (Z + Z_o)^2)^{\frac{3}{2}}} \right)$$

Here, $n$ is the number of turns on the coil, $l$ is the current (1 Amp), $\mu$ is the permeability $R$ is the radius of the coil, and $Z$ and $Z_o$ the height above the coil and the offset from zero.
The collected data was then placed into Matlab for curve fitting using the radius and $Z_o$ as parameters to be fitted to the above equation. The offset is expected since the Hall probe device is embedded in the probe which is approximately 1 mm thick. A further addition to the offset is if the probe (approximately 6 inches long) is not exactly parallel with the substrate. By curve fitting the data with the offset, the maximum field strength and field profile can be determined for comparison with simulations. All of the curve fits resulted in R-squared values better than 0.95; the extra small coil was not able to generate a curve fit better than 0.85 and was not used. An interesting result was that the multiple turn coils had radius curve fit parameter best fit to a radius value exactly between the two turns. The collected data which indicates the field flattens is actually when the probe makes contact to the substrate.

![Bz(z) Field - Planar Microcoil](image)

**Fig IV.25** Magnetic Field measurements along the z-axis for the microcoils using a Hall probe and Gauss meter. The data, ‘x’, was curve fit using the radius and an offset from $z=0$ as the fit parameters to R-square values better than 0.95. The voltage required for driving the coils at 1 Amp were 2.57, 2.11, 2.42, and 1.64 volts for the large, medium, small, and extra small coils respectively.
Fig IV.26  Magnetic Field simulations in FEMM along the z-axis for the microcoils. This simulation was for a DC current of 1 Amp and shows very good agreement with measurements.

Although the DC measurements assist in confirmation that the planar microcoil operates as design, the microcoil was intended for use as a 50 MHz NMR detector. For this purpose, it was seen that the bandwidth of the microcoil needed to be as narrow as possible to reduce the detected noise. Desiring a narrow bandwidth is synonymously asking for a high ‘Q’. For this microcoil, the ideal ‘Q’ is the same for an ideal inductor.

\[ Q = \frac{\omega}{\Delta \omega} = \frac{\omega L}{R} \]

<table>
<thead>
<tr>
<th>Microcoil Radius (µm)</th>
<th>Simulated Resistance at 50 MHz (Ω)</th>
<th>Simulated Inductance at 50 MHz (H)</th>
<th>Simulated ‘Q’ at 50 MHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000 / 2 turn</td>
<td>1.476</td>
<td>15.84 *10^{-9}</td>
<td>3.4</td>
</tr>
<tr>
<td>750 / 2 turn</td>
<td>0.9803</td>
<td>11.74 *10^{-9}</td>
<td>3.8</td>
</tr>
<tr>
<td>500 / 2 turn</td>
<td>0.5258</td>
<td>7.50 *10^{-9}</td>
<td>4.5</td>
</tr>
</tbody>
</table>

These ‘Q’ values are significantly lower than handwound coils where more typical ‘Q’ values are in the range of 30. The values are also much lower than current published work on
planar microcoils for NMR. Massin et al. demonstrated ‘Q’s of 17-19 for similar
shaped microcoils fabricated on glass slides but operated at 300 MHz (approximately 6
times the frequency). It should be noted that their fabrication sequence required the use
of a bridging contact. Taking the frequency into account, these coils should have a
comparable ‘Q’. It was hypothesized the low ‘Q’s in designed microcoils might be due to
the highly resistive silicon substrate used. To test this, simulations were performed at 46
MHz using the 1000 micron radius coil, the large coil. The substrate resistivity was then
adjusted to the following values and simulated: 5 mΩ-cm, 10 Ω-cm, and 1000 Ω-cm. The
simulated ‘Q’s were noted to increase rapidly from 3.46, 11.58, and 11.60 respectively.
Unfortunately, the Ohmic center contact relied on the highly doped silicon; 10 Ω-cm has an
approximate doping of $10^{15}$ for a depletion width of 980 nm, and 1000 Ω-cm has an
approximate doping of $10^{13}$ for a depletion width of 9.8 microns. These barrier widths
would not permit the bridgeless Ohmic tunnel contact. The ‘engineering trade-off’ made
then is the fabrication simplicity for a reduced ‘Q’. One might argue that the copper runs
should be made thicker in order to reduce the resistance. Unfortunately, the skin depth of
9.4 microns makes this task have diminishing returns after about 10 microns. One
potential direction is to use a thick epitaxial P⁺ deposited on a 10 Ω-cm substrate; when
the Ohmic contact is made it would be using P⁺ silicon but the losses due to the substrate
can be dramatically reduced.

To externally meet the demands of using a narrow bandwidth, a discrete component
circuit was designed, simulated, and tested. This discrete circuit is very similar to the
matching circuit used to tune ICP coils described in Chapter 1 and that analysis will be
referred to here. Since each coil run is insulated from the substrate by a thin oxide layer,
this parasitic capacitance needs to be accounted for. To do this the areal foot print is
broken into two parts, the area under the coil and the area under the contact pad. The thickness of the oxide layer defines the dielectric thickness; since thermal evaporation has very poor step coverage, it is assumed that the sidewalls contribute negligible capacitance. Then using the simulated inductance and resistance, the parasitic devices can be accounted for. An approximation of 0.5 Ω for the Ohmic contact resistance is used.

<table>
<thead>
<tr>
<th>Microcoil Radius (microns)</th>
<th>Coil Area ((10^{-9} \text{ m}^2))</th>
<th>Coil Capacitance 140 nm oxide</th>
<th>Pad Area ((10^{-6} \text{ m}^2))</th>
<th>Pad Capacitance 140 nm oxide</th>
<th>Simulated Inductance (nH)</th>
<th>Simulated Resistance (Ω)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000 / 2 turns</td>
<td>520.25</td>
<td>1.28318E-10</td>
<td>1.372</td>
<td>3.384E-10</td>
<td>15.84</td>
<td>1.48</td>
</tr>
<tr>
<td>750 / 2 turns</td>
<td>394.58</td>
<td>9.7322E-11</td>
<td>2.441</td>
<td>6.02066E-10</td>
<td>11.74</td>
<td>0.98</td>
</tr>
<tr>
<td>500 / 2 turns</td>
<td>268.92</td>
<td>6.63283E-11</td>
<td>4.617</td>
<td>1.13877E-09</td>
<td>7.5</td>
<td>0.53</td>
</tr>
</tbody>
</table>

Careful account of the amount of capacitance the pad area and the oxide thickness contributes permits the planar microcoils to attain a ‘natural’ resonant frequency. Hence the silicon planar microcoils are designed to have an integrated resonant frequency. The naïve calculation using only the capacitance and inductance yields the following frequencies.

<table>
<thead>
<tr>
<th>Microcoil Radius (microns)</th>
<th>Coil Resonance (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000 / 2 turns</td>
<td>58.54</td>
</tr>
<tr>
<td>750 / 2 turns</td>
<td>55.54</td>
</tr>
<tr>
<td>500 / 2 turns</td>
<td>52.94</td>
</tr>
</tbody>
</table>

Although having the circuit tuned automatically based on geometrical and fabrication controls is useful for a theoretical circuit, inevitably experimental variations in a microfab setting introduce variations to device parameters. Experimental engineers are commonly
heard cynically stating, “the simulations are amazing.” To account for the experimental variations, two trimmer capacitors are utilized in configurations similar to that of the ICP power matching circuit [57]. This circuit was simulated using Top Spice (a graphical circuit simulator) using the solved for $C_1$ and $C_2$ nominal values. It was found that approximately 150 pF was needed to tune the coil down to 50 MHz region (the parallel capacitor) and several nano Farads were need to match the phase (the series capacitor). This circuit was implemented on a PCB board with surface mounted capacitors. The silicon microcoil was placed flat on the board with the backside making contact to copper PCB runs. The silicon was held in place using a modified copper alligator clip; this clip was trimmed to the width of the contact pad and was used to make electrical contact to the planar microcoil. Two non-ferromagnetic tunable capacitors which ranged in value from 0-120 pF were used in parallel with a 85 pF Tantalum capacitors to act as the tunable parallel capacitor. For the series capacitor, two of the 0-120 capacitors were used.

Fig IV.27  Top Spice schematic of the large planar microcoil. This model includes the parasitic capacitances of the coil and contact pad, the coil, lead wires, and Ohmic contact resistances, and adds matching capacitors $C_1$ and $C_2$ (used to tune the circuits resonance).
Fig IV.28  Top Spice simulation of the large planar microcoil. This model includes the parasitic capacitances of the coil and contact pad, the coil, lead wires, and Ohmic contact resistances, and adds matching capacitors $C_1$ and $C_2$ (used to tune the circuits resonance).

The frequency measurements were performed on an Agilent 8712 ET Network Analyzer with frequency sweeps generally from 0.3 to 100 MHz; refined sweeps were used for more accurate measurements. With a 50 ohm coax cable, the machine was normalized (effectively zeroing out the reading) after a self calibration. Whenever the frequency range or type of measurement was changed, this normalization procedure was performed. As an external check, a 50 ohm termination plug was used to verify accuracy. The first measurement was to measure the ‘Q’ of the circuit holder; at 50 MHz and tuned with the capacitors the ‘Q’ was approximately 262.
Fig IV.29  Reflectance measurement using a Network Analyzer of the microcoil chip holder. The measured 'Q' is approximately 262, with the y-axis in dB.

Next the microcoils were measured using same technique. For this particular set of microcoils, 20 mΩ-cm resistivity P⁺ silicon was used. As noted earlier, less conductive silicon resulted in higher 'Q' values. A typical measurement of microcoils fabricated on 5
mΩ-cm resistivity P⁺ silicon yielded ‘Q’ values of 7.4, 3, 1.5, and 1.3 for the extra small, small, medium and large microcoils respectively. The increase in resistivity yielded significantly better ‘Q’s, 22, 5.9, 7.0, and 6.3 respectively.

With the coils tuned to the correct frequency, the next test is to place the coils in the magnetic field and run NMR pulse sequences and analyze the detected signal. By measuring the decay rate of a known signal, say water, the decoherence rate can be measured. This decoherence can be shown to be a combination of the natural decay rate plus the inhomogeneity of the magnetic field. For an apparatus such as the one built here, a good approximation is that the inhomogeneity of the field dominates.

\[ \frac{1}{T_{2}^*} = \frac{1}{T_{2}} + \gamma \Delta B_0 \]

Here \( T_{2}^* \) describes the total decoherence time, \( T_{2} \) describes the natural decoherence time, \( \gamma \) is the gyromagnetic ratio, and \( \Delta B_0 \) is the magnetic field inhomogeneity. For the unshimmed magnetic field described earlier and assuming a natural decoherence time of a few hundred milli-seconds, the field would need to be shimmed to better than 1 ppm to see the natural decoherence times. For this reason, it is typical to measure the shimming of the magnetic fields using these coils while simultaneously backing out information on the exact SNR. Further description of the microcoils will need to wait until the magnetic field can be shimmed to a useful homogeneity.

**Silicon Micropillars Point Schottky Diodes**

To understand the contact made between the silicon nanowires and the tungsten probe tip, micropillars were utilized for their much lower surface to volume ratio. These devices were fabricated using identical silicon and cleaning methods as those used for the nanowires and tested in a manner identical. The information gathered demonstrated
several experimental aspects which were hypnotized but untested for the nanowires.

One of the differences seen between the micropillars and the nanowires was due to the size of the probe tip in relation to the wire itself. This section will detail the work performed, methods used, and results.

This fabrication sequence was a combination of the nanowire and cryogenic etching. Using 2" P⁺ silicon wafers, crystal orientation of <100>, photoresist was placed on the wafer and patterned using the hexagonal hole pattern described in chapter 1. Using resist reversal 50, 20, 10, and 5 micron diameter discs were patterned on the silicon in hexagonal arrays separated by lengths equal to their diameters. A silicon cryogenic etch was then performed for 25 minutes under the following conditions:

<p>| | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>SF₆</td>
<td>70 sccm</td>
<td>ICP Power</td>
<td>900 W</td>
</tr>
<tr>
<td>O₂</td>
<td>6.5 sccm</td>
<td>Fwd Power</td>
<td>8 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-130 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

The pillar arrays were then measured in a Nova 600 dual beam SEM for the diameters and heights: 50.90/26.87, 21.14/25.46, 11.75/25.19, and 5.81/23.25 microns. The variation in etch height, although etched at the same time, is due to aspect ratio dependent etching discussed and described in Chapter 1. The resist was then removed using acetone. A silicon cleaning, identical to that performed for the nanowires, was then performed. This consisted of three cycles of: RCA 1 cleaning (3:1.5 of NH₄OH:H₂O₂ at 90C) for 3 minutes, DI rinse, 1 minute of BHF clean, followed by DI rinse. Immediately before testing, the sample was BHF dipped for 1 minute to hydrogen terminate the dangling silicon bonds on the surface.
Upon completion of cleaning, the pillars were mounted on a 90 degree probe stage in the Quanta SEM using copper adhesion tape. One probe contacted the copper tape on the back side while one probe tip was carefully brought down to make contact with the top of the pillar being tested. The probe tips were electrically connected to an Agilent Semiconductor Parameter Analyzer 4155 C for I-V curve generation. During measurement, the SEM beam was blanked to prevent electron beam induced charge carriers from being produced. The internal IR camera was also turned off to prevent photo-generated carriers from being produced.

![SEM image](image.png)

**Fig IV.31** SEM taken in the Quanta as a 10 micron diameter pillar was contacted with a tungsten probe tip.

What had been assumed with the nanowires was that the highly doped silicon and tungsten probe tip would make an Ohmic tunnel contact and that the area of the backside diode was large enough to make the resistance the diode contributed negligible (in effect, making the backside contact an Ohmic contact). Qualitatively what was seen
fundamentally with a positive voltage on the probe tip and ground on backside, was as follows: a reverse biased point contact diode from the tungsten probe tip to the top of the silicon micropillar. The backside contact seemed to be an Ohmic contact as predicted. The tungsten-silicon diode is described by the classical Schottky diode equation:

\[ J = J_o \left( \frac{V_p}{e^{\eta V_T}} \right) = A^{*2} T^2 \cdot e^{-\Phi_{BP}/\eta V_T} \cdot e^{\frac{V_p+\Delta \Phi}{V_T}} \]

In these equations, it is assumed that the voltage across the diode is more than a few \( K_b T/q \) so the '-1' term can be ignored. Here \( \eta \) is the ideality factor, \( J_o \) is the saturation current density, \( \Phi_{BP} \) is the junction barrier height, \( \Delta \Phi \) is the voltage dependant barrier height lowering and \( V_{T1} \) is \( K_b T/q \) or 0.02582 V. In reverse bias, the leakage current is approximated to be \( J_o \) and any voltage dependence is due to image charge barrier height lowering. Since the probe contact is small, the current density is determined by approximating the area of the probe contact as the diode area. This area is the same for all the pillars. As a test case, the probe was also placed on the substrate and the I-V curve measured.
I-V measurements of the silicon micropillars etched 25 microns tall. The pillars were cleaned, mounted in the SEM, and measured identically to that of the nanopillars. The tungsten probe tip creates a Schottky diode and the backside contact is Ohmic.

Micropillar measurements were conducted and plotted using I-V curves. It should be noted that although the same size probe tip is used on all the pillars, and hence the area of the Schottky point contact diode is the same in all cases, the curves are very different. This difference was needed to be understood since this contact method was also being used for the nanowire measurements.

The difference in pillars is the combination of two effects. The first effect is that the barrier potential was different for all of the measurements due to the contact. If the probe was pressed down more on the silicon, the contact improved. Unfortunately, the same contact conditions were impossible to reliably replicate from pillar to pillar. This effect can be better understood by looking at a metal-insulator-semiconductor structure. The presence of a thin oxide layer can trap surface states and generally alter the barrier potential. Sze et al. solved this problem for thermionic emission currents to have an exponential modification:
\[ J = A^{\ast}T^2 \cdot e^{-\sqrt{T\delta} \left( \sqrt{\frac{4m^*}{\hbar^2}} \right)} \cdot e^{-\Phi_B \delta / \nu T} \cdot e^{-\Phi_B / \nu T} \]

In the added exponential term \( \xi \) is the effective change in the barrier and \( \delta \) is the barrier width. To remove this effect, the barrier height for each pillar was extracted and replaced with a theoretical or ideal barrier height. The ideal value used was approximated from reported work functions and calculated to be approximately 0.65 V.

\[ \Phi_B = E_g - (\varphi_w - \chi_{si}) \]

The measured barrier height was extracted from the reversed biased diode leakage current. In reverse bias the leakage current is approximately \( I_0 \) with a small voltage dependence due to image charge barrier height reduction. Note that variations in the Richardson’ constant does not significantly change the barrier potential.

\[ \Phi_B = \nu_{ih} \cdot \ln \left( \frac{A^{\ast}T \text{ Area}}{I_o} \right) \]

The difference between the ideal and actual barrier potential was then used to adjust the measured current. Values for the measured barrier heights were typically 0.49 v - 0.52 v. For the calculations, an approximate 0.5 v barrier height was used; the value was reduced from the ideal barrier height to account for image charge barrier height lowering. Errors in this assumption will not affect the results here, since any error only linearly scales the values. What is important for this analysis is the relative barrier heights. Once the barrier height variation was removed, the I-V curves then displayed a pattern of increasing current as the pillar diameter was increased. The substrate contacted diode was the curve interpreted to be as close as possible to representing an ideal Schottky point contact diode.
Fig IV.33 I-V measurements of the silicon micropillars etched 25 microns tall. The change in barrier height from the ideal height of 0.5 V was removed.

The second effect seen was due to the series resistance incurred due to the height of the pillars. Ideally, since the pillar radius is decreased from 50 microns to 5 microns while keeping the height the same, the resistance the pillar offers to the Schottky point contact diode also increases. This series resistance provides a negative feedback to the diode and acts to reduce the current. This effect is accounted for in the ideal diode equation by modification of the diode voltage. The measured voltage applied to the diode is reduced by voltage dropped across the resistor. Unfortunately this equation is a transcendental equation with no solution and is best understood using SPICE simulators.

\[ I = I_0 \left( e^{\frac{V_{d}-IR}{nV_T}} - 1 \right) \]

Based on the geometry of the pillar, the ideal resistances were calculated to be 44, 12, 3.5, and 0.7 ohms for the 5, 10, 20, and 50 micron diameter pillars respectively. To demonstrate this effect, a circuit simulation was run for an ideal diode in series with
resistors of the same values. To graphically compare this effect, an ideal diode with no series resistance was added to the plot.

Fig IV.34  I-V simulations of an ideal diode in series with a resistor. The resistor values were 0 (blue), 0.7 (red), 3.5 (green), 12 (cyan), and 44 (purple) ohms.

Although, the effect is qualitatively the same the ideal resistance does not take into account the fact that the pillar is actually a point contact. Appendix E calculates the effect using point contacts have on a given aspect ratio planar sheet. Essentially, since the current does not use the full area of the resistor, the actually resistance is much higher than calculated for low aspect ratio structures. This calculation was performed using a current sheet, but was used as an approximation for a cylinder here. The modified resistances used were 41, 24, 17 and 9 Ohms respectively. What was seen does a shift down away from the ideal diode into a configuration closely resembling that which was actually measured.
Fig IV.35  I-V simulations of an ideal diode in series with a resistor modified to account for the point contact. The resistor values were 0 (blue), 9 (red), 17 (green), 24 (cyan), and 41 (purple) ohms.

Although these micropillars were not fabricated for use as an actual device, careful examination I-V measurements helped to understand what effects should be expected from probing the silicon nanowires using the FEI Quanta SEM with the integrated tungsten probe station. The micropillars were prepared in exactly the same method as the silicon nanowires were on the same silicon substrate, mounted in the SEM and probed identically. Fundamentally, what was observed was that contacting to the back of the silicon substrate, coated with gold, and provided an ideal Ohmic contact. This is valuable knowledge in that any curvature seen for the silicon nanowires can be attributed to the nanowire itself. Further, although the silicon was highly doped to provide a tunneling Ohmic contact, what was actually observed was a Schottky point contact diode where the tungsten probe tip came into contact with silicon micropillar. Furthermore, each time the probe contacted the pillar, variations in barrier energies were seen. This is critically important because it establishes the fact that contacting to the silicon directly will yield
variations in the I-V measurements making this method of directly probing unacceptable. It was also seen that the relative change in barrier heights could be extracted to yield the relative changes in barrier potential. The pillar itself also modified the I-V characteristics. This was due to the fact that each pillar introduced a series resistance, which could not be described classically. Instead the fact that a point contact was used actually increased the resistance.
Appendix A – Fabrication Recipes

Resist Patterning

*Photoresist – Clarion AZ 5214e*

This recipe patterns a silicon wafer (1 to 4 inches) with a 1.6 micron thick layer of patterned photoresist. The prebake and exposure steps are significantly longer than suggested by the manufacturer, but have proven to be invariant against small perturbations seen frequently in microfabrication facilities. Optional steps are denoted with an asterisk.

1. *Clean wafer with Acetone, Isopropyl Alcohol, Methanol, DI water.
2. *Dehydration bake on a hotplate at 120C for 3 minutes.
3. Spin AZ 5214e at 6000 rpm, Acl speed of 9, for 1 minute.
4. Prebake on a hotplate at 95C for a minimum of 3 minutes.
5. Lithographically expose for 52 seconds under hard mask with a 350 Hg line at 275 Watts.

At this point, the resist can be developed for use as a positive resist. If a negative resist is needed, then the following reversal step can be made.

- Reversal bake on a hotplate at 120C for exactly 1 minute. This step is critical and excessive deviations will result in pattern transfer.
- Flood expose for 52 seconds under hard mask with a 350 Hg line at 275 Watts.

Both the normal and reversed patterns continue on at this point.

6. Develop in MF 322 for 20 seconds (normal) or 25 seconds (reversal).
7. *Reflow the resist if necessary on a hotplate at 160 C for a few seconds.

*Electron beam resist – PMMA 950 A2*

This recipe patterns a silicon wafer with approximately 50 nm of electron beam resist. The exposure is conducted using an electron beam writer in the KNI at Caltech.
1. *Clean wafer with Acetone, Isopropyl Alcohol, Methanol, DI water.
2. *Dehydration bake on a hotplate at 120C for 3 minutes.
3. Spin PMMA A2 at 2500 rpm for 1 minute.
4. Prebake on a hotplate at 180C for a minimum of 5 minutes.
5. Beam expose using a approximately a 7nA. Typical write speeds are 34 MHz and doses are 900 to 100 micro-micro coulombs.
6. Develop in a 3:1 mixture of Methly-Isobutyl-Ketone (MKIB) and Isopropyl Alcohol.

**Silicon Cleans**

*RCA -1 and BHF Clean Cycle*

This clean cycle was routinely used to ensure both removal of the alumina etch mask, polymer from pseudo Bosch etching, and to ensure that the surface states were hydrogen passivated and ready for metallization. By performing this clean cycle, contacting to P silicon using both copper and gold yielded Ohmic contacts repeatably.

1. Heat 15 mL of NH4OH to 90 C on a hotplate (temperature stabilization is not critical since addition of other chemicals will result in exothermic reactions).
2. Add 5 mL of H2O2 to the heated solution. Bubbles should begin to appear (similar to 7-up soda).
3. Place silicon sample in solution for 3 minutes.
4. Remove silicon sample and rinse in DI.
5. Place silicon sample in BHF for 1 minute.
6. Remove silicon sample and rinse in DI.
7. Repeat steps 3-6 three times. Upon completion of final step, N2 dry the sample. Sample should be evaporated or placed into an N2 environment as quickly as possible.

**Etch and Deposition Recipes**

*Cryogenic Silicon Etch*

This etch recipe allows for a silicon etch, described in detail in this thesis, for a silicon etch rate of $E_o = 1.14$ microns per minute and an aspect ratio coefficient of $b = 0.04099$. 
This etch was verified in 3 different Oxford Plasmalab 100s ICPRIE 380s. Modification and control over the etch is also described in detail in this thesis. It is recommended that Fomblin oil be used for adhesion of silicon pieces to a carrier wafer. Fomblin oil can be removed using Isopropyl Alcohol or an oxygen plasma.

<table>
<thead>
<tr>
<th>SF$_6$</th>
<th>70 sccm</th>
<th>ICP Power</th>
<th>900 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>O$_2$</td>
<td>5 sccm</td>
<td>Fwd Power</td>
<td>5 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>-120 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>

_Pseudo Bosch Silicon Etch_

This etch recipe allows for a silicon etch, described in detail in this thesis, for a silicon etch rate of approximately 175 nm per minute. This etch was verified in 2 different Oxford Plasmalab 100s ICPRIE 380s. Modification and control over the etch is also described in detail in this thesis. It is recommended that Fomblin oil be used for adhesion of silicon pieces to a carrier wafer. Fomblin oil can be removed using Isopropyl Alcohol or an oxygen plasma. This etch creates silicon nanopillars using alumina as an etch mask. If this etch is used with a Gallium implanted etch mask, a modification to the etch is needed. This modification is C$_4$F$_8$ tuned down to 50 sccm and Fwd power tuned down to 10 W.

<table>
<thead>
<tr>
<th>SF$_6$</th>
<th>33 sccm</th>
<th>ICP Power</th>
<th>1200 W</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$_4$F$_8$</td>
<td>57 sccm</td>
<td>Fwd Power</td>
<td>20 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>15 C</td>
<td>Pressure</td>
<td>10 mt</td>
</tr>
</tbody>
</table>
Silicon Dioxide Etch

This etch recipe allows for a silicon dioxide etch, described in detail in this thesis, for a silicon etch rate of approximately 600 nm per minute. This etch was verified in 2 different Oxford Plasmalab 100s ICPRIE 380s. Modification and control over the etch is also described in detail in this thesis. It is recommended that Fomblin oil be used for adhesion of silicon pieces to a carrier wafer. Fomblin oil can be removed using Isopropyl Alcohol or an oxygen plasma. Selectivity using a chrome mask on a quartz wafer is 33:1.

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<thead>
<tr>
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<tbody>
<tr>
<td><strong>O₂</strong></td>
<td>2 sccm</td>
<td>ICP Power</td>
<td>2100 W</td>
</tr>
<tr>
<td><strong>C₄F₈</strong></td>
<td>45 sccm</td>
<td>Fwd Power</td>
<td>200 W</td>
</tr>
<tr>
<td><strong>Temperature</strong></td>
<td>20 C</td>
<td>Pressure</td>
<td>7 mt</td>
</tr>
</tbody>
</table>

Bosch Silicon Etch

This etch recipe allows for a silicon etch, described in detail in this thesis, for a silicon etch rate of approximately 900 nm per cycle (3.6 microns per minute). This etch was used in an Oxford Plasmalab 100s ICPRIE 380s modified with the mass flow controllers situated on top of the etcher. It is recommended that Fomblin oil be used for adhesion of silicon pieces to a carrier wafer. Fomblin oil can be removed using Isopropyl Alcohol or an oxygen plasma. Etch time was 15 seconds and deposition time is 10 seconds.

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<tbody>
<tr>
<td><strong>SF₆</strong></td>
<td>160 sccm</td>
<td>ICP Power</td>
<td>1750 W</td>
</tr>
<tr>
<td><strong>C₄F₈</strong></td>
<td>0</td>
<td>Fwd Power</td>
<td>30 W</td>
</tr>
<tr>
<td><strong>Temperature</strong></td>
<td>15 C</td>
<td>Pressure</td>
<td>20 mt</td>
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</tr>
<tr>
<td>SF₆</td>
<td>0</td>
<td>ICP Power</td>
<td>1750 W</td>
</tr>
<tr>
<td>C₄F₈</td>
<td>140 sccm</td>
<td>Fwd Power</td>
<td>10 W</td>
</tr>
<tr>
<td>Temperature</td>
<td>15 C</td>
<td>Pressure</td>
<td>20 mt</td>
</tr>
</tbody>
</table>
Appendix B – Conductance of Etch Products from a Trench

In order to show that aspect ratio dependent etching is not due to the etch product preventing the incoming etch gas from reaching the substrate, one needs to show that the conductance of the trench or hole at the etching pressure permits such gas transfer. Knudsen calculated the fundamental relation of conductance of a tube to be:

\[ C = \frac{4}{3} \int_0^{\text{length}} \frac{v_a}{\text{Perimeter}^2 \text{Area}} \, dl \]  
(B-1)

\[ v_a = 145.5 \, \text{[m/sec]} \times \sqrt{\frac{T}{M_p}} \]  
(B-2)

Where \( v_a \) is the average gas velocity, \( T \) is the temperature, \( M_p \) is the molecular weight of the etch product, and the units of the integral are in cm. Then the number of gas molecules per second that are able to flow from the base of the etched hole or trench to the chamber is given by:

\[ v = C \times (n_2 - n_1) \]  
(B-3)

Where \( n_i \) is the number of molecules per cubic centimeter at the given pressure. Now using the ideal gas law to substitute in for \( n \):

\[ v = \frac{8}{3} \int_0^{\text{length}} \frac{2}{\text{Perimeter}} \sqrt{\frac{T}{M_p}} \times \frac{145.51}{4 K_B 10^5} \times \frac{\Delta P_{\mu\text{bar}}}{T} \]  
(B-4)

\[ v = \frac{8}{3} \int_0^{\text{length}} \frac{2}{\text{Perimeter}} \sqrt{\frac{1}{T+M_p}} \times 2.635 \times 10^{19} \times \Delta P_{\mu\text{bar}} \]  
(B-5)
For calculating the mass flow rate of the gas, take the weight and the velocity. For either a circle or square with length or radius of ‘a’:

\[ \text{n} \text{v} = \frac{8}{3} \times a \times A \times \sqrt{\frac{T \times M_p}{6.023 \times 10^{23}}} \times \frac{2.625 \times 10^{19}}{6.023 \times 10^{23}} \times \Delta P_{\mu \text{bar}} \]  

(B-6)

Now for the gas created per unit time (grams per second), look to how fast the etch removes the silicon volume and the ratio of moles of etch product to moles of substrate:

\[ G = \frac{R A \rho}{M_s n} \times \frac{1}{6 \times 10^5} \]  

(B-7)

Where, R is the etch rate in microns per minute, A is the area being etched in square cm, \( \rho \) is the density of the substrate in grams per cubic centimeter, \( M_s \) is the molecular weight of the substrate, and \( n \) is previously mentioned ratio. The numerical term is a conversion term of cm to microns and seconds to minutes. Since this generation rate needs to equal the gas flow rate, we can equate the two equations and solve for the differential pressure:

\[ \Delta P_{\mu \text{bar}} = \frac{3}{8} \times \frac{1}{a} \sqrt{T \times M_p} \times \frac{6.023 \times 10^{23}}{2.625 \times 10^{19}} \times \frac{R A \rho}{6M_s n} \times 10^{-5} \]  

(B-8)

Assuming that the area remains constant for the etch, the integral simplifies down.

\[ \Delta P_{\mu \text{bar}} = \frac{3824.12}{k'} \times R \rho n \sqrt{T \times M_p} \]  

(B-9)

\[ k' = \frac{8 a}{3} \]  

(B-10)

There remains a conductance modification which accounts for the probability that a molecule incident on one end of the conduction path will actually exit the path which is
dependent on the a/l term. For this reason, the conductance term $k'$ is converted to $k$ and is typically tabulated in texts. Recall that this equation is valid for either a square or circular area. After conversion of the pressure difference to Torr:

$$\Delta P_{\text{Torr}} = \frac{2.868236 \times 10^{-5}}{k} \times R \rho n \sqrt{\frac{T + M_p}{M_s}}$$ (B-11)

This result agrees with Coburn and Winters [Coburn 1989]. Several aspect ratio to factor $k$ conversions are listed here for convenience: 5-0.210, 10-0.117, 20-0.0625, 50-0.0260. For cryogenically etching silicon, the following values are used: $n=1$, $\rho=2.3290 \text{ g/cc}$, $M_{si}=28.0855 \text{ g/mol}$, $M_{sil}=104.0719$, $T=-120^\circ \text{C} = 153.15 \text{K}$ and $R=1 \text{ micron/minute}$. Under these conditions figure A1.

---

**Fig A.1** Pressure difference from between the bottom of the etched channel and the chamber.
Although the high aspect ratio trenches do indeed build up a pressure difference, this is only part of the problem. Calculation of the mean free path of the SiF₄ gas particle should be looked at as well. Further, Knudsen relied on the assumption that the pressure was significantly low enough for the system to be under molecular flow. So looking at the mean free path assuming a Maxwellian distribution:

\[ l = \frac{K_B T}{\sqrt{2 \pi n d^2 P}} \] (B-12)

Where \( d \) is the diameter of the gas molecule, approximately 200 pm for SiF₄, and \( P \) is the pressure of the system. Under these approximations the mean free path of the etch product in 10 mTorr is 22.3 cm. This implied that the addition of 4 mTorr will not act as a significant pressure to scatter outgoing or incoming molecules (radicals or neutrals).

**Appendix C – Notching Effect in Cryogenic Etching**

Notching is what is referred to when a gentle curvature exists at the top of a cryogenically etched structure. This notching can limit the etch height of very small features, such as a 5 micron diameter pillar, well before the etch mask begins eroding. This notching is not the same as lateral etching, where the entire etched wall is etched horizontally, but instead is characterized by very straight and vertical sidewall except for the top few microns of the structure.

![Fig A.2 Scanning electron micrographs of 5 micron width silicon ridges. The left image was a silicon ridge 5.105 microns wide, 530 nm undercut, and etched for 20 min, middle was a silicon ridge 5.018 microns, 1.165 microns, and 40 min, and the right image was a silicon ridge 5.338 microns, 2.1495 microns, and 60 minutes.](image-url)
To date, the exact nature of notching is unknown. Two possible candidates are IADF and localized heating. Since IADF implies that there will always be some lateral etching due to ions approaching the surface with some parallel velocity vector, as the trench aspect ratio increases the number of ions with lateral velocity vectors striking the sidewall decreases. For this reason, an hour glass shape is expected at the top of the sidewall. Localized heating refers to the fact that the top of the etched structure is exposed to a constant thermal flux from the plasma. This thermal flux is expected to transit through the silicon to the cooled etch table. If the surface area of the etched structure is small, then as the etch height increases the thermal resistance also increases. To accommodate a constant flux of thermal energy, this implies that the temperature at the top of the etched structure should rise in temperature. A rise in temperature has been demonstrated earlier to reduce the passivation which could explain the hourglass shape. This phenomenon is unique to cryogenic etching; in fact for the same DC bias this notching does not arise with the pseudo Bosch etching. Since both etches are based on passivation, it is hypothesized that the basis of the notching is due to the thin SiO$_x$F$_y$ passivation layer.

Thermal heating is caused by 2 basic events: ionic bombardment energy flux and chemical reaction heating from the etching process. Since this problem is based on the idea that the heating starts at the top of the etched structure, it is assumed that there is no chemical reaction occurring with the etch mask and impinging ions. To calculate the ion bombardment flux, one assumes that the SiF$_4$ leaving a Si carrier wafer (unmasked) is due to F ions impinging on the surface. Based on the fact that the cryogenic etch is more radial etching and less ion etching, this assumption over accounts in energy by a factor of several thousand. This over account of the ion flux will generate a higher than actual temperature, but as it will be seen to be navigable. For a given etch rate, the number of incoming fluorine ions is calculated to:

$$G_{SiF_4} = \frac{R \cdot A \cdot \rho_{si}}{M_{Si}}$$

Where R is the etch rate, A is the area of the wafer, $\rho_{si}$ is the density of silicon and $M_{si}$ is the molar weight of silicon. Then by associating all the fluorine flux attacking the surface as the ion flux is:
\[ J_{Fions} = 4 \times \frac{R_{[\text{microns min}]} \times \rho_{\text{Si}}[\text{g cm}^{-3}] \times N_A[\text{ions mol}^{-1}] \times q[\text{C ion}]}{6 \times 10^5[\text{microns sec}^{-1}] \times M_{\text{Si}}[\text{g mol}^{-1}]} \]

Calculation of the ionic bombardment energy flux is:

\[ \frac{H}{\text{Area}} = J_{Fions} \times V_{\text{DC Bias}} \]

Then using Newton’s Law of cooling:

\[ H = \frac{dQ}{dt} = k \times A \times \frac{dT}{dx} \]

\[ \frac{H}{A} = k \times \frac{dT}{dx} \]

Substitution of the energy flux into the equation:

\[ \frac{dT}{dx} = \frac{J_{Fions} \times V_{\text{DC Bias}}}{k} \]

For a 1.14 micron per minute etch rate, the ion current density is 61 mA per cm².

Using a DC Bias of 40 volts, the energy flux is 2.44 W per cm². This means that the vertical temperature change along an etched structure per micron is 0.165*10⁻³ C per micron. This would not be enough to affect the passivation, hence the likely explanation for the undercutting is IADF.
Appendix D – Mathematica Code for Microcoil Calculations

- \( \text{gamma} = 2.673222 \times 10^8; \text{Ns} = 6.66576567 \times 10^{24}; \text{hbar} = \frac{6.626 \times 10^{-34}}{2 \pi}; \text{spin} = 1/2; \text{Bo} = 1.15; \)
- \( \mu = 4 \pi \times 10^{-7}; \omega = \text{gamma} \times \text{Bo}; \delta = 70 \times 10^{-6}; \text{P} = 1.72 \times 10^{-5}; \text{K} = 1.3806503 \times 10^{-23}; \text{T} = 300; \omega_c = 40 \times 10^{-6}; \text{h} = 15 \times 10^{-5}; \omega_d = 9.4 \times 10^{-5}; \text{bw} = 10000; \)
- \( \text{Ho} = \frac{\text{Ns} \times \text{gamma}^2 \times \text{hbar}^2 \times \text{spin} \times (\text{spin} - 1) \times \text{Bo}}{3 \times \pi \times T} \)

Radius = 250 \times 10^{-6}; \text{turns} = 1;

\[
\text{Bz}[\text{R}, \text{r}, \text{rho}, \text{N}] := \sum_{\text{n}=0}^{\text{N}} \left[ \frac{\mu}{\sqrt{((\text{R} + \delta \times \text{n}) + \rho)^2 + (\text{z})^2}} \right] \left[ \frac{4 \times (\text{R} + \delta \times \text{n})^2 \times \rho}{((\text{R} + \delta \times \text{n}) - \rho)^2 + (\text{z})^2} \right] \left[ \frac{\text{EllipticK}\left[\frac{4 \times (\text{R} + \delta \times \text{n})^2 \times \rho}{((\text{R} + \delta \times \text{n}) - \rho)^2 + (\text{z})^2}\right]}{\text{EllipticK}\left[\frac{\text{EllipticK}\left[\frac{4 \times (\text{R} + \delta \times \text{n})^2 \times \rho}{((\text{R} + \delta \times \text{n}) - \rho)^2 + (\text{z})^2}\right]}{((\text{R} + \delta \times \text{n}) - \rho)^2 + (\text{z})^2}\right]} \right]
\]

\[
\text{Noise}[\text{R}, \text{N}] := \sqrt{4 \pi \times 7 \times \text{h} \times \text{Bo} \times \sum_{\text{n}=0}^{\text{N}} \left[ \frac{2 \times \pi \times (\text{R} + \delta \times \text{n})}{(2 \times \pi \times \text{d}) \times (\text{h})} \right]}
\]

\[
\text{Resistance}[\text{R}, \text{N}] := \sum_{\text{n}=0}^{\text{N}} \left[ \frac{2 \times \pi \times (\text{R} + \delta \times \text{n})}{(2 \times \pi \times \text{d}) \times (\text{h})} \right]
\]

- \( \text{SNR} = \frac{\omega \times \text{Ho} \times \text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]]}{\text{Noise}[\text{Radius}, \text{turns}]} \)

Signal = \( \omega \times \text{Ho} \times \text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]]} \)

\text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]} \]

Resistance[\text{Radius}, \text{turns}]

- Clear[\text{turns}]; \text{turns} = 2;

\[
\text{SNR} = \frac{\omega \times \text{Ho} \times \text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]]}{\text{Noise}[\text{Radius}, \text{turns}]} \)

Signal = \( \omega \times \text{Ho} \times \text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]]} \)

\text{NIntegrate}[\text{Bz}[\text{Radius}, \text{height}, \text{radius}, \text{turns}], \text{[height, 5 \times 10^{-6}, 24 \times 10^{-6}], [radius, 0, \text{Radius} - 20 \times 10^{-6}]} \]

Resistance[\text{Radius}, \text{turns}]

Appendix E – Effect of Point Contacts on Resistance

This calculation was first performed as a homework problem I had for an electromagnetic physics course and the problem hypothetical. However, the theoretical framework is quite powerful and versatile. After spending time in industry trying to calculate how the location of where bond wires attach to a semiconductor can change the intended resistance, I realized at once that this was the method to achieve a closed form solution I was looking for. This answer can also serve as what happens when a probe tip makes contact on a wire run, or if wire runs change from very thin to thick wire runs. At the end of this appendix, modifications are discussed for using the solutions for applicability to silicon nanowires.

Begin with the basic electrostatic equations:

\[ \nabla \times \vec{E} = 0, \quad \vec{E} = \rho \cdot \vec{J}, \quad \nabla \cdot \vec{J} = 0 \]

Then if we assume the sheet is essentially a surface current, requiring the assumption that it is longer and wider than it is thick, then \( \vec{J} \) is replaced with a \( K/t \) (the \( t \) will be implicit regarding the symbol \( K \)). At this point a \( \phi \) is created, in a similar fashion as one might define a fictitious vector potential, and utilized in the equations:

\[ \hat{z} \times \nabla \phi = K = -\partial_y \phi \hat{x} + \partial_x \phi \hat{y} \]

\[ \nabla \times \vec{E} = (\partial_x E_y - \partial_y E_x) \hat{z} = (\rho_y \cdot \partial_x K_y - \rho_x \cdot \partial_y K_x) \hat{z} = 0 \]

\[ \rho_y \cdot \partial_x^2 \phi + \rho_x \cdot \partial_y^2 \phi = 0 \]

This 2-D partial differential equation is solvable by separation of variables, \( \phi = f(x)g(y) \):
The solutions to the now ordinary differential equations are also classical:

\[ f(x) = c_3 \sin(mx) + c_4 \cos(mx) \]

\[ g(y) = c_1 \sinh \left( \frac{\rho_y}{\rho_x} my \right) + c_2 \cosh \left( \frac{\rho_y}{\rho_x} my \right) \]

As with all problems, the interesting things happen when boundary conditions are applied. Assume that a bond wire connects up at \( x=0 \) and \( y=w/2 \) and at \( x=l \) and \( y=w/2 \) for a sheet that is \( w \) wide and \( l \) long and the corner of the sheet is situated at \( x=0 \). A second assumption is that the current \( I \) is injected from the bond wires.

\[ K_x(x = 0, l) = 0 \text{ and } K_y(y = 0, w) = 0 \]

\[ K_y \delta \left( x = 0, l, y = \frac{w}{2} \right) = -\frac{l}{2} \text{ and } K_x \cdot \delta(x = 0, l, y = \frac{w}{2}) = -l \]

Translating the BC for the vector potential gives:

\[ \partial_y \phi(x = 0, l) = 0 \text{ and } \partial_x \phi(y = 0, w) = 0 \]

\[ f(x = 0) = 0 + c_4 \cos(mx) = 0, \text{ so } c_4 = 0 \]

\[ f(x = l) = c_3 \sin(ml) = 0, \text{ so } m = \frac{n\pi}{l} \text{ for } n = 0, 1, 2, \ldots \]

\[ g(y = 0) = 0 + c_2 \cos h(0) = 0, \text{ so } c_2 = 0 \]

Looking at the delta function with some symmetry (half the current flows upward and half the current flows downward at \( y=w/2 \) at the contact),

\[ \int_0^w K_x \, dx = -\frac{l}{2} \text{ implies } f(x)g \left( y = \frac{w}{2} \right) = -\frac{l}{2} \]

So,

\[ g \left( y = \frac{w}{2} \right) = -\frac{l}{2} = c_1 \sinh \left( \frac{\rho_y n\pi w}{\rho_x l/2} \right), \text{ so } c_1 = -\frac{l}{2 \sinh \left( \frac{\rho_y n\pi w}{\rho_x l/2} \right)} \]

And hence,
\[ \phi(x,y) = -c_3 \sin\left(\frac{n\pi}{l}x\right) \cdot \frac{I \cdot \sinh\left(\frac{\rho_y n\pi y}{\sqrt{\rho_x l}}\right)}{2\sinh\left(\frac{\rho_y n\pi w}{\sqrt{\rho_x (l + Z)}}\right)} \]

Since there could be an infinite number of solutions to satisfy \( \phi \),

\[ \phi(x,y) = \sum_n c_n \sin\left(\frac{n\pi}{l}x\right) \cdot \frac{\sinh\left(\frac{\rho_y n\pi y}{\sqrt{\rho_x l}}\right)}{\sinh\left(\frac{\rho_y n\pi w}{\sqrt{\rho_x l + Z}}\right)} \]

\[ \phi\left(x, y = \frac{w}{2}\right) = \sum_n c_n \sin\left(\frac{n\pi}{l}x\right) = -\frac{I}{2} \]

Now applying Fourier’s trick (multiply both sides by a similar \( \sin \) function and integrating over the space):

\[ \int_0^l \sum_n c_n \sin\left(\frac{n\pi}{l}x\right) \cdot \sin\left(\frac{m\pi}{l}x\right) dx = \int_0^l -\frac{I}{2} \cdot \sin\left(\frac{m\pi}{l}x\right) dx \]

\[ c_m \cdot \frac{1}{2} = -\frac{I}{2} \cdot \frac{l}{m\pi} (\cos(m\pi) - 1) \]

\[ c_m = \frac{1}{m\pi} (1 - \cos(m\pi)) \]

\[ \phi(x,y) = \sum_n \frac{1}{m\pi} \left(1 - \cos(n\pi)\right) \cdot \sin\left(\frac{n\pi}{l}x\right) \cdot \frac{\sinh\left(\frac{\rho_y n\pi y}{\sqrt{\rho_x l}}\right)}{\sinh\left(\frac{\rho_y n\pi w}{\sqrt{\rho_x l + Z}}\right)} \]

Going back to the surface current:

\[ K_x = -\partial_y \phi \]

\[ K_x = \sum_n -\frac{\rho_y l}{\sqrt{\rho_x l}} \left(1 - \cos(m\pi)\right) \cdot \sin\left(\frac{n\pi}{l}x\right) \cdot \frac{\cosh\left(\frac{\rho_y n\pi y}{\sqrt{\rho_x l}}\right)}{\sinh\left(\frac{\rho_y n\pi w}{\sqrt{\rho_x l + Z}}\right)} \]

Now finding the voltage drop across the sheet (note that \( t \) is the thickness of the sheet to convert from J to K/t:}
\[ V = -\int_0^l E_x \cdot dx = \int_0^l \rho_x \cdot \frac{1}{t} \cdot \sum_n \sqrt{\frac{\rho_y}{\rho_x}} \cdot l \cdot (1 - \cos(m\pi)) \cdot \sin\left(\frac{n\pi}{l} \cdot x\right) \cdot \frac{\cosh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}{\sinh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)} \cdot dl \]

\[ V = \sum_n \frac{1}{n\pi} \cdot \frac{1}{t} \cdot \sqrt{\rho_x \rho_y} \cdot l \cdot (1 - \cos(n\pi))^2 \cdot \frac{\cosh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}{\sinh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)} \]

Dividing by the injected current yields the resistance:

\[ R = \sum_n \frac{1}{n\pi} \cdot \frac{1}{t} \cdot \sqrt{\rho_x \rho_y} \cdot (1 - \cos(n\pi))^2 \cdot \frac{\cosh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}{\tanh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)} \]

The function of the t in the equation, serves to change the sheet resistance to a resistance. Comparison of the modified resistance to what was expected and assuming an isotropic resistivity:

\[ \Delta R = \left(\sum_n \frac{1}{n\pi} \cdot \frac{1}{t} \cdot \rho \cdot (1 - \cos(n\pi))^2 \cdot \frac{\cosh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}{\tanh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}\right) - \frac{\rho l}{tw} \]

\[ \text{error factor} = \frac{\Delta R}{R} = \sum_n \frac{1}{n\pi \cdot AR} \cdot (1 - \cos(n\pi))^2 \cdot \frac{\cosh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)}{\tanh\left(\frac{\rho_y \cdot n\pi \cdot w}{\sqrt{\rho_x \cdot \frac{l}{2}}}\right)} - 1 \]

Fig A.3 Plot of error factor in resistance (delta R / R) due to contacting the structure with a point contact. As the aspect ratio gets large, the effect of the contact diminishes quickly.


